

#### HIGGS THEORY OVERVIEW

- ➤ Slides from 3 to 20 pages
- > You may skip them

A few basics on Lagrangians

$$\mathcal{L} = T(\text{kinetic}) - V(\text{potential})$$

The Euler-Lagrange equation brings the equation of motion

$$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = 0$$

$$\mathcal{L}_{\text{scalar}} = \frac{1}{2} \left( \partial_{\mu} \phi \right) \left( \partial^{\mu} \phi \right) - \frac{1}{2} m^{2} \phi^{2} \rightarrow \text{Euler-Lagrange} \rightarrow \underbrace{\left( \partial_{\mu} \partial^{\mu} + m^{2} \right) \phi = 0}_{\text{Klein-Gordon equation}}$$

In general, the Lagrangian for a real scalar particle  $(\phi)$  is given by:

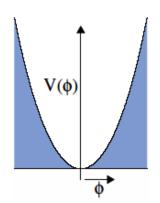
$$\mathcal{L} = \underbrace{(\partial_{\mu}\phi)^{2}}_{\text{kinetic term}} + \underbrace{\beta\phi^{2}}_{\text{mass term}} + \underbrace{\gamma\phi^{3}}_{\text{3-point int.}} + \underbrace{\delta\phi^{4}}_{\text{4-point int.}}$$

A real scalar field

$$\mathcal{L} = \frac{1}{2} (\partial_{\mu} \phi)^2 - V(\phi)$$
$$= \frac{1}{2} (\partial_{\mu} \phi)^2 - \frac{1}{2} \mu^2 \phi^2 - \frac{1}{4} \lambda \phi^4$$

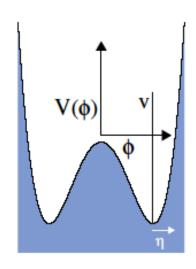
 $\mathcal{L}$  is symmetric under  $\phi \rightarrow -\phi$ 

For  $\mu^2 > 0$ , the minimum (vacuum) is at  $\phi = 0$ 



$$\mathcal{L} = \underbrace{\frac{1}{2}(\partial_{\mu}\phi)^{2} - \frac{1}{2}\mu^{2}\phi^{2}}_{\text{free particle, mass }\mu} \underbrace{-\frac{1}{4}\lambda\phi^{4}}_{\text{interaction}}$$

For  $\mu^2$  < 0, introducing a particle with imaginary mass?



$$\phi_0 = \sqrt{-\frac{\mu^2}{\lambda}} = v \quad \text{or} \quad \mu^2 = -\lambda v^2$$

> To study a particle spectrum, we look at an excited state (near ground state),  $\eta = \phi - v$ .

 $\succ$  Rewriting the Lagrangian in terms of  $\eta$ 

Kinetic term: 
$$\mathcal{L}_{kin}(\eta) = \frac{1}{2}(\partial_{\mu}(\eta + v)\partial^{\mu}(\eta + v))$$
  
=  $\frac{1}{2}(\partial_{\mu}\eta)(\partial^{\mu}\eta)$  , since  $\partial_{\mu}v = 0$ .

Potential term: 
$$\begin{aligned} \mathrm{V}(\eta) &=& +\frac{1}{2}\mu^2(\eta+v)^2 + \frac{1}{4}\lambda(\eta+v)^4 \\ &=& \lambda v^2\eta^2 + \lambda v\eta^3 + \frac{1}{4}\lambda\eta^4 - \frac{1}{4}\lambda v^4, \end{aligned}$$
 we used  $\mu^2 = -\lambda v^2$ 

➤ Symmetry is broken → spontaneous symmetry breaking.

$$V(-\eta) \neq V(\eta)$$

Full Lagrangian

$$\mathcal{L}(\eta) = \frac{1}{2} (\partial_{\mu} \eta)(\partial^{\mu} \eta) - \lambda v^2 \eta^2 - \lambda v \eta^3 - \frac{1}{4} \lambda \eta^4 - \frac{1}{4} \lambda v^4$$

This describe the kinematics for a massive scalar particle

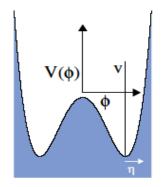
$$\frac{1}{2}m_{\eta}^2 = \lambda v^2 \to m_{\eta} = \sqrt{2\lambda v^2} \quad \left(=\sqrt{-2\mu^2}\right) \quad \text{Note: } m_{\eta} > 0.$$

- Adding a particle with imaginary mass with a four-point self-interaction, thus we examine the particle spectrum using perturbation around the vacuum
  - We find that it actually describes a massive scalar particle (real, positive mass) with three- and four-point self interactions.
  - The vacuum is not symmetric in the field η though the Lagrangian is symmetric in φ → spontaneous symmetry breaking.

- ➤ The Universe is filled with a spin-zero field, a Higgs field that is a doublet in the SU(2) space and carries non-zero U(1) hypercharge but a singlet in color space
- Spontaneous Symmetry Breaking
- A real scalar field

$$\mathcal{L} = \frac{1}{2} (\partial_{\mu} \phi)^2 - V(\phi)$$
$$= \frac{1}{2} (\partial_{\mu} \phi)^2 - \frac{1}{2} \mu^2 \phi^2 - \frac{1}{4} \lambda \phi^4$$

 $\mathcal{L}$  is symmetric under  $\phi \rightarrow -\phi$ 



$$\begin{split} \mathcal{L}(\eta) &= \frac{1}{2}(\partial_{\mu}\eta)(\partial^{\mu}\eta) - \lambda v^2\eta^2 - \lambda v\eta^3 - \frac{1}{4}\lambda\eta^4 - \frac{1}{4}\lambda v^4 \\ \\ m_{\eta} &= \sqrt{2\lambda v^2} \end{split}$$

$$\phi_0 = \sqrt{-\frac{\mu^2}{\lambda}} = v$$

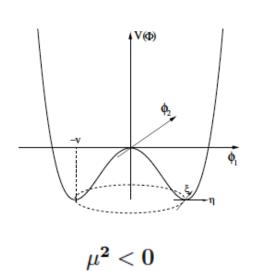
vacuum is not symmetric in the field  $\eta$ : spontaneous symmetry breaking.

#### A global symmetry

$$\mathcal{L} = (\partial_{\mu}\phi)^{*}(\partial^{\mu}\phi) - V(\phi) \qquad , \text{ with } V(\phi) = \mu^{2}(\phi^{*}\phi) + \lambda(\phi^{*}\phi)^{2}$$

$$\phi = \frac{1}{\sqrt{2}}(\phi_{1} + i\phi_{2}) \qquad U(1) \text{ global symmetry, i.e. under } \phi' \to e^{i\alpha}\phi$$

$$\mathcal{L}(\phi_{1}, \phi_{2}) = \frac{1}{2}(\partial_{\mu}\phi_{1})^{2} + \frac{1}{2}(\partial_{\mu}\phi_{2})^{2} - \frac{1}{2}\mu^{2}(\phi_{1}^{2} + \phi_{2}^{2}) - \frac{1}{4}\lambda(\phi_{1}^{2} + \phi_{2}^{2})^{2}$$



$$\sqrt{\phi_1^2 + \phi_2^2} = \sqrt{\frac{-\mu^2}{\lambda}} = v \qquad \phi_0 = \frac{1}{\sqrt{2}} (\eta + v + i\xi)$$

$$\mathcal{L}_{kin}(\eta, \xi) = \frac{1}{2} \partial_{\mu} (\eta + v - i\xi) \partial^{\mu} (\eta + v + i\xi)$$

$$= \frac{1}{2} (\partial_{\mu} \eta)^2 + \frac{1}{2} (\partial_{\mu} \xi)^2 \quad , \text{ since } \partial_{\mu} v = 0.$$

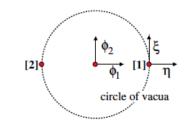
$$V(\eta, \xi) = \mu^2 \phi^2 + \lambda \phi^4$$

$$= -\frac{1}{2} \lambda v^2 [(v + \eta)^2 + \xi^2] + \frac{1}{4} \lambda [(v + \eta)^2 + \xi^2]^2$$

$$= -\frac{1}{4} \lambda v^4 + \lambda v^2 \eta^2 + \lambda v \eta^3 + \frac{1}{4} \lambda \eta^4 + \frac{1}{4} \lambda \xi^4 + \lambda v \eta \xi^2 + \frac{1}{2} \lambda \eta^2 \xi^2$$

A global symmetry

$$\mathcal{L}(\eta,\xi) = \underbrace{\frac{1}{2}(\partial_{\mu}\eta)^{2} - (\lambda v^{2})\eta^{2}}_{\text{massive scalar particle }\eta} + \underbrace{\frac{1}{2}(\partial_{\mu}\xi)^{2} + 0 \cdot \xi^{2}}_{\text{massless scalar particle }\xi} + \text{higher order terms}$$



no 'force' acting on oscillations along the  $\xi$ -field.

➤ This Lagrangian describes a massive scalar particle and a massless particle (Goldstone boson) by spontaneous symmetry breaking

#### A local symmetry

$$\mathcal{L} = (\partial_{\mu}\phi)^{*}(\partial^{\mu}\phi) - V(\phi) \qquad , \text{ with } V(\phi) = \mu^{2}(\phi^{*}\phi) + \lambda(\phi^{*}\phi)^{2}$$

$$\phi = \frac{1}{\sqrt{2}}(\phi_{1} + i\phi_{2}) \qquad \phi' \rightarrow e^{i\alpha(x)}\phi$$

$$\partial_{\mu} \rightarrow D_{\mu} = \partial_{\mu} - ieA_{\mu}$$

$$A'_{\mu} = A_{\mu} + \frac{1}{e}\partial_{\mu}\alpha \qquad \mathcal{L} = (D^{\mu}\phi)^{\dagger}(D_{\mu}\phi) - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} - V(\phi)$$

$$\mathcal{L}_{kin}(\eta, \xi) = (D^{\mu}\phi)^{\dagger}(D_{\mu}\phi)$$

$$= (\partial^{\mu} + ieA^{\mu})\phi^{*}(\partial_{\mu} - ieA_{\mu})\phi \qquad \phi_{0} = \frac{1}{\sqrt{2}}(\eta + v + i\xi)$$

$$\mathcal{L}(\eta, \xi) = \underbrace{\frac{1}{2}(\partial_{\mu}\eta)^{2} - \lambda v^{2}\eta^{2}}_{\eta\text{-particle}} + \underbrace{\frac{1}{2}(\partial_{\mu}\xi)^{2}}_{\xi\text{-particle}} - \underbrace{\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}e^{2}v^{2}A_{\mu}^{2}}_{\text{photon field}} - \underbrace{evA_{\mu}(\partial^{\mu}\xi)}_{\gamma} + \text{int.-terms}$$

$$\frac{1}{2}(\partial_{\mu}\xi)^{2} - evA^{\mu}(\partial_{\mu}\xi) + \frac{1}{2}e^{2}v^{2}A_{\mu}^{2} = \frac{1}{2}e^{2}v^{2}\left[A_{\mu} - \frac{1}{ev}(\partial_{\mu}\xi)\right]^{2} = \frac{1}{2}e^{2}v^{2}(A_{\mu}')^{2}$$

$$\phi' \to e^{-i\xi/v}\phi = e^{-i\xi/v}\frac{1}{\sqrt{2}}(v+\eta+i\xi) = e^{-i\xi/v}\frac{1}{\sqrt{2}}(v+\eta)e^{+i\xi/v} = \frac{1}{\sqrt{2}}(v+h)$$

$$\mathcal{L}_{\text{scalar}} = \underbrace{\frac{1}{2}(\partial_{\mu}h)^{2} - \lambda v^{2}h^{2}}_{\text{massive scalar}} + \underbrace{\frac{1}{2}e^{2}v^{2}A_{\mu}^{2}}_{\text{gauge field }(\gamma)} + \underbrace{e^{2}vA_{\mu}^{2}h + \frac{1}{2}e^{2}A_{\mu}^{2}h^{2}}_{\text{interaction Higgs}} - \underbrace{\lambda vh^{3} - \frac{1}{4}\lambda h^{4}}_{\text{Higgs self-}}$$

particle h with mass and gauge fields

- > A mass term for the gauge boson and a massive scalar particle.
- Goldstone boson of the previous section has become the longitudinal polarization state of the gauge boson

interactions

#### The Higgs Mechanism

Breaking the local gauge invariant  $SU(2)_L \times U(1)_Y$  symmetry

$$\phi = \begin{pmatrix} \phi^{+} \\ \phi^{0} \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_{1} + i\phi_{2} \\ \phi_{3} + i\phi_{4} \end{pmatrix}$$

$$\mathcal{L}_{\text{scalar}} = (D^{\mu}\phi)^{\dagger} (D_{\mu}\phi) - V(\phi), \qquad D_{\mu} = \partial_{\mu} + ig\frac{1}{2}\vec{\tau} \cdot \vec{W}_{\mu} + ig'\frac{1}{2}YB_{\mu}$$

$$\text{Vacuum} = \phi_{0} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} \qquad \phi_{1} = \phi_{2} = \phi_{4} = 0$$

$$\phi_{3} = v$$

$$\text{SU}(2)_{L}: \quad \tau_{1}\phi_{0} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} = +\frac{1}{\sqrt{2}} \begin{pmatrix} v+h \\ 0 \end{pmatrix} \neq 0 \rightarrow \text{broken}$$

$$\tau_{2}\phi_{0} = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} = -\frac{i}{\sqrt{2}} \begin{pmatrix} v+h \\ 0 \end{pmatrix} \neq 0 \rightarrow \text{broken}$$

$$\tau_{3}\phi_{0} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} = -\frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} \neq 0 \rightarrow \text{broken}$$

$$\text{U}(1)_{Y}: \quad Y\phi_{0} = \qquad Y_{\phi_{0}} \quad \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} = +\frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} \neq 0 \rightarrow \text{broken}$$

Un-ki Yang, KCMS Collider Lecture

#### The Higgs Mechanism

$$W_1$$
  $W_2$   $W_3$   $B$   $W^+$  and  $W^-$  bosons Z-boson and  $\gamma$ 

$$U(1)_{EM}: Q\phi_0 = \frac{1}{2}(\tau_3 + Y)\phi_0 = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix} = 0 \to unbroken$$

- W<sub>1</sub> and W<sub>2</sub> mix and will form the massive a W<sup>+</sup> and W<sup>-</sup> bosons.
- 2)  $W_3$  and B mix to form massive Z and massless  $\gamma$ .
- 3) Remaining degree of freedom will form the mass of the scalar particle (Higgs boson)

$$\mathcal{L}_{\text{scalar}} = (D^{\mu}\phi)^{\dagger}(D_{\mu}\phi) - V(\phi)$$

$$D_{\mu}\phi = \left[\partial_{\mu} + ig\frac{1}{2}\vec{\tau} \cdot \vec{W}_{\mu} + ig'\frac{1}{2}YB_{\mu}\right] \frac{1}{\sqrt{2}} \begin{pmatrix} 0\\ v+h \end{pmatrix}$$

## The Higgs Mechanism

- 1) Masses for the gauge bosons ( $\propto v^2$ )
- 2) Interactions gauge bosons and the Higgs  $(\propto vh)$  and  $(\propto h^2)$

$$(D^{\mu}\phi)^{\dagger} (D_{\mu}\phi) = \frac{1}{8}v^{2} \left[ g^{2}(W_{1}^{2} + W_{2}^{2}) + (-gW_{3} + g'Y_{\phi_{0}}B_{\mu})^{2} \right]$$

$$g^{2}(W_{1}^{2} + W_{2}^{2}) = g^{2}(W^{+2} + W^{-2})$$

$$(-gW_{3} + g'Y_{\phi_{0}}B_{\mu})^{2} = (g^{2} + g'^{2})Z_{\mu}^{2} + 0 \cdot A_{\mu}^{2}$$

$$M_{W^{+}} = M_{W^{-}} = \frac{1}{2}vg$$

$$M_{Z} = \frac{1}{2}v\sqrt{(g^{2} + g'^{2})}$$

$$\frac{M_{W}}{M_{Z}} = \frac{\frac{1}{2}vg}{\frac{1}{2}v\sqrt{g^{2} + g'^{2}}} = \cos(\theta_{W})$$

$$M_{\gamma} = 0$$

$$m_h = \sqrt{2\lambda v^2}$$

V~246 GeV,but λ is a free parameter

#### Fermion masses

A term like  $-m\bar{\psi}\psi = -m[\bar{\psi_L}\psi_R + \bar{\psi_R}\psi_L]$  is <u>not</u> gauge invariant

left handed doublet 
$$= \chi_L \rightarrow \chi'_L = \chi_L e^{i\vec{W}\cdot\vec{T}+i\alpha Y}$$
  
right handed singlet  $= \psi_R \rightarrow \psi'_R = \psi_R e^{i\alpha Y}$ 

- a term:  $\propto \bar{\psi}_L \psi_R$  is not invariant under  $SU(2)_L \times U(1)_Y$
- a term:  $\propto \bar{\psi}_L \phi \psi_R$  is invariant under  $SU(2)_L \times U(1)_Y$

using the complex (Higgs) doublet

$$\mathcal{L}_{\text{fermion-mass}} = -\lambda_f [\bar{\psi}_L \phi \psi_R + \bar{\psi}_R \bar{\phi} \psi_L]$$

#### Lepton masses

$$\mathcal{L}_{e} = -\lambda_{e} \frac{1}{\sqrt{2}} \left[ (\bar{\nu}, \bar{e})_{L} \begin{pmatrix} 0 \\ v+h \end{pmatrix} e_{R} + \bar{e}_{R}(0, v+h) \begin{pmatrix} \nu \\ e \end{pmatrix}_{L} \right]$$

$$= -\frac{\lambda_{e}(v+h)}{\sqrt{2}} [\bar{e}_{L}e_{R} + \bar{e}_{R}e_{L}]$$

$$= -\frac{\lambda_{e}(v+h)}{\sqrt{2}} \bar{e}e$$

$$= -\frac{\lambda_{e}v}{\sqrt{2}} \bar{e}e \qquad -\frac{\lambda_{e}v}{\sqrt{2}} h\bar{e}e$$

$$= \text{electron mass term electron-higgs interaction}$$

$$m_{e} = \frac{\lambda_{e}v}{\sqrt{2}} \qquad \frac{\lambda_{e}}{\sqrt{2}} \propto m_{e}$$

- 1) The Yukawa coupling is often expressed as  $\lambda_f = \sqrt{2} \left( \frac{m_f}{v} \right)$
- 2) The mass of the electron is **not** predicted since  $\lambda_e$  is a free parameter.

$$\frac{\Gamma(h\to ee)}{\Gamma(h\to WW)} \propto \frac{\lambda_{eeh}^2}{\lambda_{WWh}^2} = \left(\frac{gm_e/2M_W}{gM_W}\right)^2 = \underbrace{\frac{m_e^2}{4M_W^4}} \approx 1.5 \cdot 10^{-21}$$

#### Quark masses

The fermion mass term  $\mathcal{L}_{\text{down}} = \lambda_f \bar{\psi}_L \phi \psi_R$  (leaving out the hermitian conjugate term  $\bar{\psi}_R \bar{\phi} \psi_L$  for clarity) only gives mass to 'down' type fermions, i.e. only to one of the isospin doublet

$$\mathcal{L}_{\rm up} = \bar{\chi}_L \tilde{\phi}^c \phi_R + \text{h.c.}, \text{ with}$$

$$\tilde{\phi}^c = -i\tau_2 \phi^* = -\frac{1}{\sqrt{2}} \begin{pmatrix} (v+h) \\ 0 \end{pmatrix}$$

down-type: 
$$\lambda_d(\bar{u}_L, \bar{d}_L)\phi d_R = \lambda_d(\bar{u}_L, \bar{d}_L) \begin{pmatrix} 0 \\ v \end{pmatrix} d_R = \lambda_d v \ \bar{d}_L d_R$$

up-type: 
$$\lambda_u(\bar{u}_L, \bar{d}_L)\tilde{\phi}^c d_R = \lambda_u(\bar{u}_L, \bar{d}_L) \begin{pmatrix} v \\ 0 \end{pmatrix} u_R = \lambda_u v \; \bar{u}_L u_R$$

## Higgs Mechanism Summary

#### Slide from Prof. I. Park

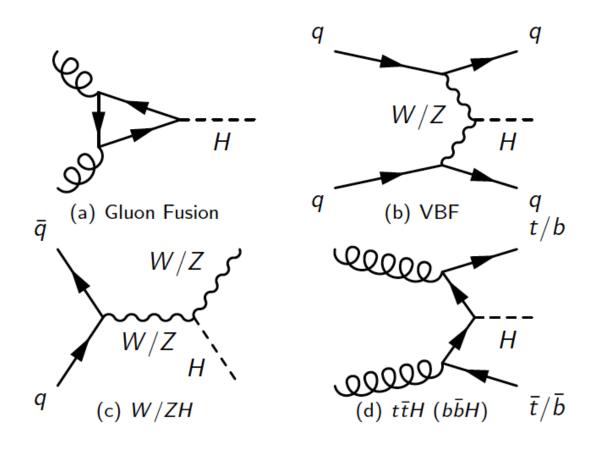
	스칼라 장	U(1)	SU(2)
라그랑지안	$\mathcal{L} = (\partial_{\mu}\phi)^2 - V(\phi)$	$\mathcal{L} = \left  (i\partial_{\mu} - q\vec{A}_{\mu})\phi \right ^2 - V(\phi)$	$\mathcal{L} = \left  (i\partial_{\mu} - g\frac{\vec{\tau}}{2} \cdot \vec{W}_{\mu})\phi \right ^2 - V(\phi)$
포텐셜	$\mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2$	$\mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2$	$\mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2$
스칼라 장	$\phi = \phi_1 + i\phi_2$	$\phi = \phi_1 + i\phi_2$	$\phi = \begin{pmatrix} \phi_1 + i\phi_2 \\ \psi_3 + i\phi_4 \end{pmatrix}$
최저점	$\phi^*\phi = \frac{1}{2}(\phi_1^2 + \phi_2^2) = v^2$	$\phi^*\phi = \frac{1}{2}(\phi_1^2 + \phi_2^2) = v^2$	$\phi^*\phi = \frac{1}{2}(\phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2) = v^2$
	$v \equiv \sqrt{-\mu^2/\lambda}$	$v \equiv \sqrt{-\mu^2/\lambda}$	$v \equiv \sqrt{-\mu^2/\lambda}$
진공	$\phi_1=v,\phi_2=0$	$\phi_1=v,\phi_2=0$	$\phi_1 = \phi_2 = \phi_4 = 0, \phi_3 = v$
좌표 이동	$\phi = \frac{1}{\sqrt{2}}(v + \eta(x) + i\xi(x))$	$\phi = \frac{1}{\sqrt{2}}(v + h(x))e^{i\theta(x)/v}$	$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix} e^{i\vec{\tau} \cdot \vec{\theta}(x)/v}$
질량	$m_{\xi} = 0$	$m_h = \sqrt{2\lambda v^2}$	$m_{\eta} = \sqrt{2\lambda v^2}$
	$m_{\eta} = \sqrt{2\lambda v^2}$	$m_A = qv$	$m_W = \frac{1}{2}gv$

## Higgs Mechanism Summary

	SU(2) x U(1)	
라그랑지안	$\mathcal{L} =  (i\partial_{\mu} - g\frac{\vec{\tau}}{2} \cdot \vec{W}_{\mu} - g'\frac{Y}{2}B_{\mu})\phi ^2 - V(\phi)$	
포텐셜	$\mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2$	
스칼라 장	$\phi = \begin{pmatrix} \phi_1 + i\phi_2 \\ \psi_3 + i\phi_4 \end{pmatrix}$	
최저점	$\phi^*\phi = \frac{1}{2}(\phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2) = v^2$	
	$v \equiv \sqrt{-\mu^2/\lambda}$	
진공	$\phi_1 = \phi_2 = \phi_4 = 0, \phi_3 = v$	
좌표 이동	$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix} e^{i\vec{\tau} \cdot \vec{\theta}(x)/v}$	
	$m_h = \sqrt{2\lambda v^2}$	
질량	$m_W = \frac{1}{2}gv$	
ਦ ਨ	$m_Z = \frac{1}{2} \sqrt{g^2 + g'^2} v$	
	$m_A = 0$	

Slide from Prof. I. Park

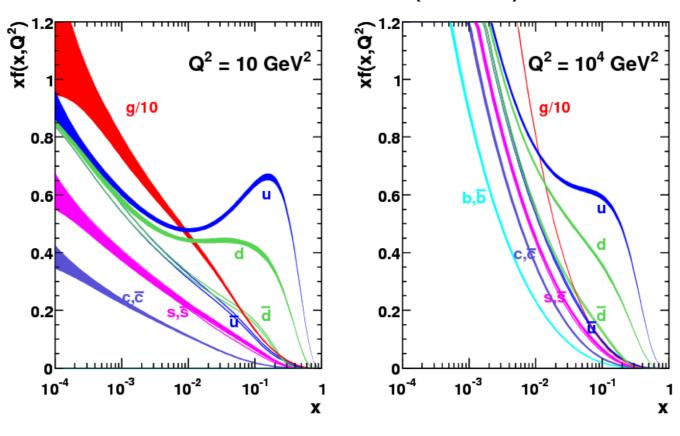
#### Higgs Production at LHC



- What process dominates?
  - depending on Higgs mass?

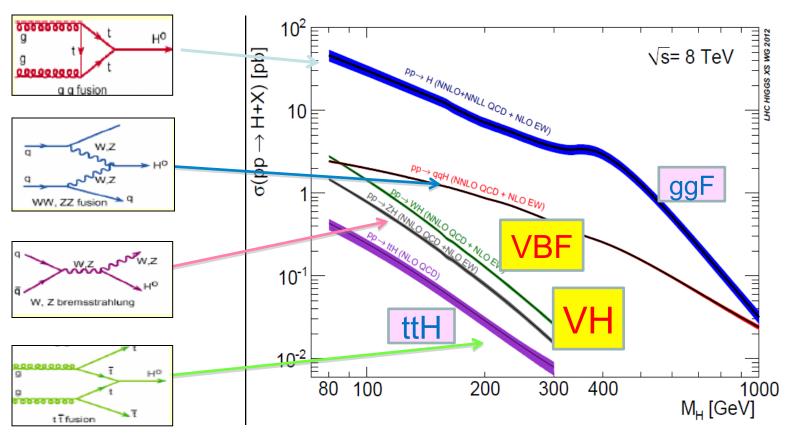
#### Parton Distributions Functions

#### MSTW 2008 NLO PDFs (68% C.L.)



$$\langle x \rangle = \frac{Q}{\sqrt{S}} \approx 0.06$$
 (Tevatron), 0.015 (LHC) for  $m_H = 125$  GeV

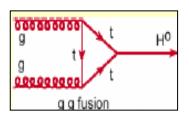
#### Higgs productions at the LHC



- → ggF: a dominant process through the top quark loop → indirect probe of Higgs-fermion coupling
- ➤ VBF: two forward jets → direct probe of vector boson coupling
- ➤ VH: signature with hi-pt leptons → direct probe of vector boson coupling
- ttH: direct probe of Higgs-top quark coupling

#### Higgs Production at Tevatron

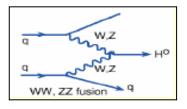
#### **Primary production modes:**



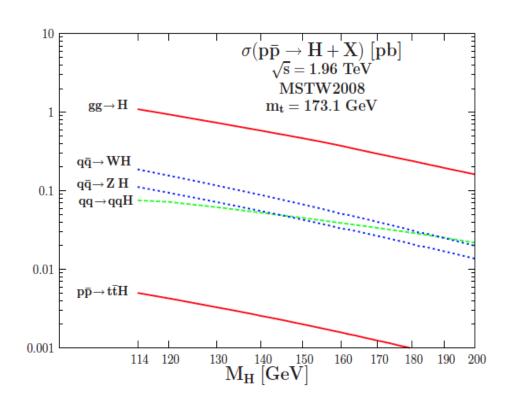
1.8~0.2 pb



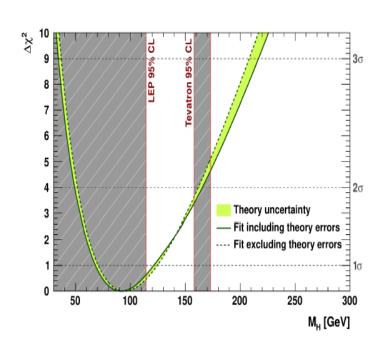
0.5~0.03 pb

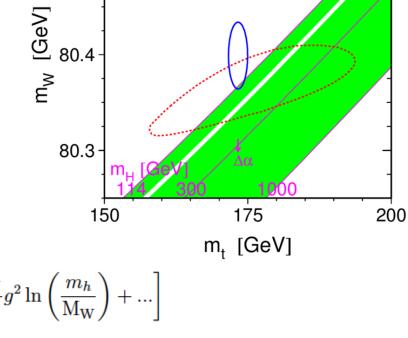


0.1~0.02 pb



#### Constraints on Higgs Before Discovery

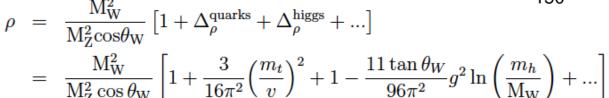




- LEP2 and Tevatron (prel.)

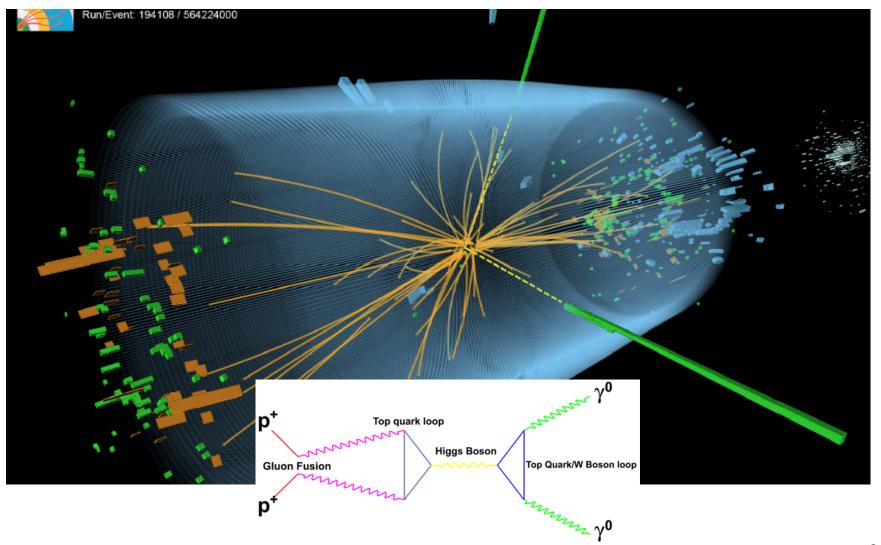
---- LEP1 and SLD

68% CL



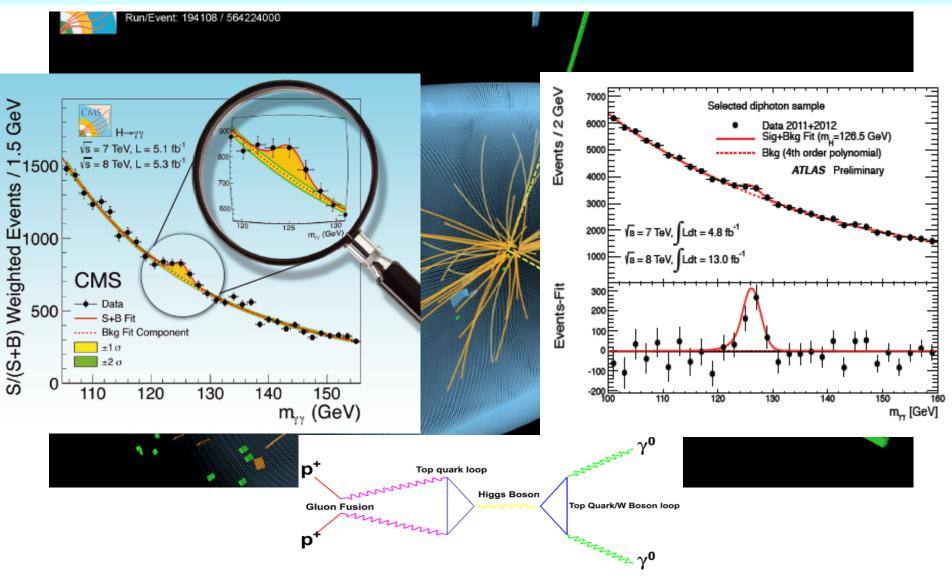
- Global EWK fits: preferred a light Higgs with large uncertainty
- LEP and Tevatron exclusions

# Discovery of a Higgs boson (2012)

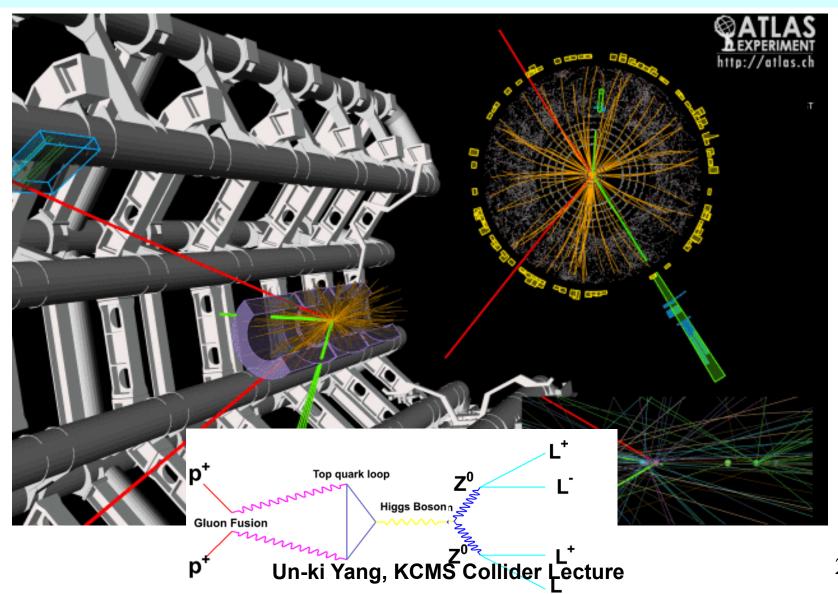


**Un-ki Yang, KCMS Collider Lecture** 

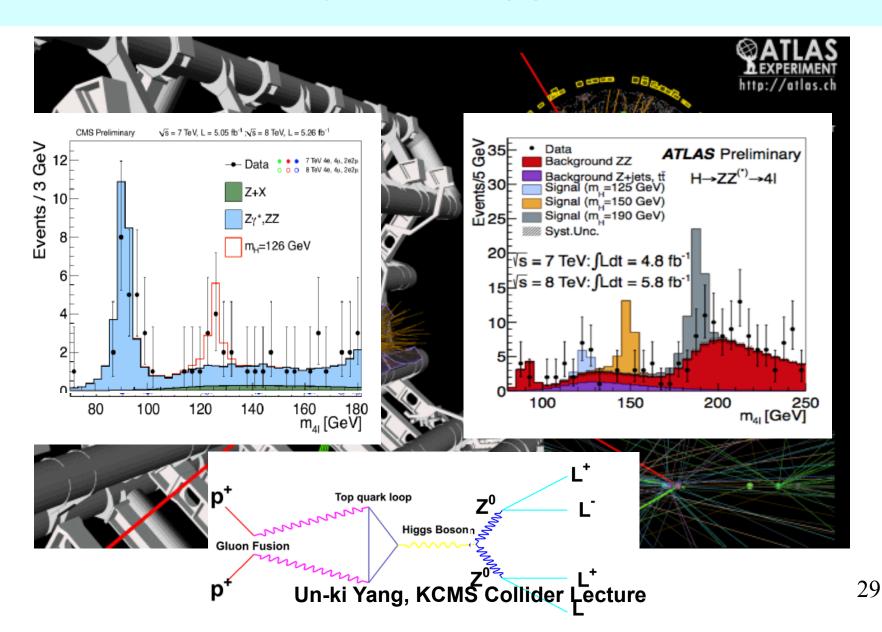
#### Discovery of a Higgs boson



# Discovery of a Higgs boson



# Discovery of a Higgs boson

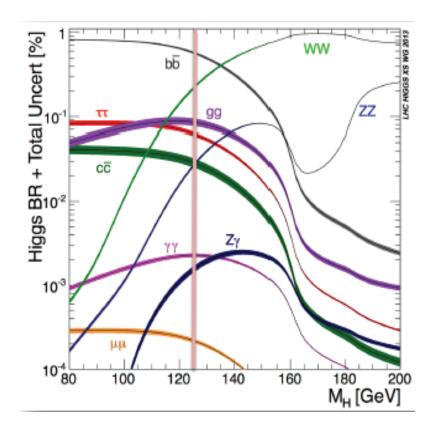


# Two of these 10,000 people presented results...



#### Higgs decays at the LHC

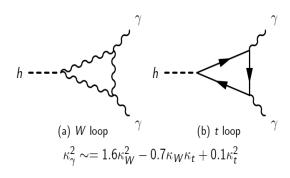
Discovery channels:  $H \rightarrow \gamma \gamma$ ,  $H \rightarrow -ZZ^* \rightarrow 40$ 



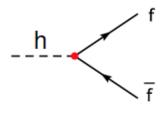
Rich decay modes at m<sub>H</sub> ~ 125 GeV

m <sub>H</sub> =125.5GeV	BR(%)
H→γγ	0.23
H→ZZ	2.8
H→WW	22
H→ τ τ	6.2
H→bb	57

- ⊢ H→γγ: decays via W or t loop: negative interference
  - → indirect measurement on couplings

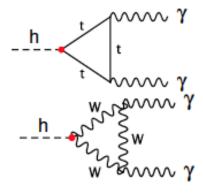


#### Higgs Decays



$$\Gamma(h \to f \bar{f}) = \frac{N_c}{8\pi v^2} \ m_f^2 \ m_h \ \sqrt{1-x}$$
 , with  $x = \frac{4m_f^2}{m_h^2}$ 

$$\Gamma(h \to VV) = \frac{g^2}{64\pi M_W^2} \ m_h^3 \ \mathcal{S}_{VV} \ (1 - x + \frac{3}{4}x^2) \sqrt{1 - x}$$
 , with  $x = \frac{4M_V^2}{m_h^2}$  and  $\mathcal{S}_{WW,ZZ} = 1, \frac{1}{2}$ .



$$\Gamma(h \to \gamma \gamma) = \frac{\alpha^2}{256\pi^3 v^2} m_h^3 \left| \frac{4}{3} \sum_f N_c^{(f)} e_f^2 - 7 \right|^2$$

, where  $e_f$  is the fermion's electromagnetic charge.

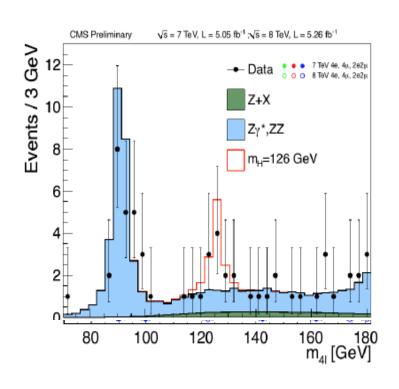
Note: - WW contribution  $\approx 5$  times top contribution

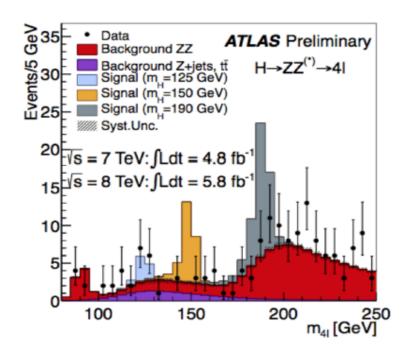
- Some computation also gives  $h \to \gamma Z$ 

#### Higgs Searches

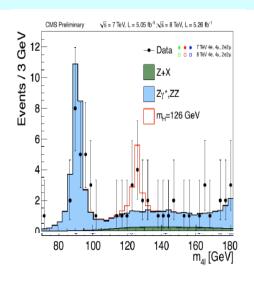
- Two special channels in the search
  - H $\rightarrow$ ZZ\* $\rightarrow$ 4l (l=e, $\mu$ ), H $\rightarrow$  $\gamma\gamma$
  - Fully reconstructed final state (no neutrinos):
     a special role in mass determination
  - Well reconstructed objects with excellent energy/momentum resolutions (only tracking and EM calorimeters)
- $\rightarrow$  H $\rightarrow$ ZZ\* $\rightarrow$ 4l (l=e, $\mu$ )
  - So small branching fraction: ~ 10<sup>-5</sup>
  - But extremely small bkgds.:
    - irreducible: ZZ→4I
    - reducible: mis-identified leptons (mostly 2 real + 2 mis-id)
  - Challenges:
    - Maximize lepton eff. & acceptance, down to low pt, 5 GeV
    - Optimize lepton resolution and estimation of mis-ID

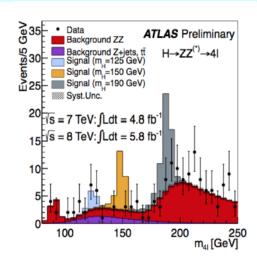
#### $H \rightarrow ZZ^* \rightarrow 4I$ (Discovery)

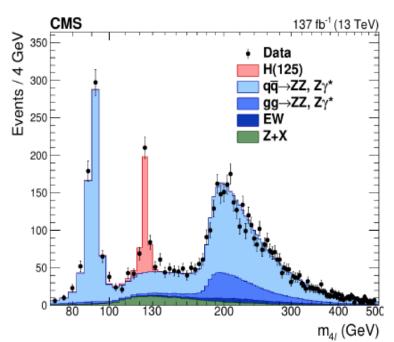


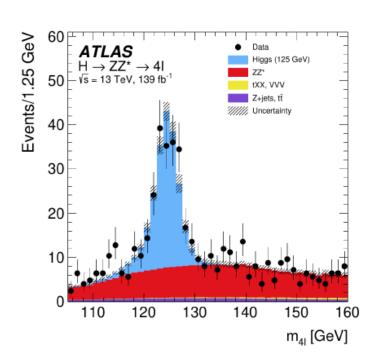


# $H \rightarrow ZZ^* \rightarrow 4I$ (Full Run II)



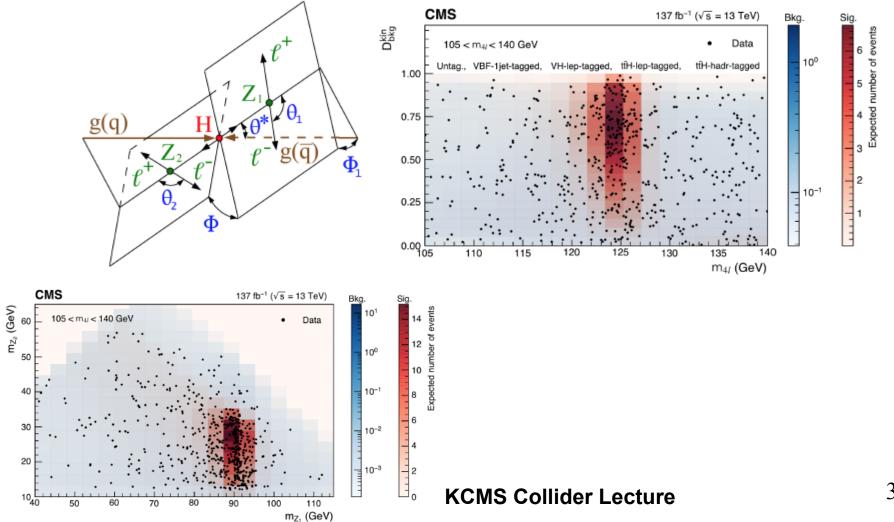






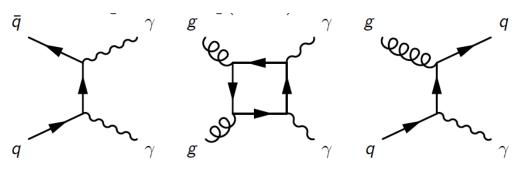
# $H \rightarrow ZZ^* \rightarrow 4I$ (Kinematics)

Masses of lepton pairs and decays angles: additional information

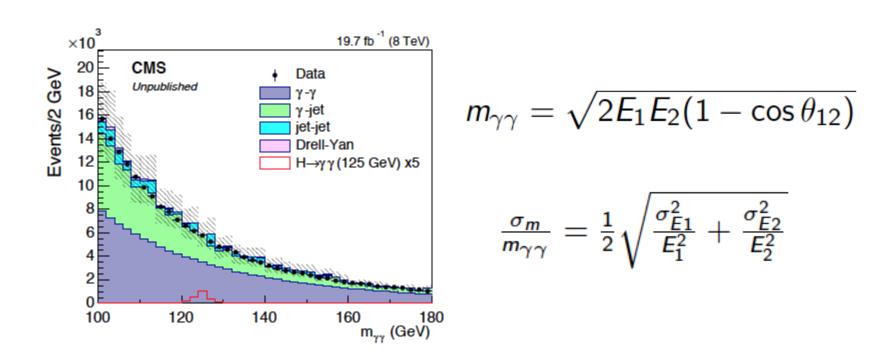


# $H \rightarrow \gamma \gamma$

- Small branching fraction: ~ 2 x10<sup>-3</sup> (larger than H→ZZ\*→4I)
- Significant bkgds.:
  - Irreducible: pp→γγ (relatively large cross section)
  - reducible:
    γ + jet with one mis-ID and multijet with two mis-IDs
  - Challenges:
    - Maximize lepton eff. & acceptance, down to low pt, 5 GeV
    - Optimize diphoton mass resolution
    - Photon ID efficiency
    - Background modelling (mass fit)

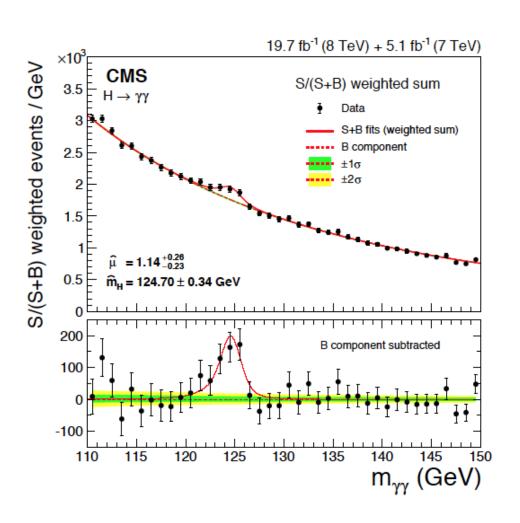


## Search for $H \rightarrow \gamma\gamma$



- Search for a small narrow mass peak on top of a large smoothly falling background
- Take an advantage of multivariate techniques to optimize the sensitivity, but basically, "bump hunt"

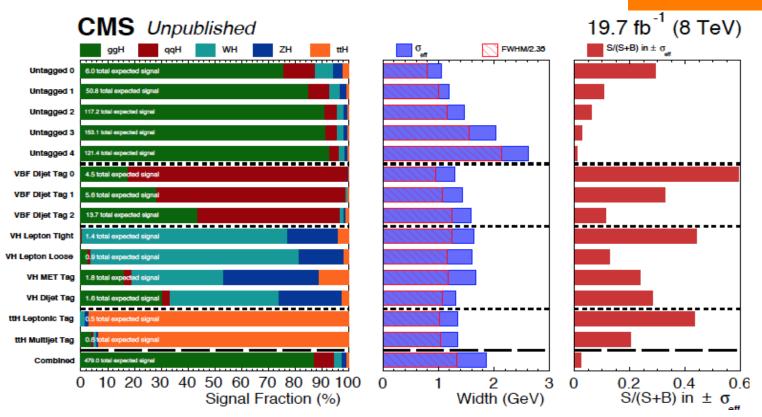
## Search for $H \rightarrow \gamma\gamma$



- Results extracted from simultaneous fit to 25 event classes, but combined mass spectrum useful for visualisation
- Combination of all 25 event classes, weighted by S/(S+B) for a  $\pm \sigma_{\it eff}$  window in each event class
- Weights are normalised to preserve the fitted number of signal events

## $H \rightarrow \gamma \gamma$ : event classification

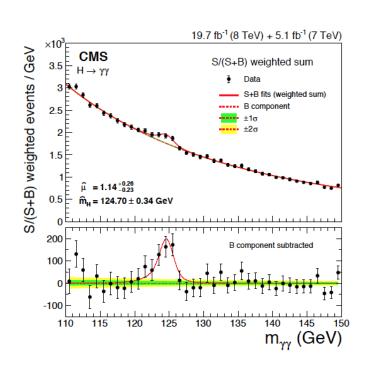
Slide from J. Bendavid

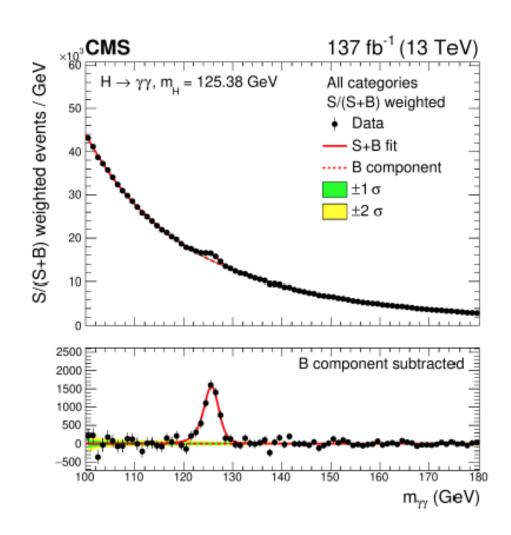


Events classified according to di-photon MVA output plus tagging of additional objects

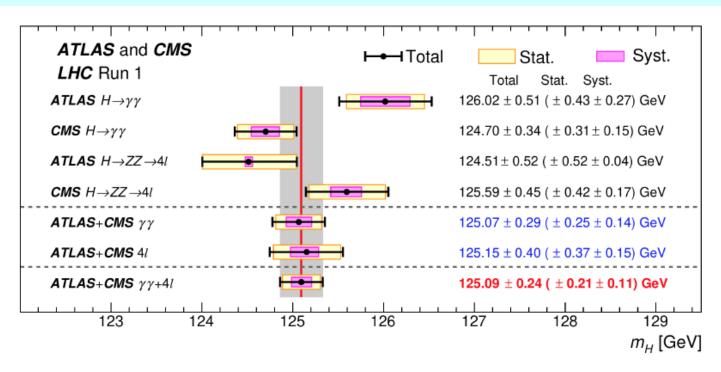
Large variation in resolution and S/B across categories

# Search for H $\rightarrow \gamma \gamma$ (full Run II)





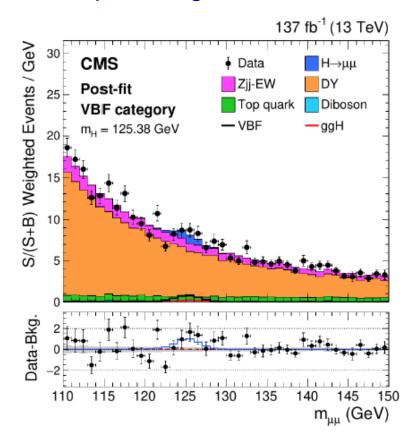
#### Higgs Mass

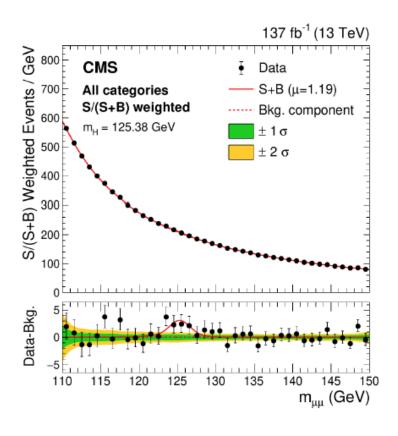


- Higgs mass is measured from the peak position in γγ and 4I
- Calibration of the photon, electron, and muon, mainly using the Z peak
- γγ channel has small statistical error, but larger systematics due to e → photon extrapolation

# Search for H → μμ

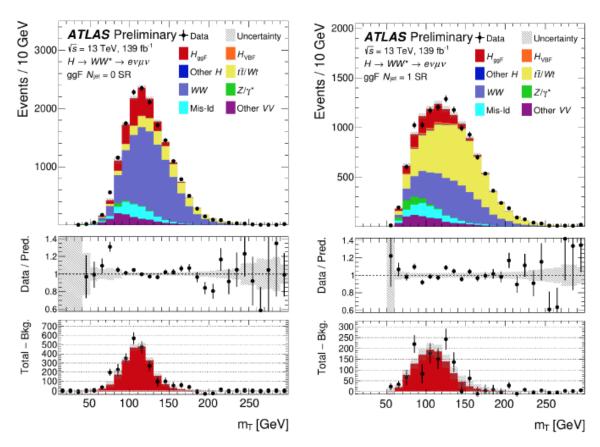
- Tiny branching fraction and larger DY → μμ bkgd
- Bump hunting





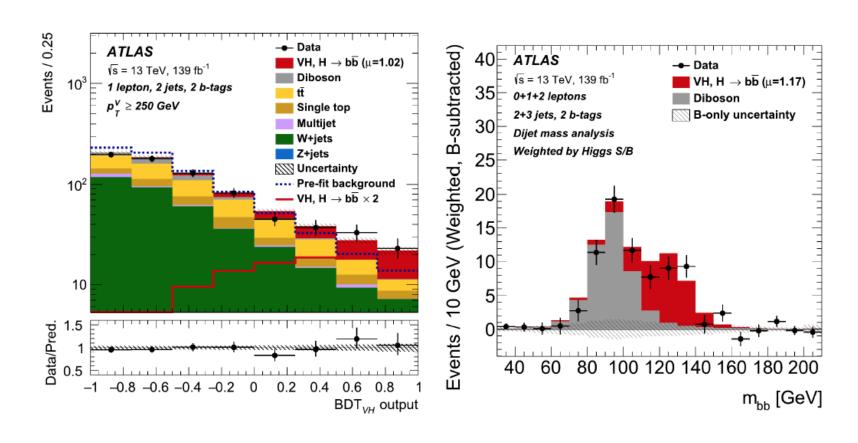
#### $H \rightarrow WW^* \rightarrow 212v$

- Relatively large branching ratio and significant bkgds from WW, ttan d W+jets with mis-ID
- Bkgds with two real leptons from control regions (WW, tt with b-tag, DY with Z mass)



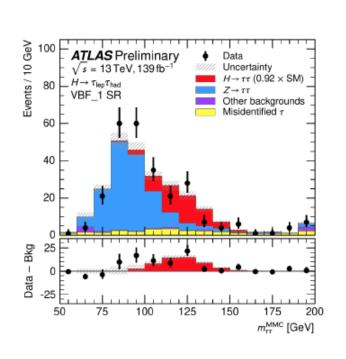
#### H→bb

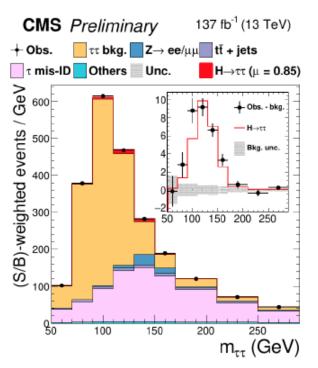
- Large branching ratio, but huge QCD bkgds
- > Strategically, use V+H $\rightarrow$  II, Iv, vv + bb with large W/Z Pt



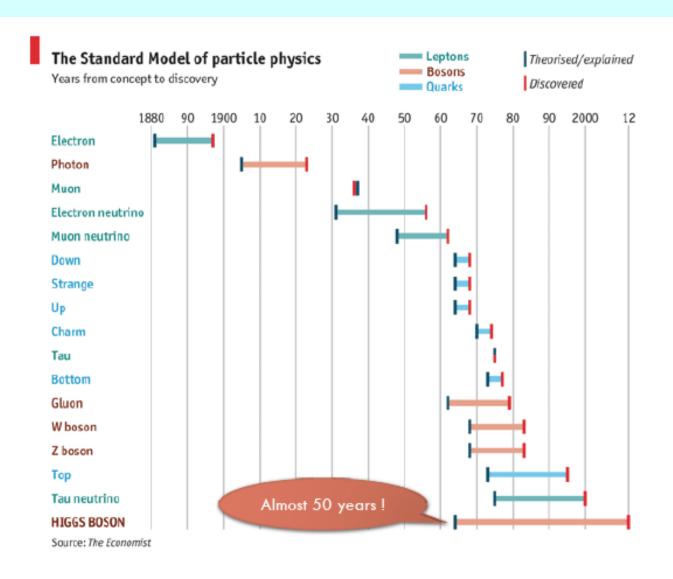
### $H \rightarrow \tau \tau$

- > Select events in eμ, eτ(h)  $\mu\tau$ (h)  $\tau$ (h) $\tau$ (h) final states.
- $\succ$   $\tau\tau$  mass reconstruction using various techniques (kinematic fit, and constraints on decay kinematics etc)
- Categorized with lepton, VBF tagged, boosted, jets





## Discovery to Higgs



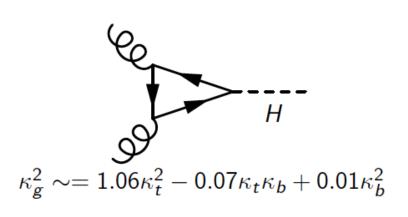
### **Higgs Couplings**

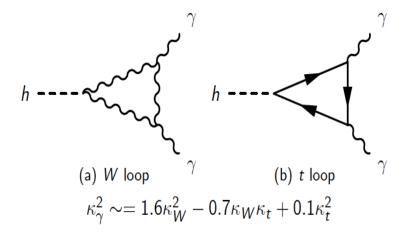
Parameterizing compatibility with the SM (or small deviations)

$$\mu \equiv (\sigma \times BR)_{\text{observed}}/(\sigma \times BR)_{\text{expected}}$$

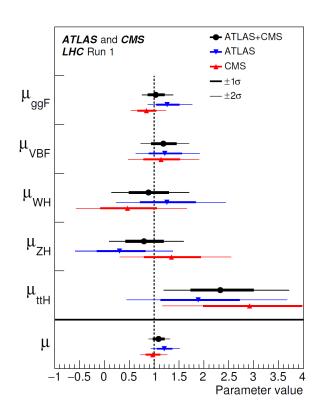
 $\kappa$  parameterize the ratio of the **coupling** of the Higgs to a given particle as a ratio to the SM prediction

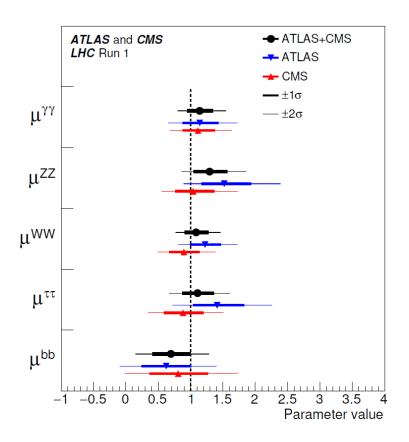
Loop-induced couplings



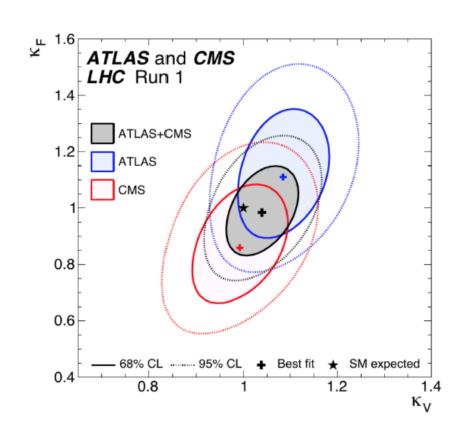


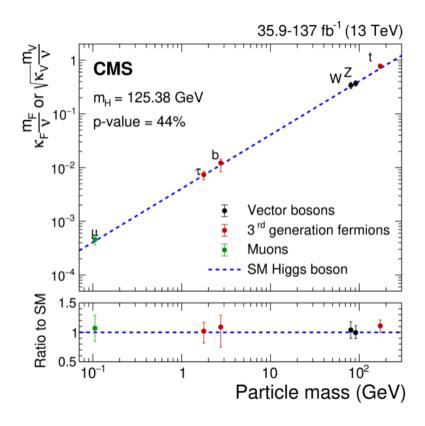
## **Higgs Couplings**





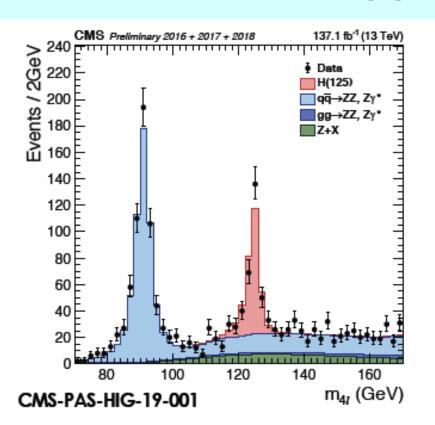
### **Higgs Couplings**

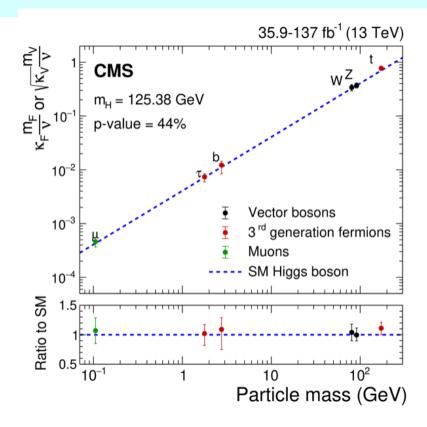




Consistent with the SM predictions

### **Higgs Physics**





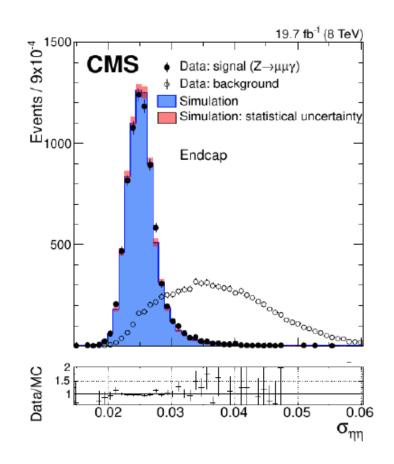
- Higgs mass: 125.38 GeV with 0.1% precision
- Couplings to the SM particles: consistent with the SM predictions
- All consistent with the SM Higgs world

## Backup Slides

#### Photon ID

#### Main sources of Misidentified Prompt Photons:

- $\pi^0 \to \gamma \gamma$  (at high energies, the decay is collimated and tends to merge into a single shower)
- Electrons where primary track is not reconstructed, or misidentified as belonging to a conversion



Transverse shower width (parallel to B-field)

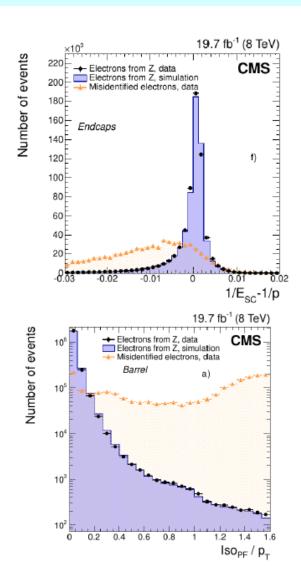
#### Electron ID

#### Main sources of Misidentified Prompt Electrons:

- Heavy flavour decays

   (e.g. B and D hadrons)
   producing displaced
   electrons
- Photon conversions

   (attempt to reconstruct or identify them, but difficult to do efficiently)
- Early showering of charged hadrons in EM calorimeter (e.g. via inelastic charge exchange  $\pi^+ p \to \pi^0 n$ )

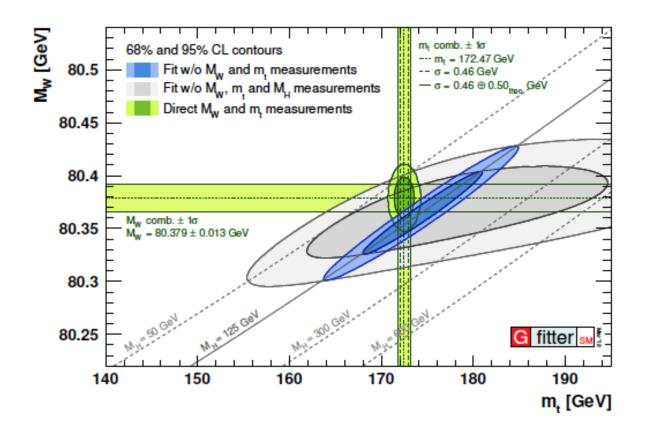


#### Muon ID

#### Main sources of Misidentified Prompt Muons:

- Heavy flavour decays
   (e.g. B and D hadrons)
   producing displaced
   muons
- **Decay in flight** of charged hadrons (e.g.  $\pi^+/K^+ \to \mu^+ \nu$ ), can be supressed with track quality, "kink-finding"
- "Punch through" of charged hadrons (negligible with enough hadronic interaction lengths upstream)

#### **EWK Fit**



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