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Neutrino mass and number constraints from cosmology

Julien Lesgourgues

Institut für Theoretische Teilchenphysik und Kosmologie (TTK), RWTH Aachen University

Setting the stage

- Neutrino expected to be in thermal equilibrium until $T \sim 1$ MeV, number density = 68% of CMB photons for $T < 0.5$ MeV: constitute the **Cosmic Neutrino background (C ν B)**
- **Indirect proof of C ν B** from BBN+primordial abundances, CMB anisotropies, and large scale structure of the universe

- $$N_{\text{eff}} = \frac{\text{(energy density of neutrinos + possible other light/massless relics)}}{\text{(energy density of one neutrino family in instantaneous decoupling limit)}}$$

- $N_{\text{eff}} \simeq 3$ in absence of extra relics (light sterile ν s, axions, dark radiation)

The Cosmic Neutrino Background (C ν B)

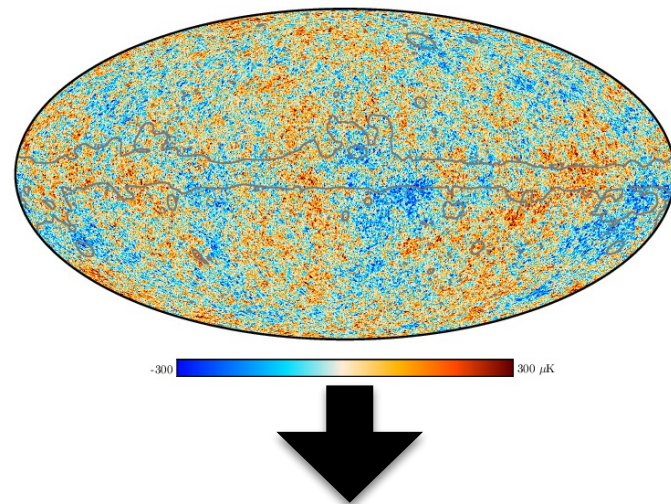
- Precise study of neutrino decoupling (flavour effects, QED corrections) predict $N_{\text{eff}} = 3.044$ (Froustey et al. 2020, Bennett et al. 2020)
- Today, $n_{\nu}^0 = 339.5\text{cm}^{-3}$, $T_{\nu}^0 = 1.7 \times 10^{-4}\text{eV} = 1.9\text{ K}$
- Direct detection very difficult due to low momentum (high energy resolution, background events...)
- Future attempts with PTOLEMY (Tritium β -decay stimulated by C ν B neutrino capture) \Rightarrow *talk by M. Messina (Wednesday)*

The Cosmic Neutrino Background (C ν B)

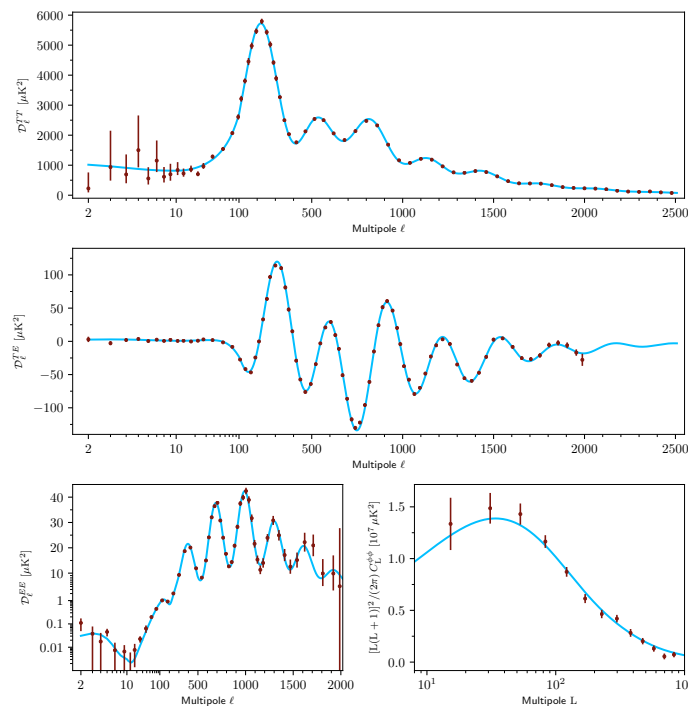
- $T_\nu < |\Delta m^2|_{\text{sol,atm}}^{1/2}$: at least 2 mass eigenstates non-relativistic today
- Each eigenstate :
 - radiation till non-relativistic transition at $z_{\text{NR}} \sim m_i/[0.53 \text{ meV}] - 1$,
 - then, **fraction of Dark Matter**
- Today $\Omega_\nu = (\sum_i m_i)/[93.12 h^2 \text{ eV}] \geq 0.5\%$ of matter components
(Mangano et al. 2005, updated by Froustey & Pitrou);
- cosmology probes **this combination**, i.e. $M_\nu = \sum_i m_i$, not enough sensitivity to individual m_i 's
(JL, Pastor, Perotto 2004; ...; Archidiacono, JL, Hannestad 2020)

Cosmological observables

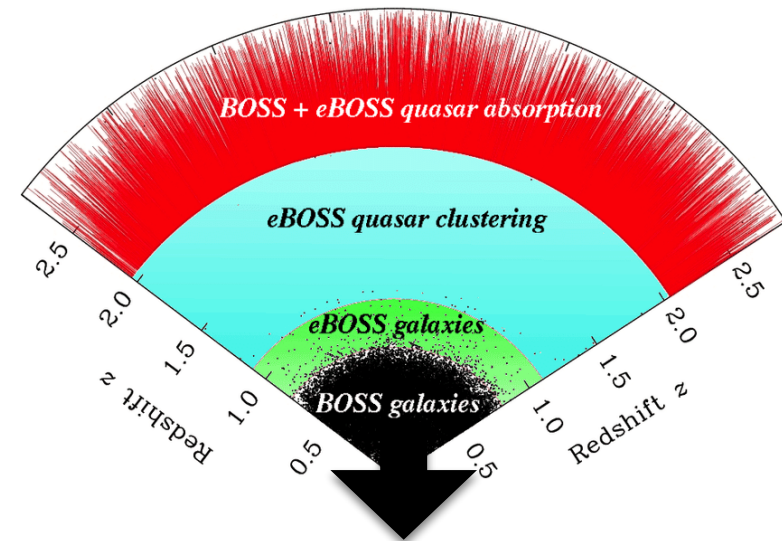
CMB temperature/polarisation maps



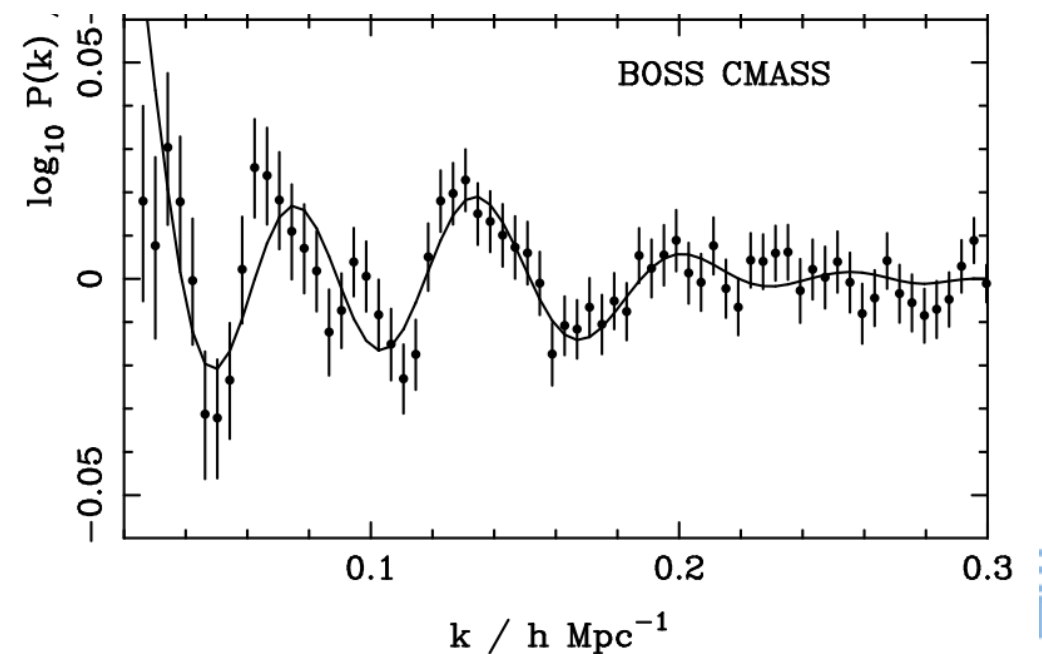
CMB temp./polar. spectrum



Galaxy distribution and lensed shapes

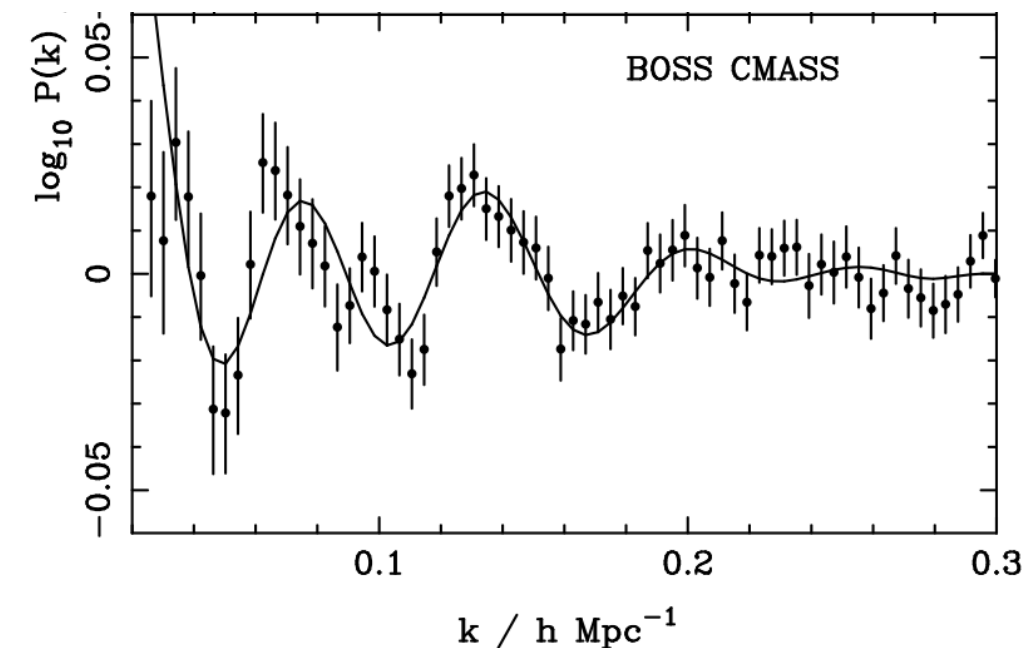
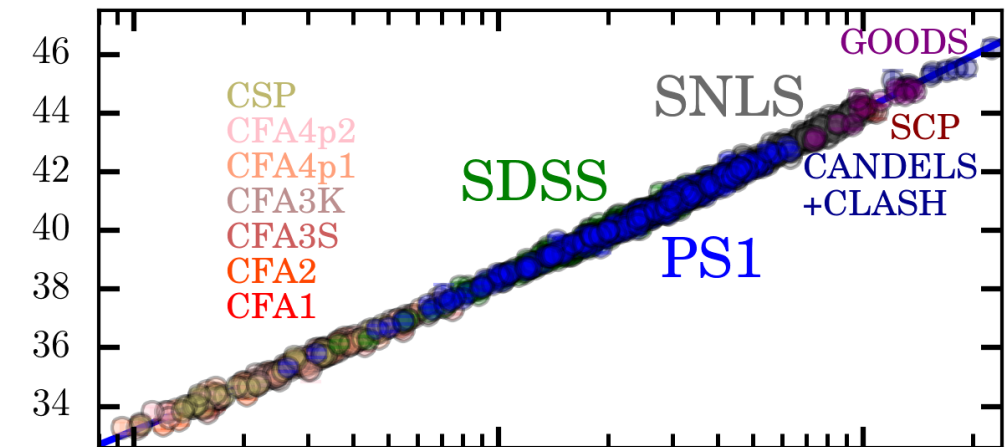


LSS (matter) power spectrum



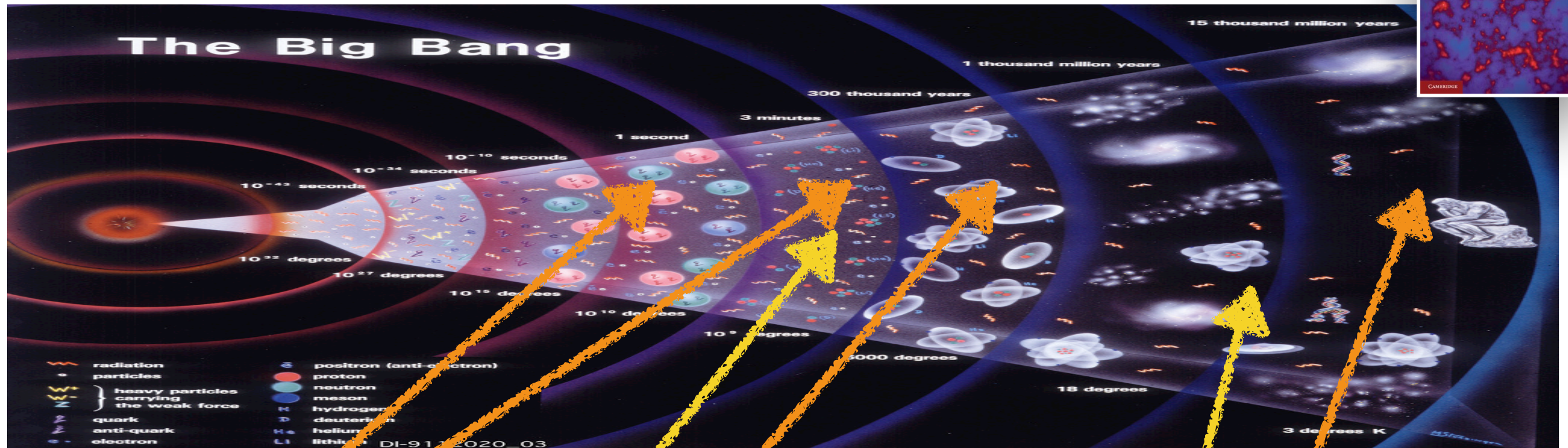
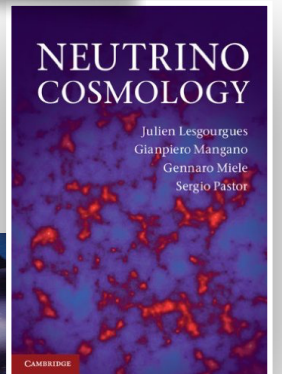
Cosmological observables

- Probes of **background expansion**:
 - from distance ladder (luminosity of cepheids, supernovae)
 - from robust geometrical information contained in LSS spectrum
(BAO = Baryon Acoustic Oscillations, RSD = Redshift Space Distorsions)
- Primordial Deuterium / Helium and theory of **BBN**



Neutrino effects on cosmological observables

JL & Pastor Pys. Rep. 2016; JL, Mangano, Miele, Pastor “Neutrino Cosmology” CUP;
Drewes et al. 2016; Gerbino & Lattanzi 2017 ; RPP of PDG: JL & Verde “Neutrinos in Cosmology”;



relativistic
neutrino contribution
to early expansion

metric fluctuations during non-
relativistic **neutrino** transition
(early ISW)

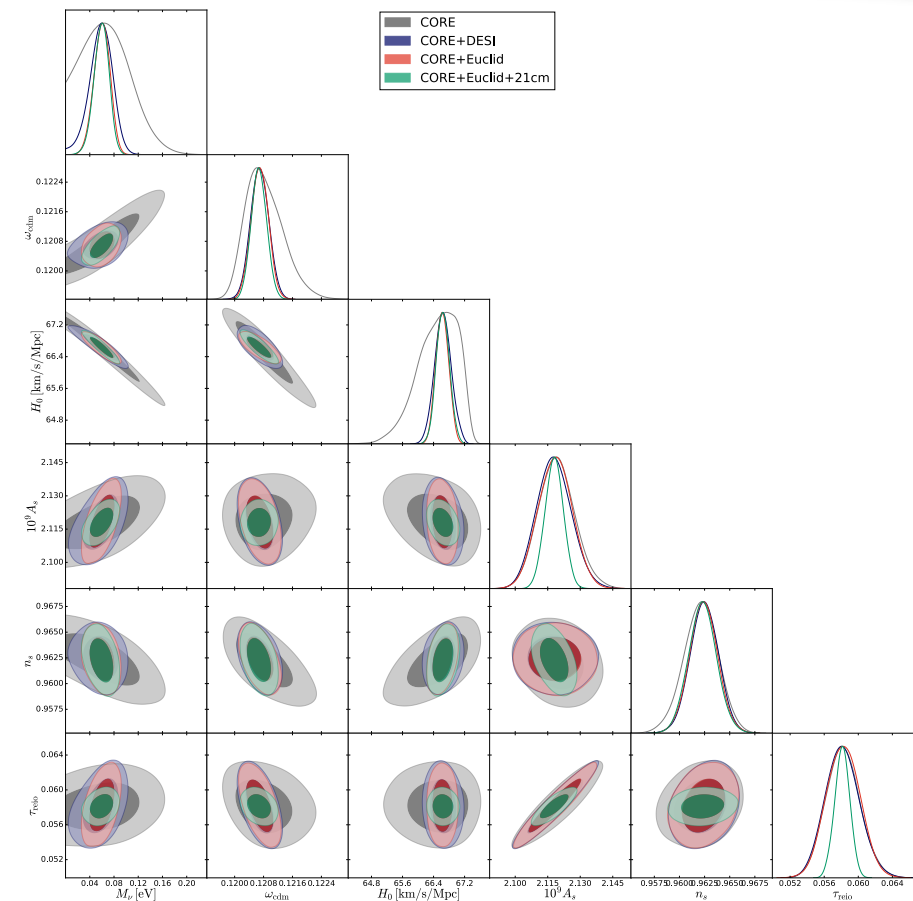
non-relativistic **neutrino**
contribution to late expansion
rate (acoustic angular scale)

neutrino free-streaming slows
down CMB photon clustering

neutrino free streaming slows down late
ordinary/dark matter clustering

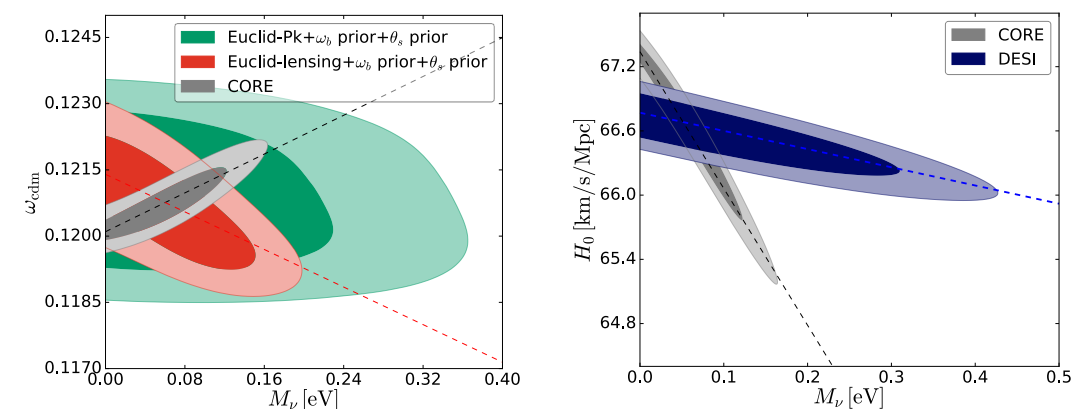
Cosmological bounds are model dependent!

Global fit of cosmological model to data: bounds are **model-dependent** (can be relaxed when adding new ingredients)



e.g. Archidiacono et al. 1610.09852

Model-dependence **decreases** quickly over the years (more types of independent observations, smaller error bars)



Model dependance

What do we do with cosmological tensions appearing in Λ CDM framework:

- on current Hubble rate H_0 ?
(5σ , dominated by one collaboration, SH0ES [Riess et al. 2112.04510](#))
- on matter spectrum amplitude S_8 ?
($2 - 3\sigma$, found by many collaborations: KiDS, DES, CHFTLens, etc.) ?

... and to a lesser extent:

- (n_s, Ω_m) tension between Lyman- α forest spectrum and CMB
- Small-scale CMB polarisation anisotropies from ACT versus SPT-3G
- internal consistency of Planck data (" A_L anomaly" -> *not a concern for me*
(fluctuating unphysical parameter, look-elsewhere effect, decreased to 1.5σ
in recent re-analysis of [Rosenberg et al. 2022](#))

Model dependance

What do we do with cosmological tensions appearing in Λ CDM framework:

1. Assume they will go away (**systematics**). Fit neutrino parameters (N_{eff}, M_ν) in:
 1. Minimal Λ CDM
 2. Most obvious extensions (light relics, dynamical DE, curvature, T/S...)
 3. Models with more freedom (beyond-Einstein gravity, non-trivial Dark Sector...)
2. Assume they are “real”, investigate **new scenarios accommodating the tension**, explore neutrino bounds within that framework

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\Rightarrow this talk

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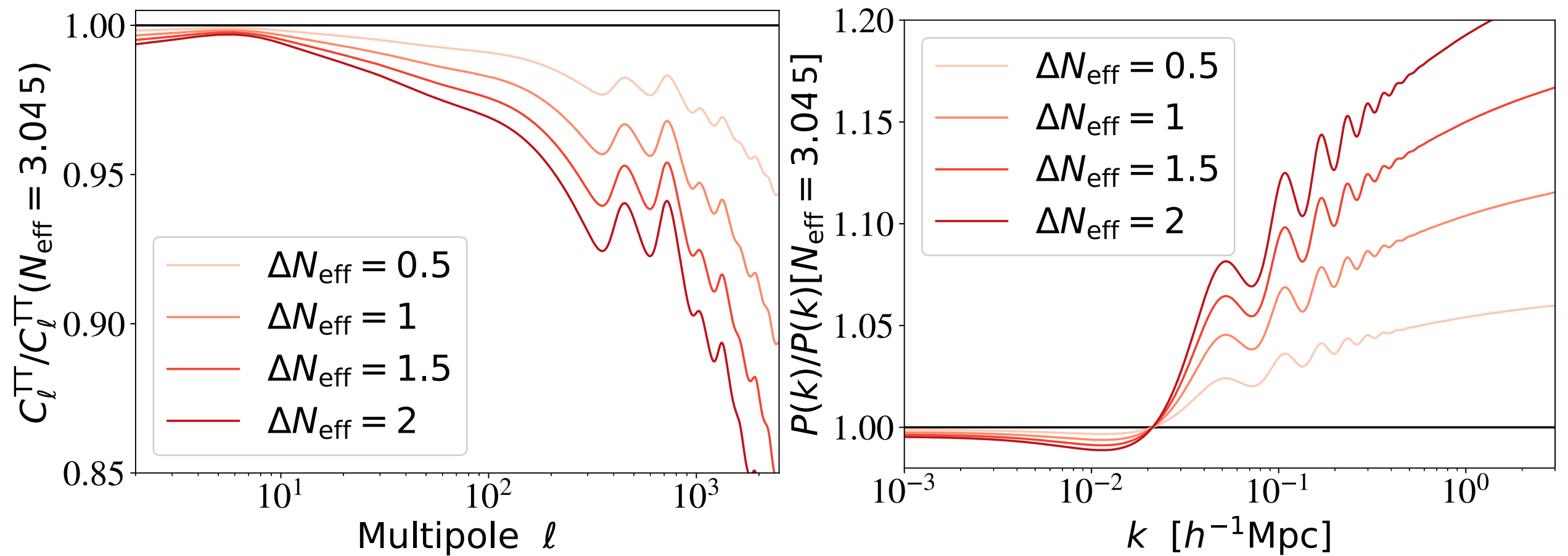
\Rightarrow talk by O. Mena

Impact of N_{eff}

Measuring N_{eff} or $\Delta N_{\text{eff}} = N_{\text{eff}} - 3.044$ with cosmological observables may :

- Confirms presence of $C\nu B$
- Confirm standard thermal history of the universe (reheating, neutrinos decoupling, positron annihilation...)
- Bound non-thermal corrections from e.g. late decays into neutrinos
- Bound existence of additional light relics (light sterile ν s, axions, dark radiation...)
- Together with Helium abundance, bound new physics around time of Nucleosynthesis

Impact of N_{eff}



Fixed $\{\Omega_r, \Omega_m, \Omega_\Lambda\}$

(from RPP, JL & Verde)

Measurement of N_{eff}

(from RPP, JL & Verde)

	Model	95%CL	Ref.
CMB alone			
P18[TT,TE,EE+lowE]	$\Lambda\text{CDM}+N_{\text{eff}}$	$2.92^{+0.36}_{-0.37}$	[22]
CMB + background evolution + LSS			
P18[TT,TE,EE+lowE+lensing] + BAO	$\Lambda\text{CDM}+N_{\text{eff}}$	$2.99^{+0.34}_{-0.33}$	[22]
” + BAO + R21	$\Lambda\text{CDM}+N_{\text{eff}}$	3.34 ± 0.14 (68%CL)	[11]
P18[TT,TE,EE+lowE+lensing] + BAO	” +5-params.	2.85 ± 0.23 (68%CL)	[23]

- Compatible with BBN + Helium (+ Deuterium) bounds
(even after LUNA update: see [Pisanti et al. 2021](#), [Pitrou et al. 2021](#))

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- Provides bounds on neutrino asymmetry

$$\left| \sum_{\alpha=e,\mu,\tau} \frac{n_{\nu_\alpha}^{\text{dec}} - \bar{n}_{\nu_\alpha}^{\text{dec}}}{n_\gamma^{\text{dec}}} \right| < 0.084 \quad (95\%, \text{ Planck TT, TE, EE + lowP + lensing})$$

(Oldengott & Schwarz 2017)

- BBN / Helium more sensitive through beta decay and oscillations

$$-0.071 < \sum_{\alpha=e,\mu,\tau} \frac{n_{\nu_\alpha}^{\text{ini}} - \bar{n}_{\nu_\alpha}^{\text{ini}}}{n_\gamma^{\text{ini}}} < 0.054 \quad (95\%, \text{ WMAP + Helium}) \quad (\text{Castorina et al. 2012})$$

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- Global fit, in principle model-dependent, in practise not so much for simple extensions of ΛCDM

(De Valentino et al. 2020)

Measurement of N_{eff}

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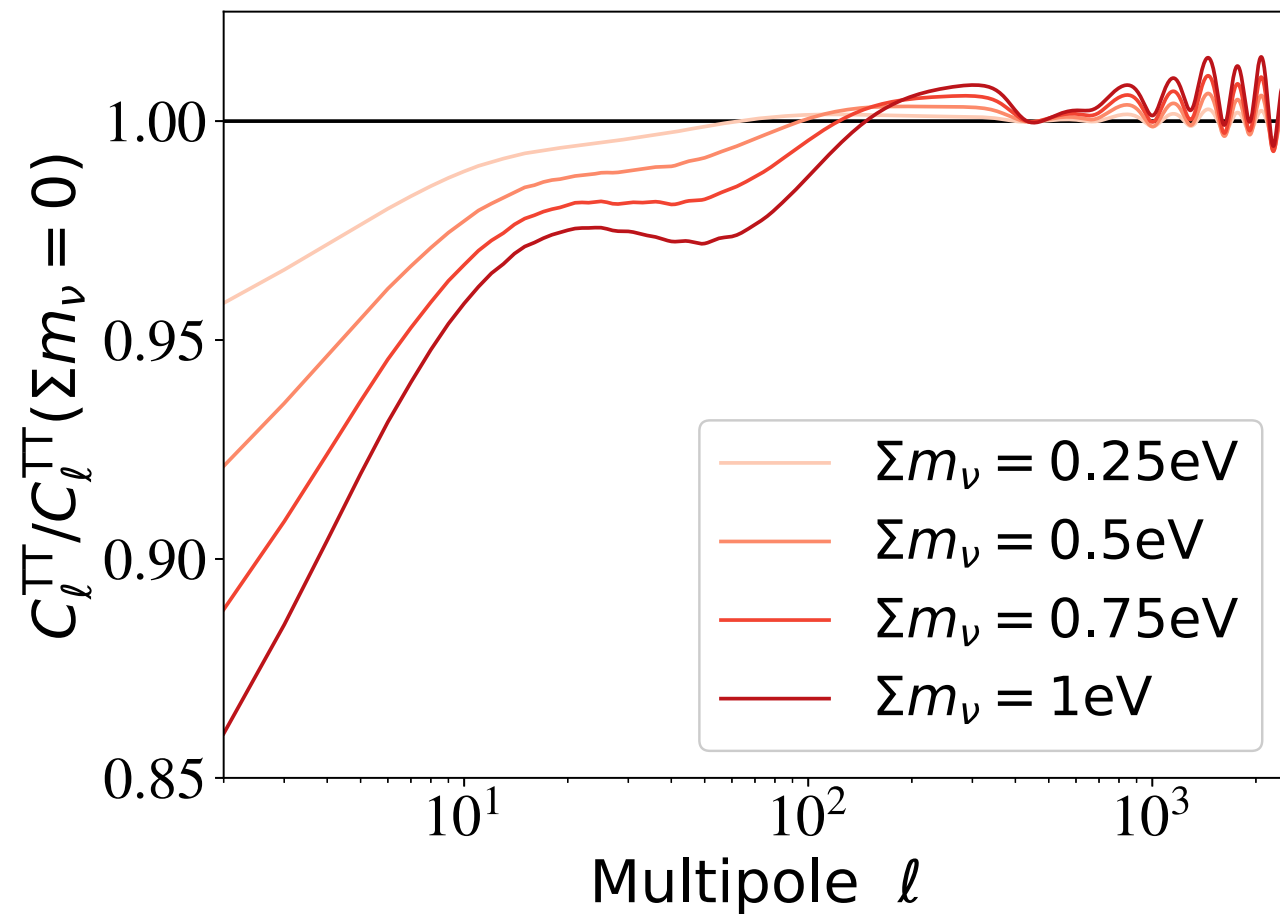
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- Global fit, in principle model-dependent, in practise not so much for simple extensions of ΛCDM
(De Valentino et al. 2020)
- Hubble tension ?... positive $H_0 - N_{\text{eff}}$ correlation. Discussions about $N_{\text{eff}} > 3$ as a solution. Currently disfavoured.

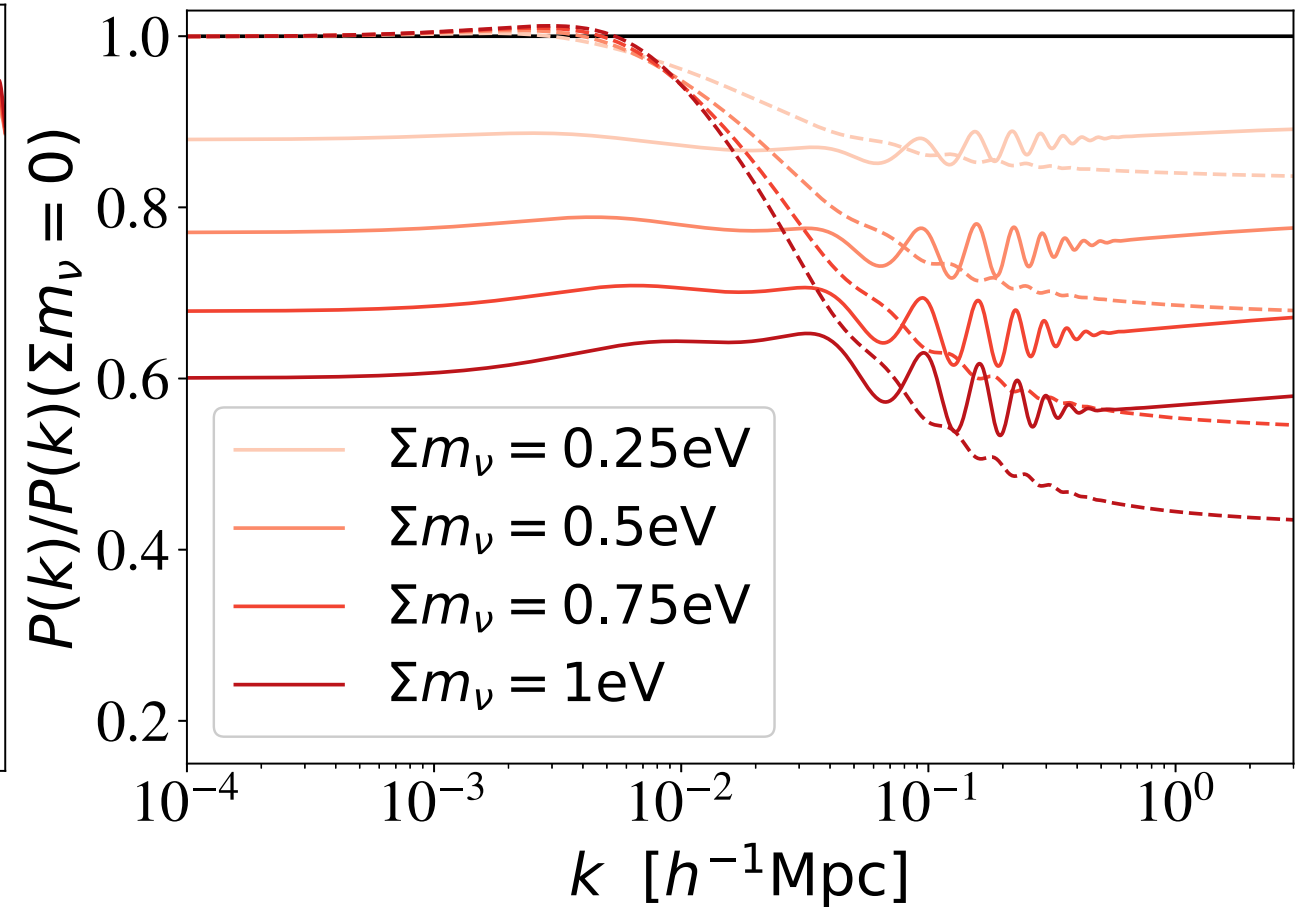
Probes of $C_{\nu B}$

- measured N_{eff} compatible with prediction 3.044 (although... H_0 tension)
- details of acoustic oscillations in CMB and LSS spectra probe neutrino drag effect : indicate free streaming ultra-relativistic species. $C_{\nu B}$ detected at level of its background and perturbations
(Bashinsky & Seljak 2004 , Audren et al. 2015, Baumann et al. 2019, ...)
- Limits on non-standard neutrino self-interactions: $\log_{10}(G_{\text{eff}} \text{MeV}^2) < -0.8$
(Park et al. 2019)

Impact of Σm_ν



Fixed $\{\omega_b, \omega_c, \tau, \theta_s\}$



(from RPP, JL & Verde)

Bounds on Σm_ν

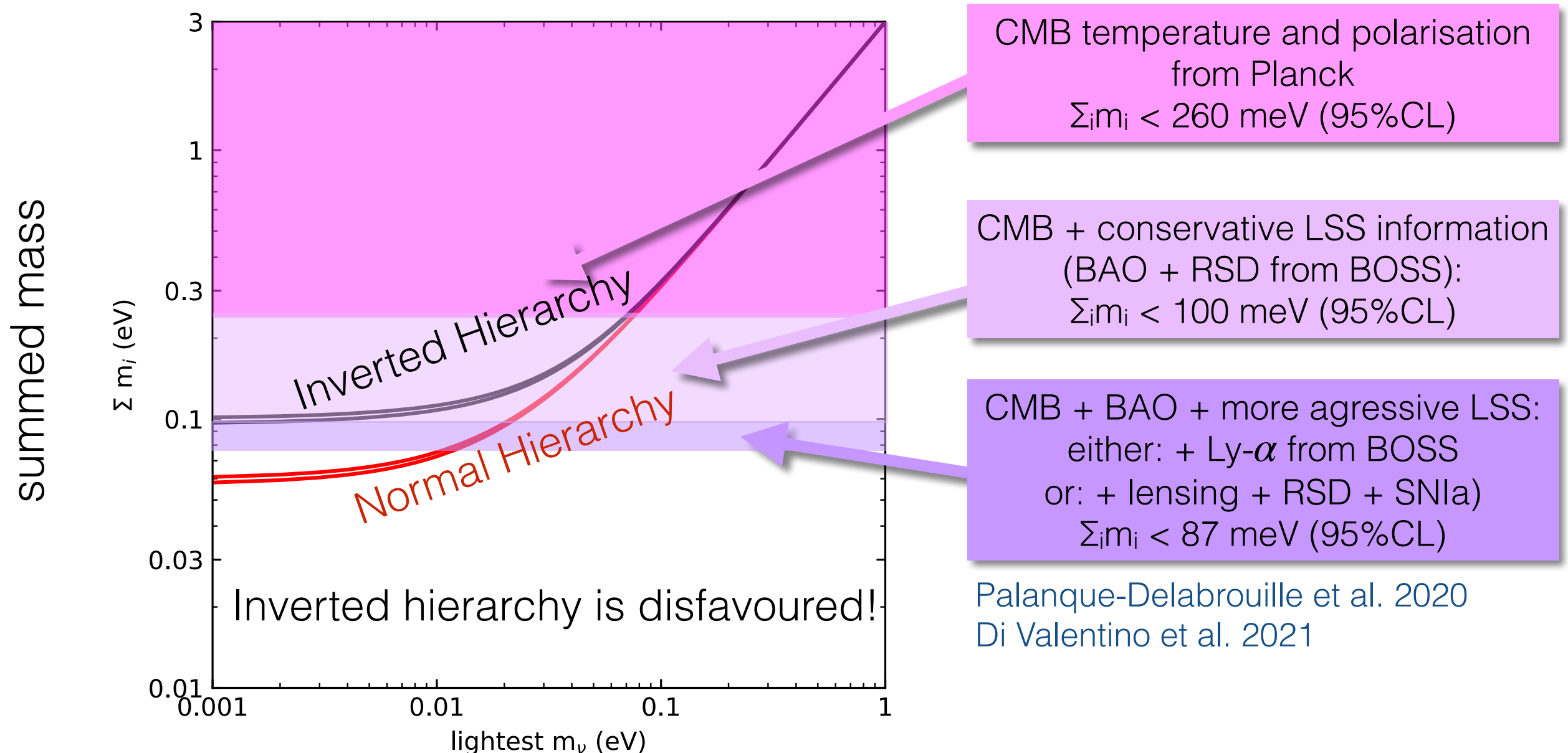
(from RPP, JL & Verde)

	Model	95% CL (eV)	Ref.
CMB alone			
P18[TT+lowE]	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.54	[22]
P18[TT,TE,EE+lowE]	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.26	[22]
CMB + probes of background evolution			
P18[TT+lowE] + BAO	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.13	[43]
P18[TT,TE,EE+lowE]+BAO	$\Lambda\text{CDM}+\Sigma m_\nu+5 \text{ params.}$	< 0.515	[23]
CMB + LSS			
P18[TT+lowE+lensing]	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.44	[22]
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CMB + probes of background evolution + LSS			
P18[TT,TE,EE+lowE] + BAO + RSD	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.10	[43]
P18[TT+lowE+lensing] + BAO + Lyman- α	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.087	[44]
P18[TT,TE,EE+lowE] + BAO + RSD + Pantheon + DES	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.13	[45]
P18[TT,TE,EE+lowE+lensing] + BAO + RSD + Pantheon.	$\Lambda\text{CDM}+\Sigma m_\nu$	< 0.087	[dVGM]

2021: new eBOSS
and DES data

Bounds on Σm_ν

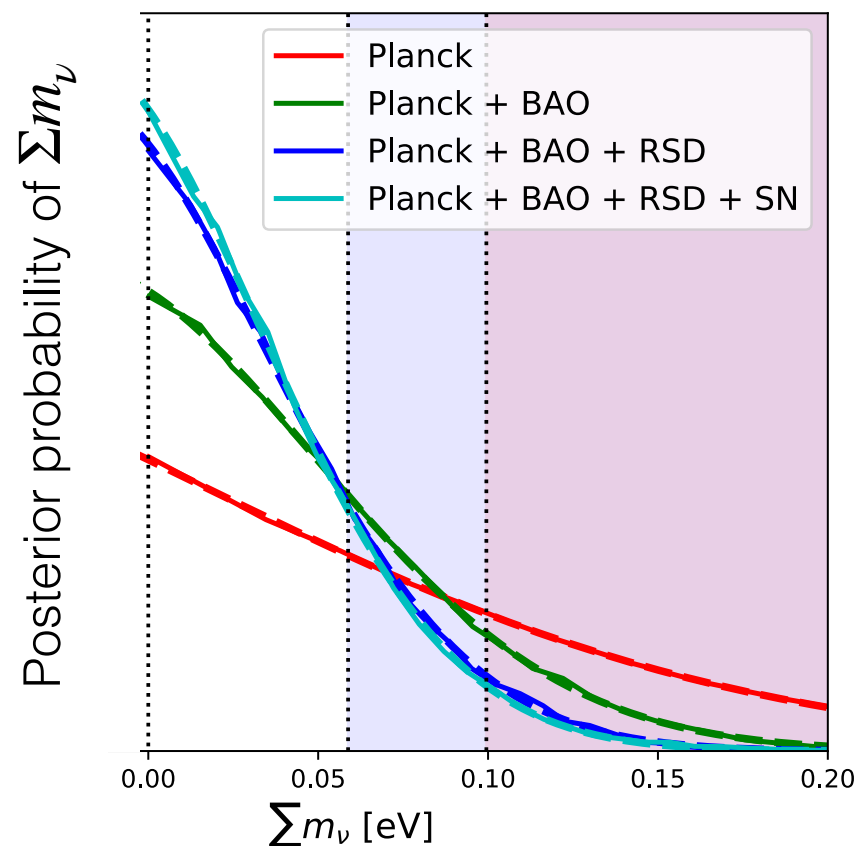
95%CL upper bounds on $\Sigma_i m_i$ for 7 parameters



Model dependance

Shall we be concerned about posterior peaking in zero?:

- $\sigma(\Sigma m_\nu)$ reducing to ~ 0.05 eV, and still no hint of a posterior peaking anywhere above 0 eV



From Alam et al. 2020 (eBOSS)

- May be the consequence of only the randomness of instrumental errors + underlying theory (cosmic variance), with still acceptable level of probability
- Or, like tensions, sign of systematics or using wrong model...

Bounds on Σm_ν

(from RPP, JL & Verde)

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- Crucial role of CMB (WMAP+SPT: similar bounds, WMAP+ACT: twice weaker bounds) (Di Valentino & Melchiorri 2021)
- Robustness against simple LCDM extensions (De Valentino et al. 2020)
- Negative $M_\nu - H_0$ correlation: Inclusion of direct Hubble measurement from SH0ES makes bounds even stronger but subject to caution

Is inverted hierarchy excluded ?

Calculation of Bayesian evidence using laboratory (oscillations, KATRIN)+ cosmological data:

- **Decisive evidence for NH** according to [Jimenez et al. 2022](#) - driven by cosmology
- Only **moderate evidence for NH** according to [Gariazzo et al. 2022](#) - driven by oscillation data

Main issue = **Bayesian prior dependence** of the results (discussed by both groups). Second group ensures that prior alone gives 1:1 odds for NH/IH.

My take: too many self-consistency issues in cosmological data / standard model for including current bounds in such detailed statistical analyses.

If S_8 tension is “real”, but not H_0 tension

- Naive explanation: $M_\nu \sim 0.6 \text{ eV}$... ruled out by CMB in all simple ΛCDM extensions
- List of alternative mechanisms **reducing growth of matter fluctuations** on small scales and compatible with CMB, BAO, Weak Lensing, Lyman- α ...
- Modified gravity (e.g. $f(R)$), cold+warm DM, (self-)interacting DM, DM with 2-body decay... (Boyarsky et al. 0812.0010; Buen-Abad et al. 1708.09406; Becker et al. 2010.04074; Heimersheim et al. 2008.08486; Abellan et al. 2008.09615; ...)

Neutrino mass bounds depend on each case, but usually **CMB+BAO sets barrier around 0.13 eV**, unlikely to be challenged by these models which have minimal impact on CMB...

If H_0 tension is “real”

- Naive explanation in terms of $N_{\text{eff}} \sim 5$ ruled out by both CMB and BBN
- No very simple alternative compatible with CMB, BAO, Pantheon (= high- z supernovae)... Price to pay is high (Schöneberg et al. 2021):
 1. Shifted recombination (variation of particle masses (Hart & Chluba 2020) ? Inhomogeneous recombination (Jedamzik & Pogosian 2020) ?);
 2. Non-minimal Dark Radiation: self-interactions, density increasing after BBN (possible precise scenarios: Majoron (Escudero & Witte 2021), Wess-Zumino (Aloni et al. 2011), ...);
 3. Early Dark Energy; Modified gravity ...
- Neutrino mass bounds depend on each case, could be significantly released (e.g. like for self-interacting neutrinos of Cyr-Racine et al.), more work needed...
- Same if both tensions are “real”...

Prospects on mass measurement

- Future LSS surveys: DESI, Euclid, LSST, SPHEREx, SKA...
- Future CMB observations: Simons Observatory, CMB-Stage4, LiteBird
- Planck+Euclid: at least $\sim 2\sigma$
- Should grow to $3\text{--}4\sigma$ with new CMB data (SO, CMB-S4) and better LSS data
- Could reach 5σ after better measurements of reionization and 21cm fluctuations (radioastronomy: SKA, ...)
- Null detection would be revolutionary (NSI, neutrino decay...)
- Possible shift of paradigm could reshuffle conclusions...