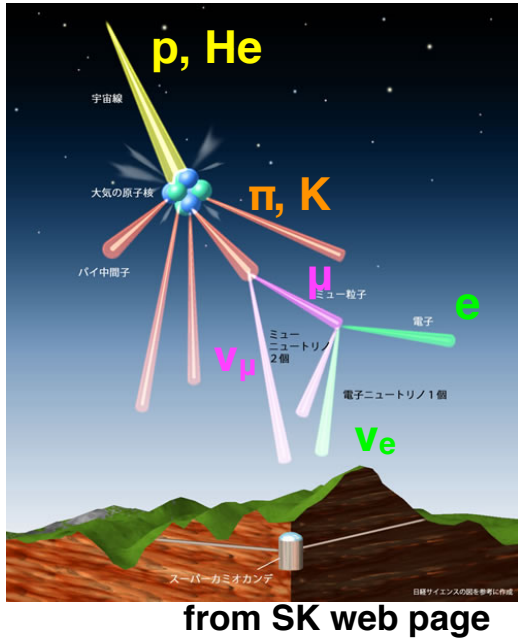


low energy atm. neutrino flux

Sato Kazufumi (ICRR, U of Tokyo)
2 June 2022 @ Neutrino2022

atmospheric neutrino (atm. ν)



primary cosmic-ray particles (p, He, ...) hit to air nucleus

→ develop hadronic shower

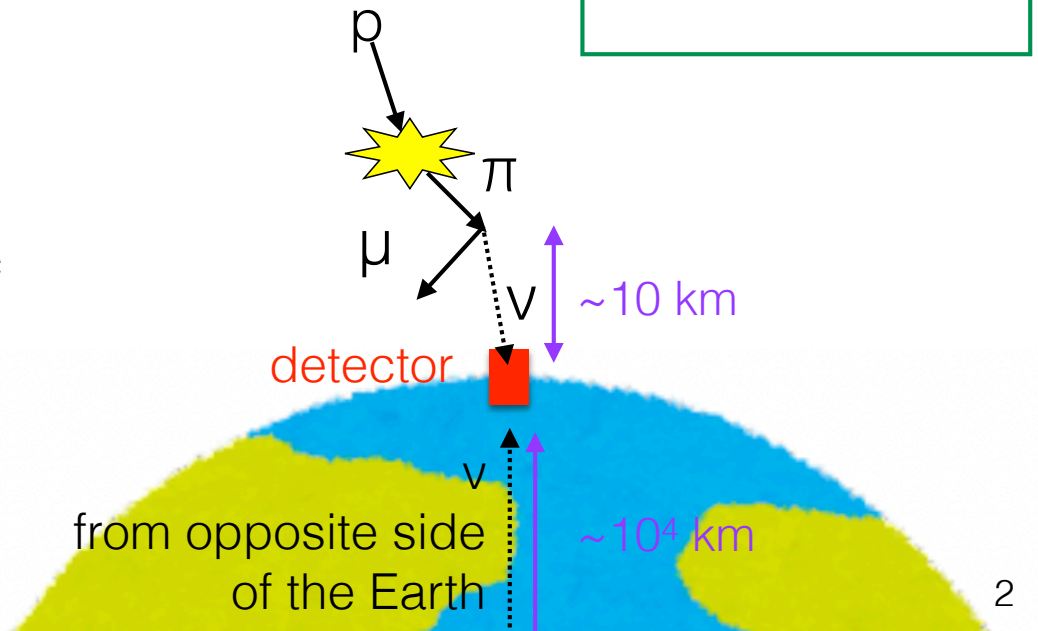
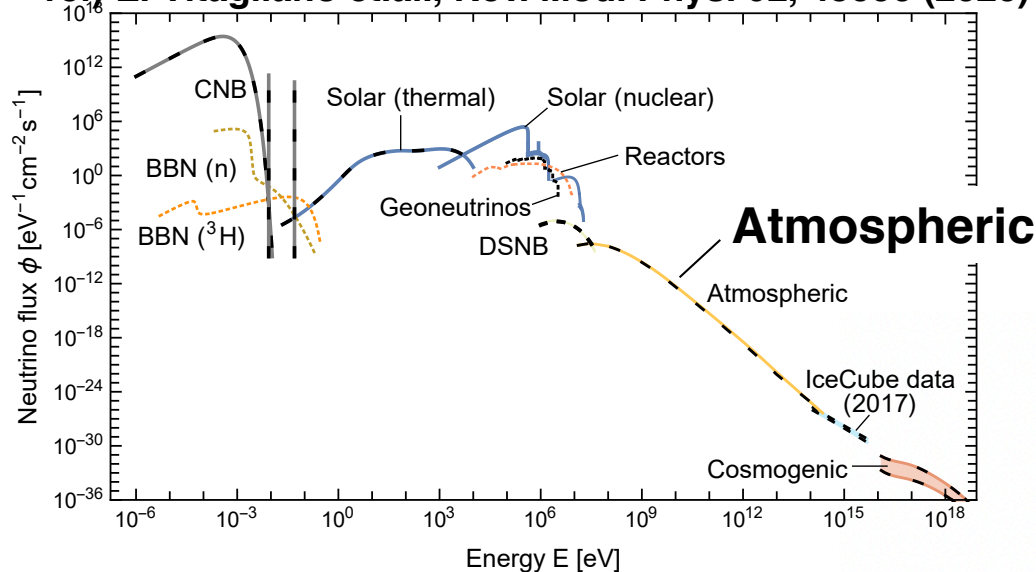
→ decay of $\pi, \mu, K \rightarrow \underline{\nu}$
atm. ν 's

- E_ν : O(10) MeV — O(10) TeV
- flight length L : 10 — O(1e4) km

**In this talk,
focus on
 $E_\nu < 100$ GeV**

natural neutrino source

ref) E. Vitagliano et.al., Rev. Mod. Phys. 92, 45006 (2020)



physics of low energy neutrinos

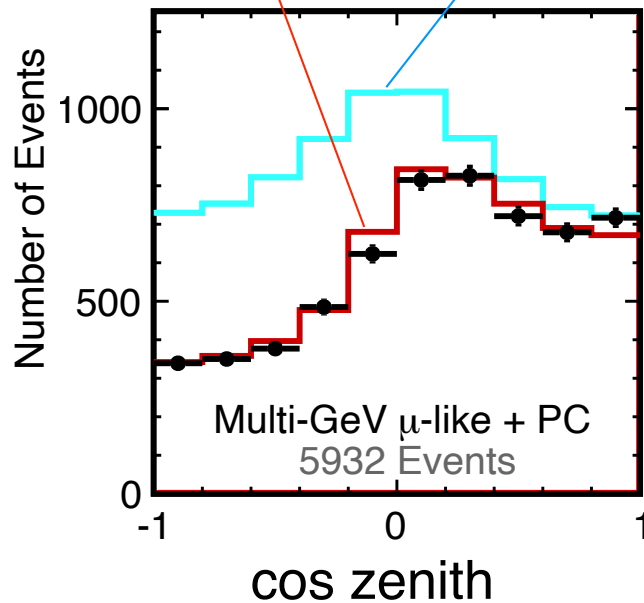
As a physics target

- ★ discovery of **ν oscillation** in 1998
 - ν_μ deficit in large L/E region
- ★ sensitivity for **δ_{CP}** and **Mass ordering** in future big ν detectors

ν oscillation observed in SK

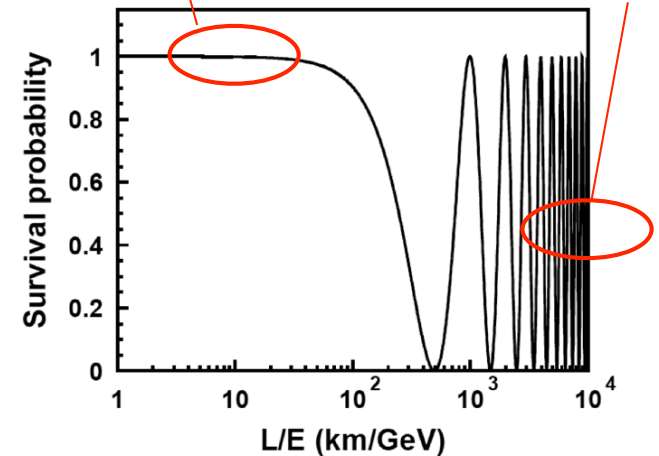
(from IPMU News vol. 15)

best fit w/
oscillation non-oscillated
prediction



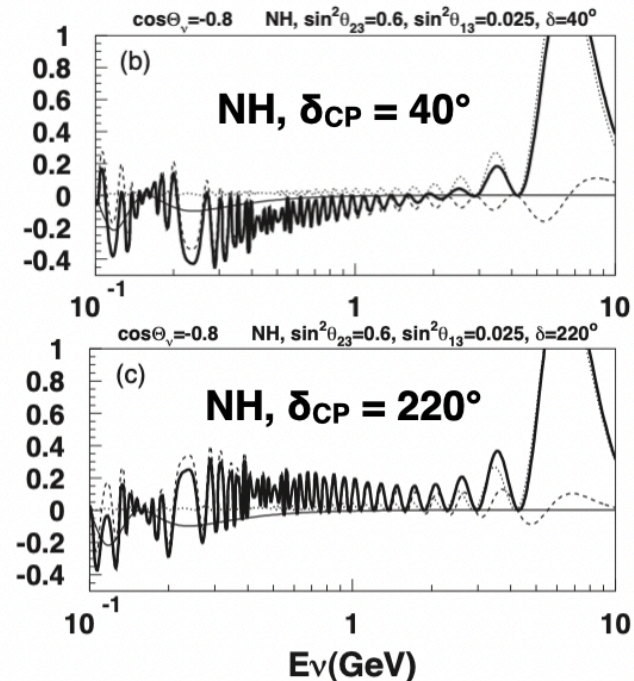
$E \sim 1 \text{ GeV}, \cos\theta = 1$

$E \sim 1 \text{ GeV}, \cos\theta = -1$



from HK design report

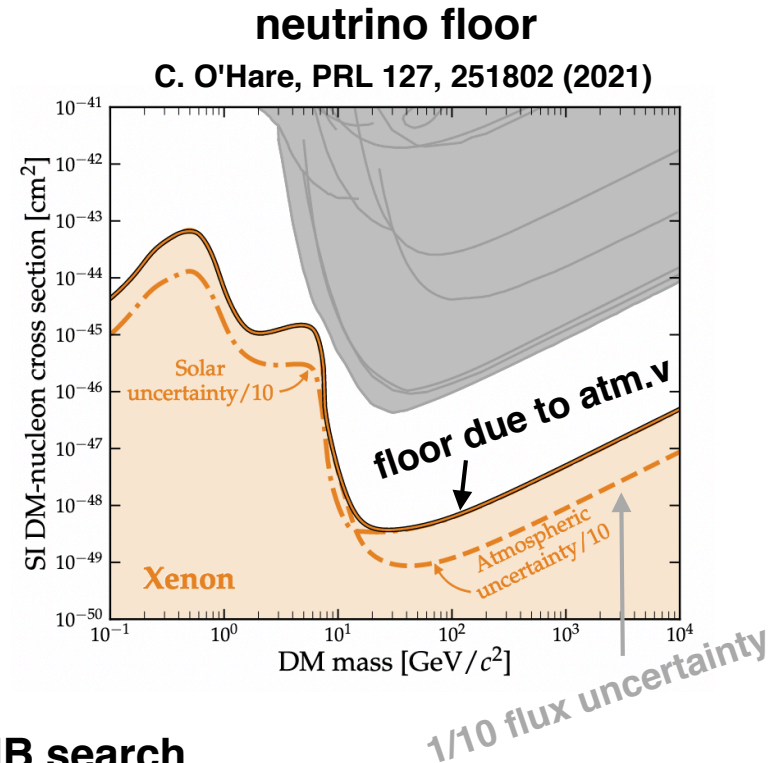
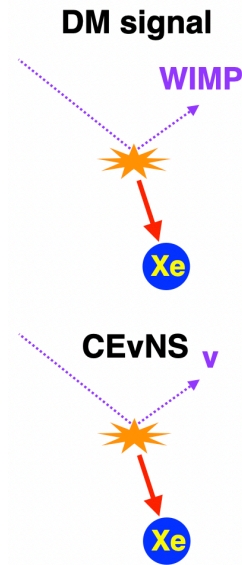
ν flux ratio
(oscillation / non-oscillation)



physics of low energy neutrinos

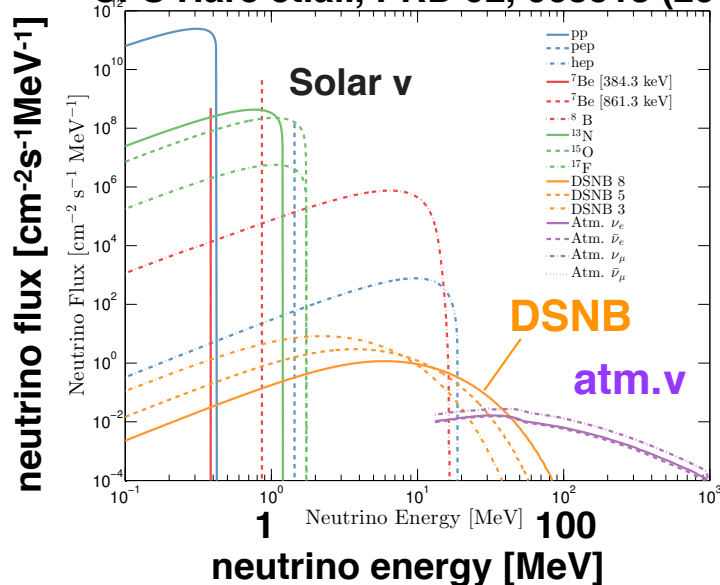
As an important background

- Direct Dark Matter search
 - 40--100 MeV atm. ν can be ultimate BG = neutrino floor
- Diffuse Supernova BG (DSNB)
 - predicted in 20--40 MeV = excess on atm. ν BG
- Proton decay, Indirect DM search, etc...



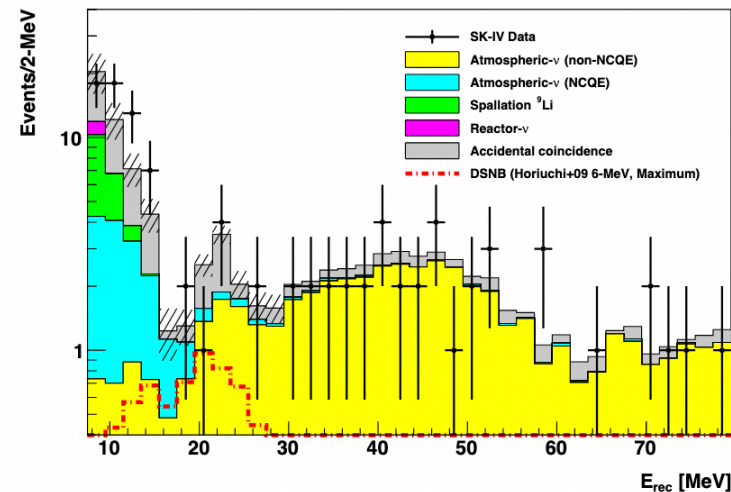
neutrino sources in 0.1--1000 MeV

C. O'Hare et al., PRD 92, 063518 (2015)



DSNB search

SK group, Phys. Rev. D 104, 122002 (2021)



flux prediction

flux of $\nu_{\mu,e}$

$$\phi_{\nu_i} = \sum_A \phi_A \otimes R \otimes Y_{A \rightarrow \nu_i}$$

A : primary nuclei
p : 75%
He : 15%
others : ~10%

Yields of ν through hadronic interactions

Transportation in geomagnetic field and atmosphere

flux of primary cosmic-ray

☞ use numerical calculation

- Monte Carlo technique
 - Honda
 - Bartol
- solve cascade equation
 - MCEq

3D simulation

→ **low E**

1D calculation

→ **high E**

flux prediction

flux of $\nu_{\mu,e}$

$$\phi_{\nu_i} = \sum_A \phi_A \otimes R \otimes Y_{A \rightarrow \nu_i}$$

A : primary nuclei
p : 75%
He : 15%
others : ~10%

flux of primary cosmic-ray

Yields of ν through hadronic interactions

Transportation in **geomagnetic field** and atmosphere

+ **transverse momentum of secondaries**

* **1D-3D difference in low E**

- **for $E_\nu < O(1\text{GeV})$** horizon enhancement
- **for $E_\nu < O(10\text{GeV})$** East-West effect

☞ use numerical calculation

- Monte Carlo technique
 - Honda
 - Bartol
- solve cascade equation
 - MCEq

3D simulation

→ **low E**

1D calculation

→ **high E**

source of uncertainty

flux of $\nu_{\mu,e}$

$$\phi_{\nu_i} = \sum_A \phi_A \otimes R \otimes Y_{A \rightarrow \nu_i}$$

uncertainty of hadron production

Yields of ν through hadronic interactions

Transportation in geomagnetic field and atmosphere

* 1D-3D difference in low E

flux of primary cosmic-ray

uncertainty of primary flux measurements

- dominant uncertainty arises from

- **primary CR flux**
- **hadron production cross-section**

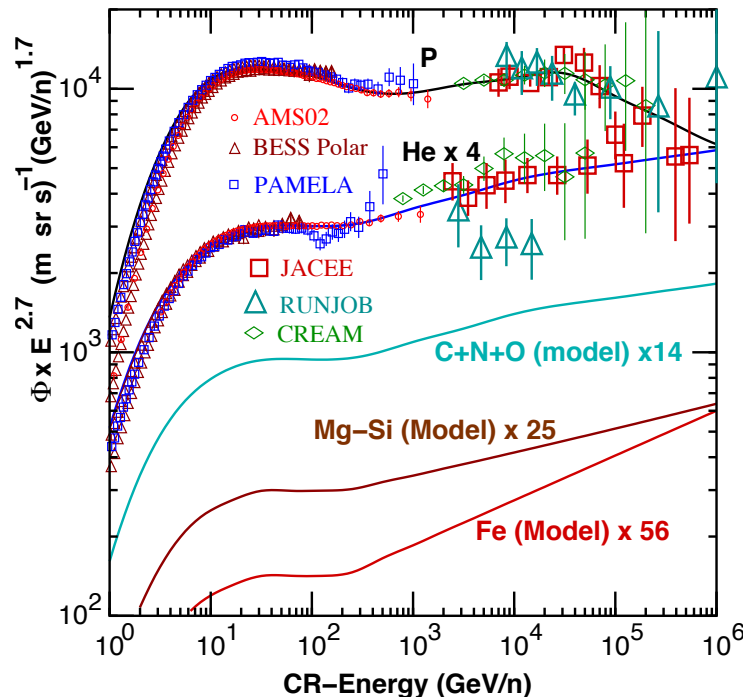
→ Reducing these uncertainties is a key for accurate prediction

primary cosmic-ray flux

- Provided by satellite-based & balloon experiments
→ Improvement in recent data reduces uncertainty

Primary CR flux

M. Honda et.al., PoS ICRC2017, 1022

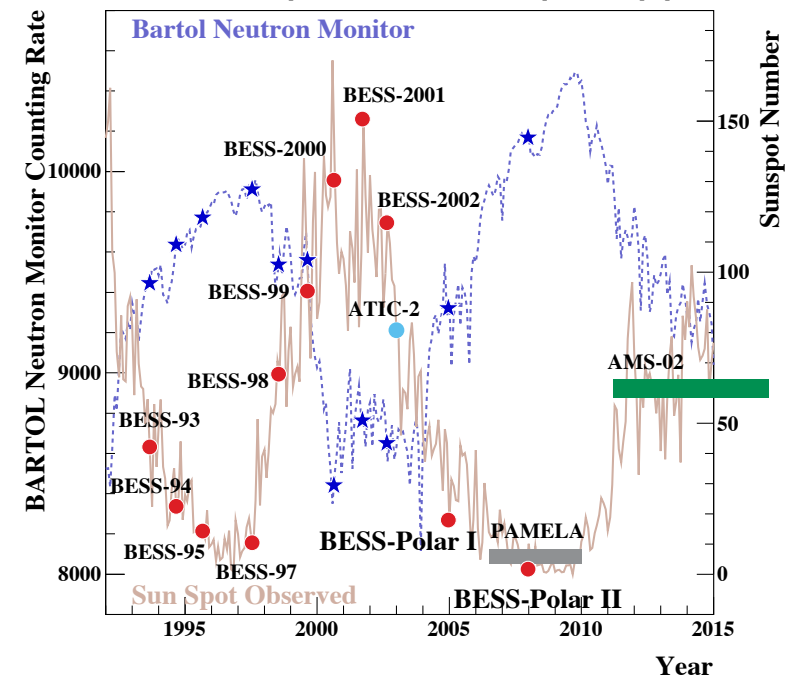


← AMS-02 provides flux up to 1 TeV with < few% accuracy

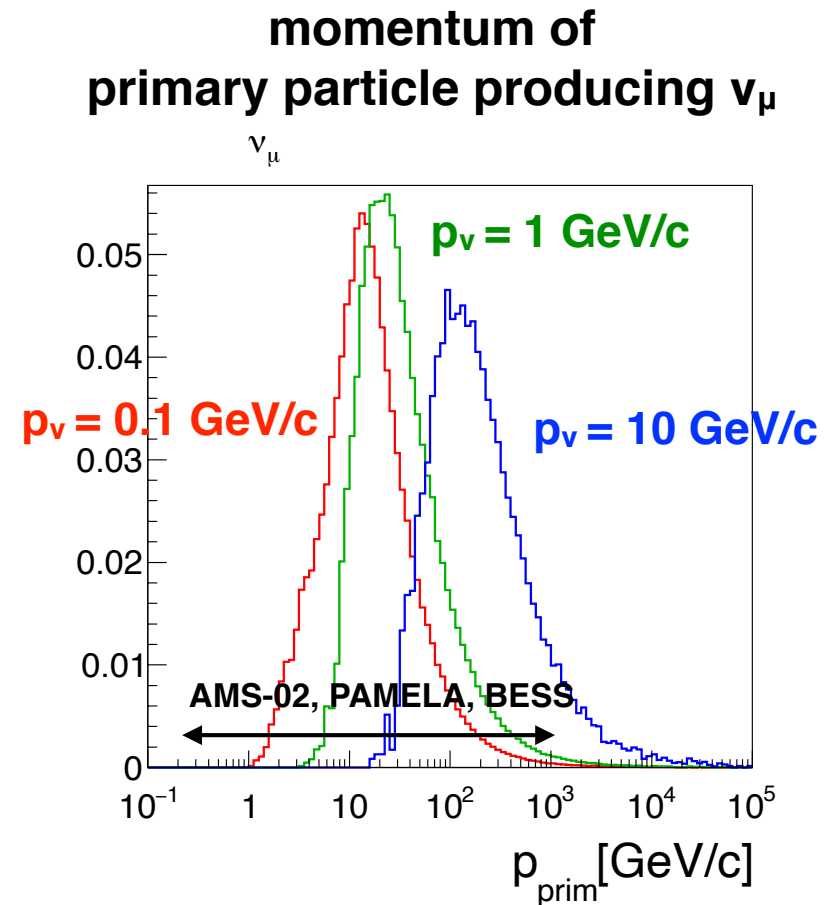
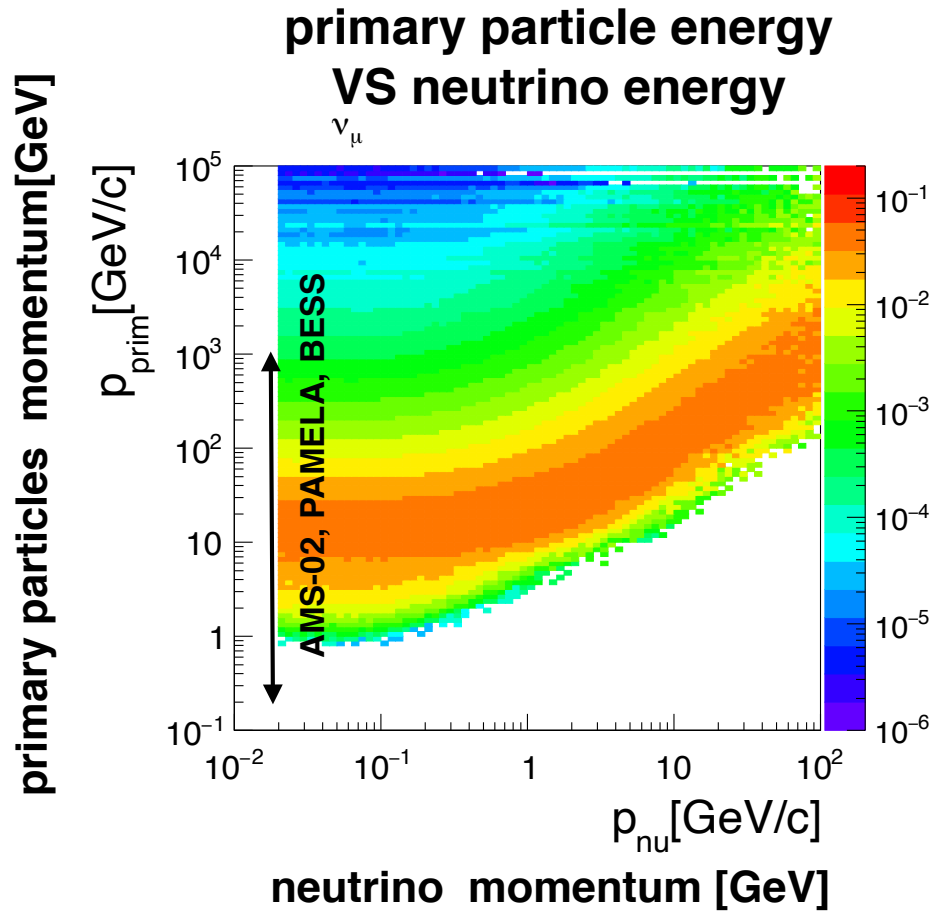
data covers >20 years solar activity →

Data taking period and Solar activity

BESS (APJ 822 65 (2016))



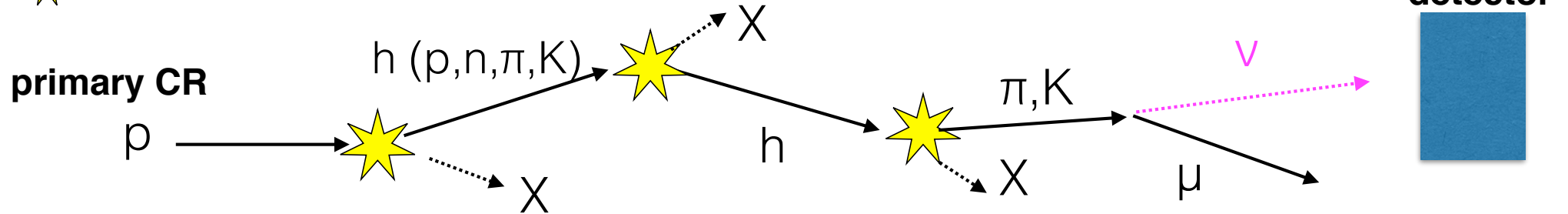
primary particle energy of interest



- Accurate measurement of primary flux up to 1TeV
= improvement for $E_\nu < 10\text{GeV}$ ν flux accuracy

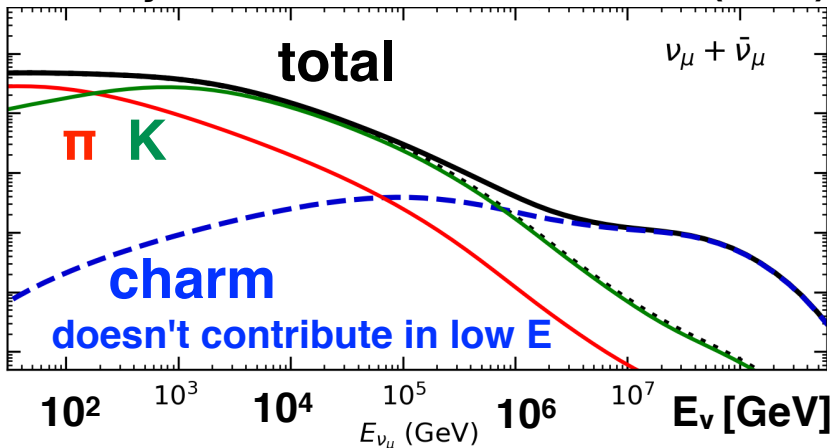
hadronic interactions

★ : hadron interaction with nucleus in air

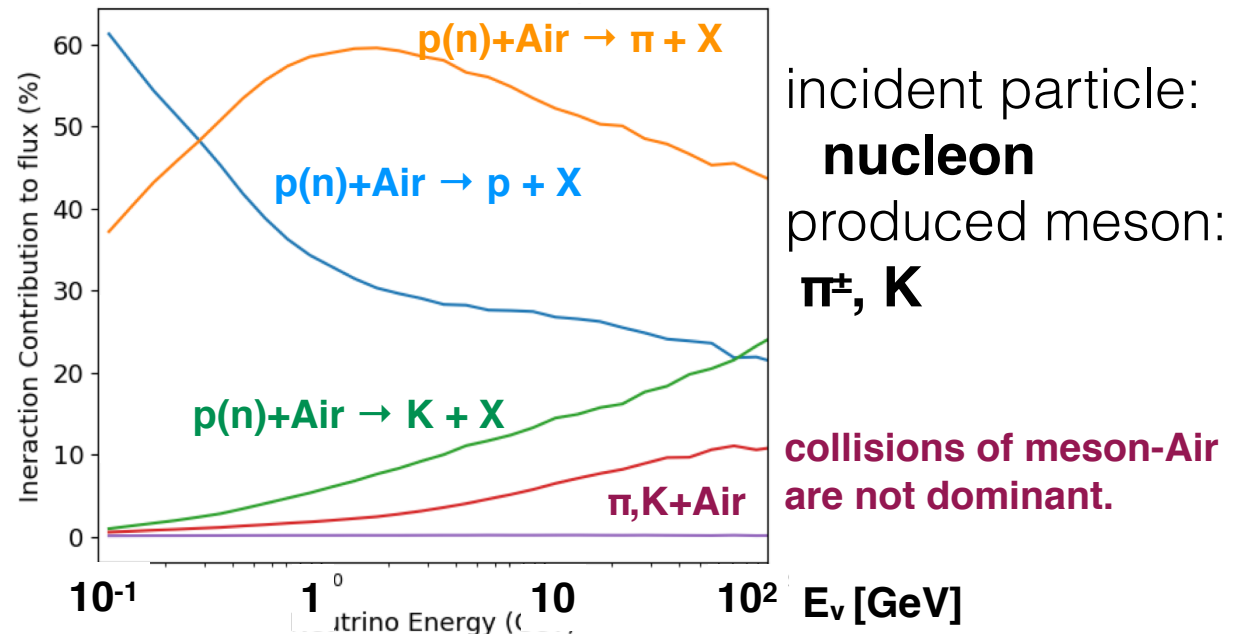


- chain of hadron interactions before producing ν
- hadron production $d^3\sigma/dp^3$ on each vertex contributes to ν flux uncertainty

parent hadron of ν_μ
A. Fedynitch et.al. PRD100, 103018 (2019)



types of hadron interactions on the chain
(plot by L. Cook w/ Bartol flux simulation)



→ **p + Air → π, K + X** is important

accelerator-data-driven tuning

Hadronic interactions are calculated with event generator

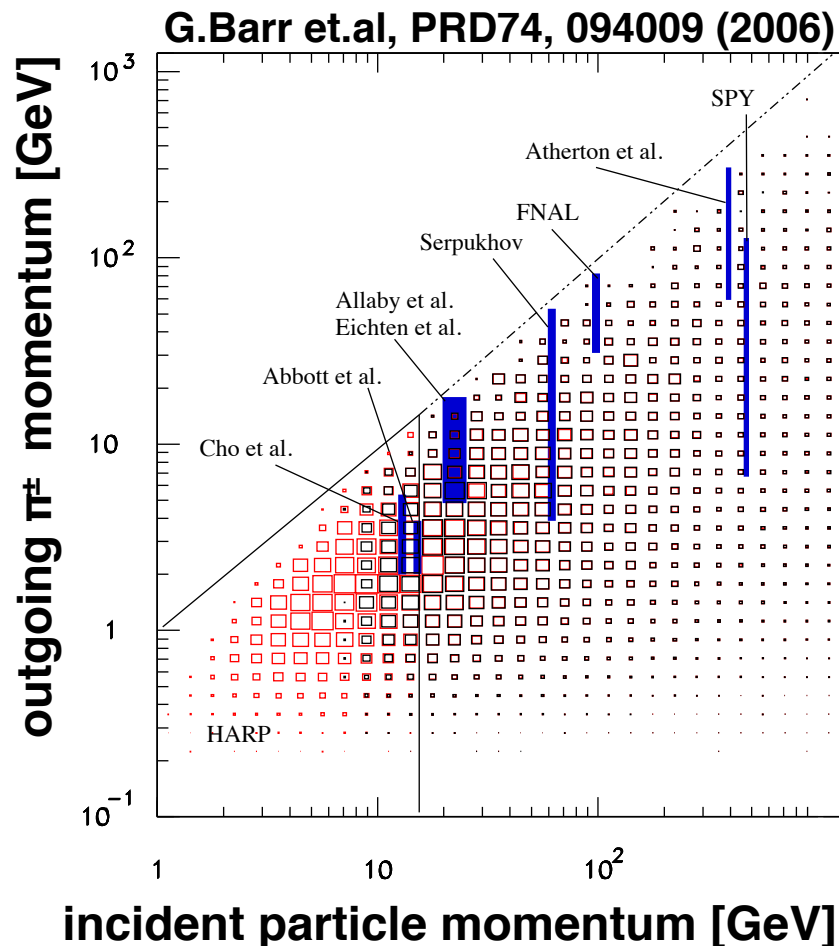
Honda flux MC : JAM & dpmJet3 with tuning based on atm. μ

Bartol flux MC : Target 2.4

→ activity for **accelerator-data-driven tuning** has started.

Nagoya group : K. Sato, Y. Itow, H. Menjo (+ M. Honda)

Bartol group : L. Cook, G. Barr, M. Hartz (+T.K Gaisser, T. Stanev)



- Tune the hadron interactions in MC based on **accelerator data**

Both group are working independently
→ **cross-check**

accelerator-data-driven tuning

Hadronic interactions are calculated with event generator

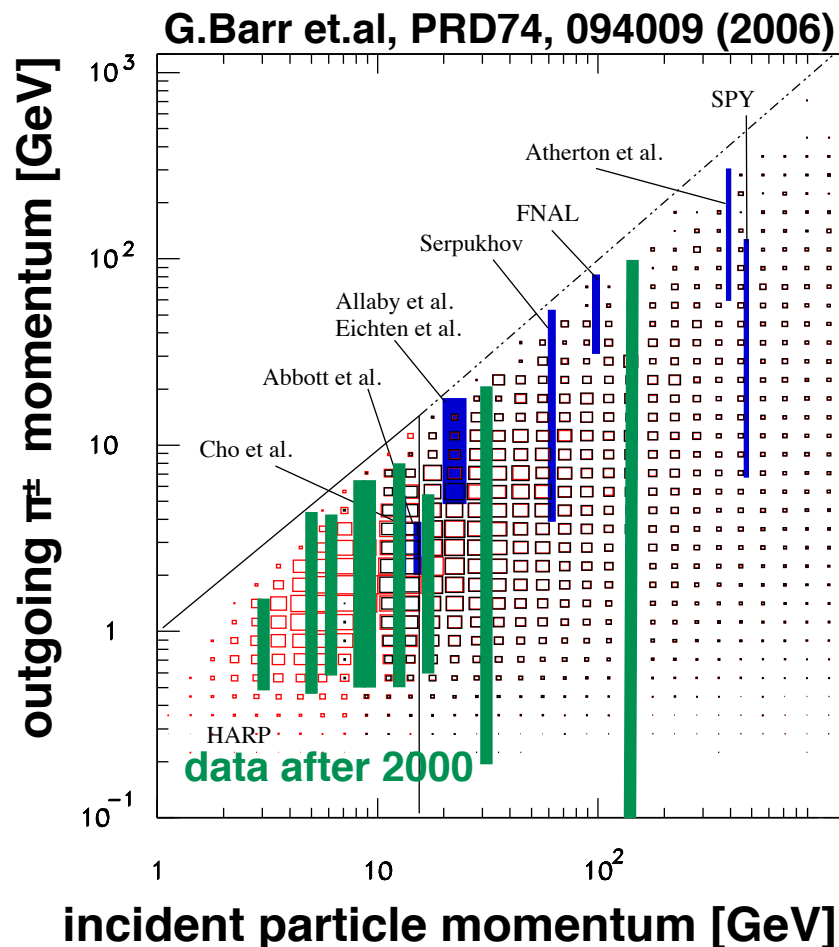
Honda flux MC : JAM & dpmJet3 with tuning based on atm. μ

Bartol flux MC : Target 2.4

→ activity for **accelerator-data-driven tuning** has started.

Nagoya group : K. Sato, Y. Itow, H. Menjo (+ M. Honda)

Bartol group : L. Cook, G. Barr, M. Hartz (+T.K Gaisser, T. Stanev)



$\pi^\pm$ & $K^\pm$ production meas. in 2000s

• **NA61, NA49, HARP, E910, ...**

→ tune the differential cross-section for hadron production in MC

weight for tuning:

$$w = \frac{\left(\frac{d\sigma}{dpd\Omega}\right)_{data}}{\left(\frac{d\sigma}{dpd\Omega}\right)_{MC}}$$

based on
measurements

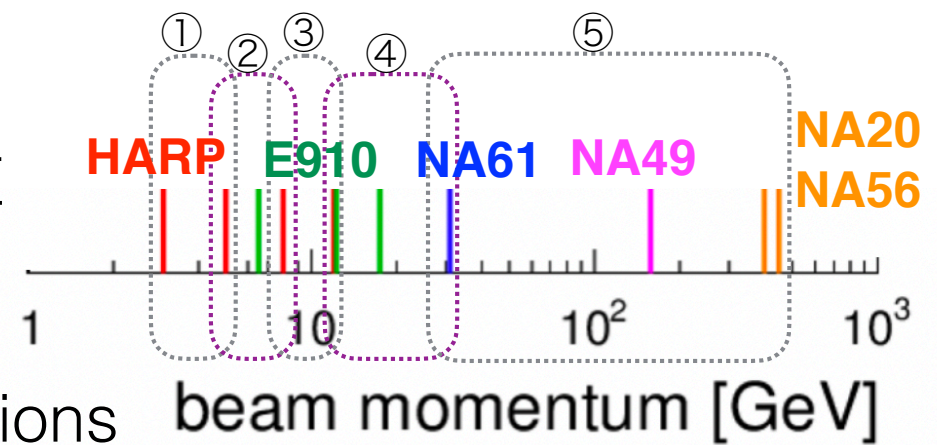
used in MC 12

Nagoya group data fit

Interpolation between discrete beam E is a challenge.

- Feynman scaling is not applicable.

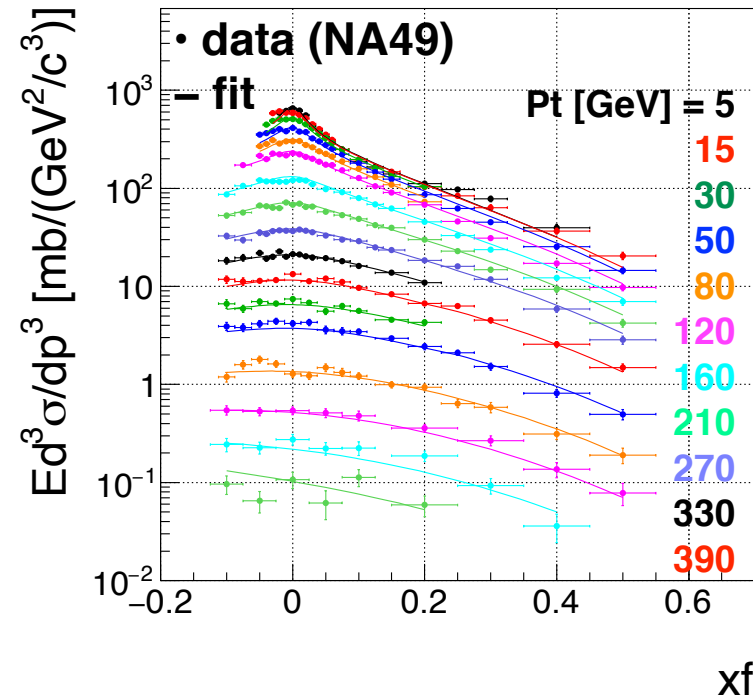
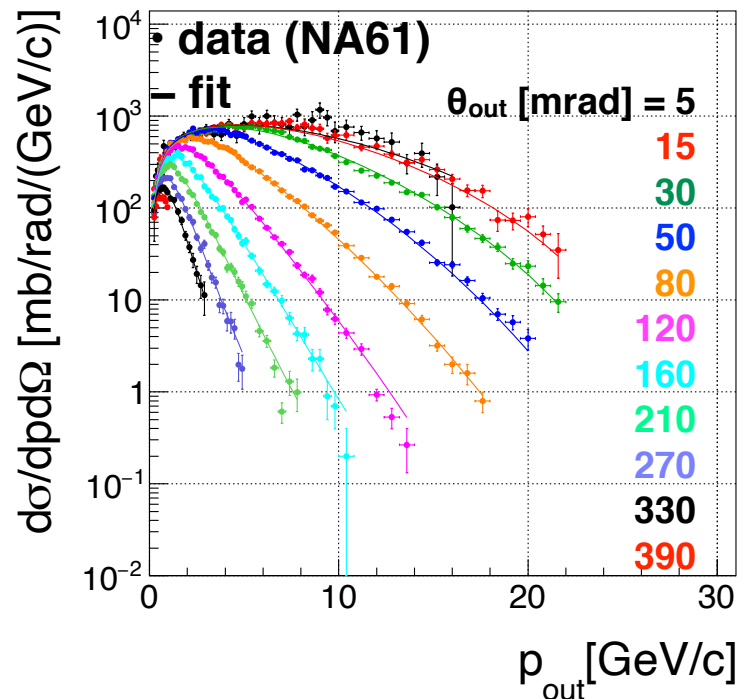
→ grouped beam data into small sections



$$f_{fit} = f_{pp} \times f_{pA_0/pp} \times f_{A/A_0} \times \left(1 + C_1 \log_{10} \frac{p_{beam}}{C_2} \right) \quad \text{beam E dependence}$$

result of simultaneous fit for π^+ data in group ⑤ (NA61, NA49, NA56)

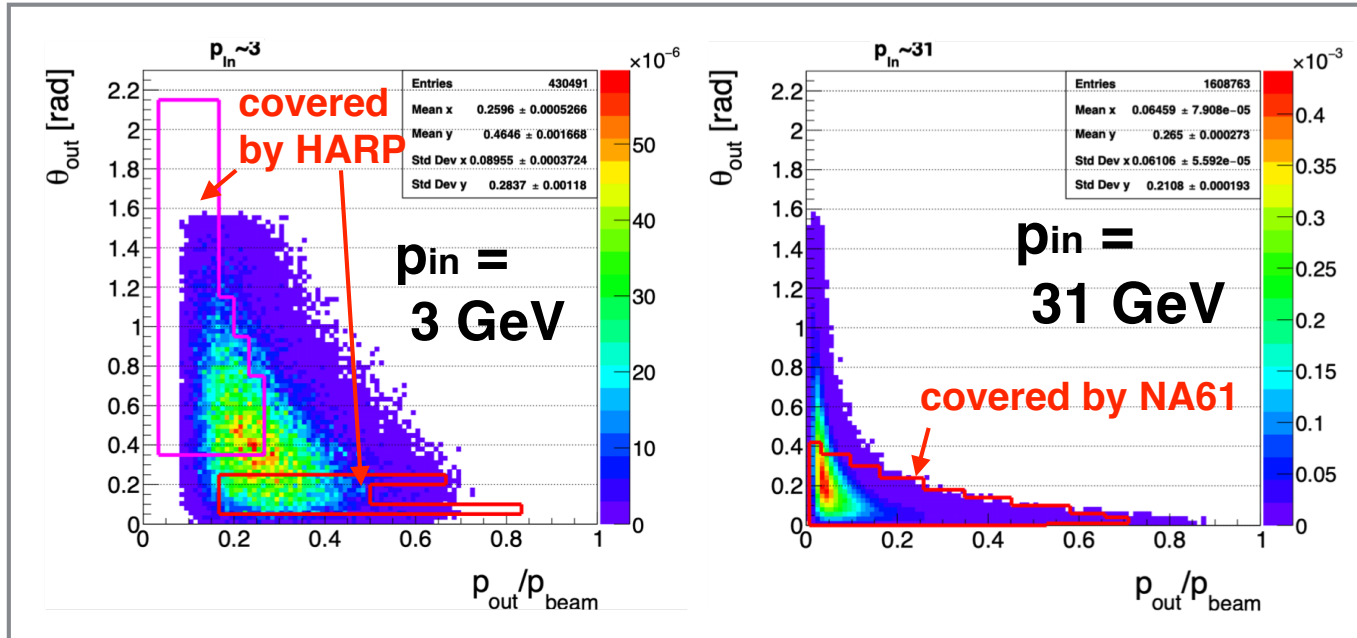
$$\chi^2 / \text{NDF} = 1227 / 692$$



→ reduced $\chi^2 < \sim 2$ in all energy range

phase space coverage

ex) phase space of π^+ production for 0.3 GeV ν_μ

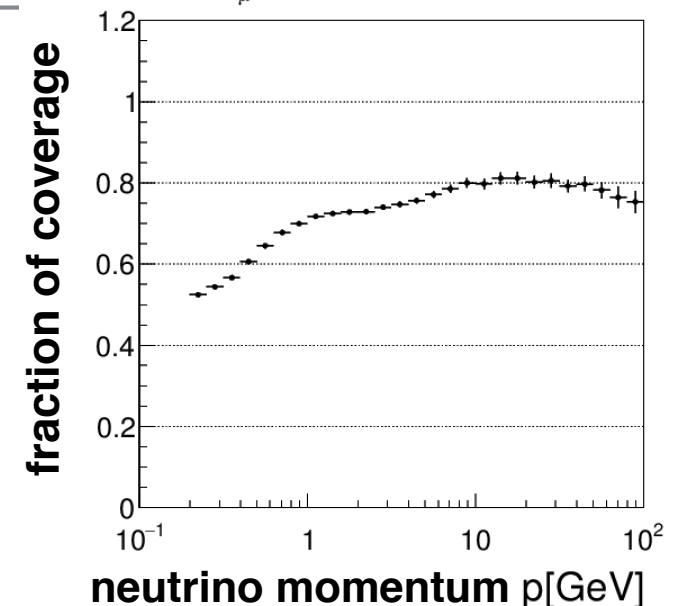


← hadron production phase space (PS) as a function of p_{in} , p_{out} , θ_{out}

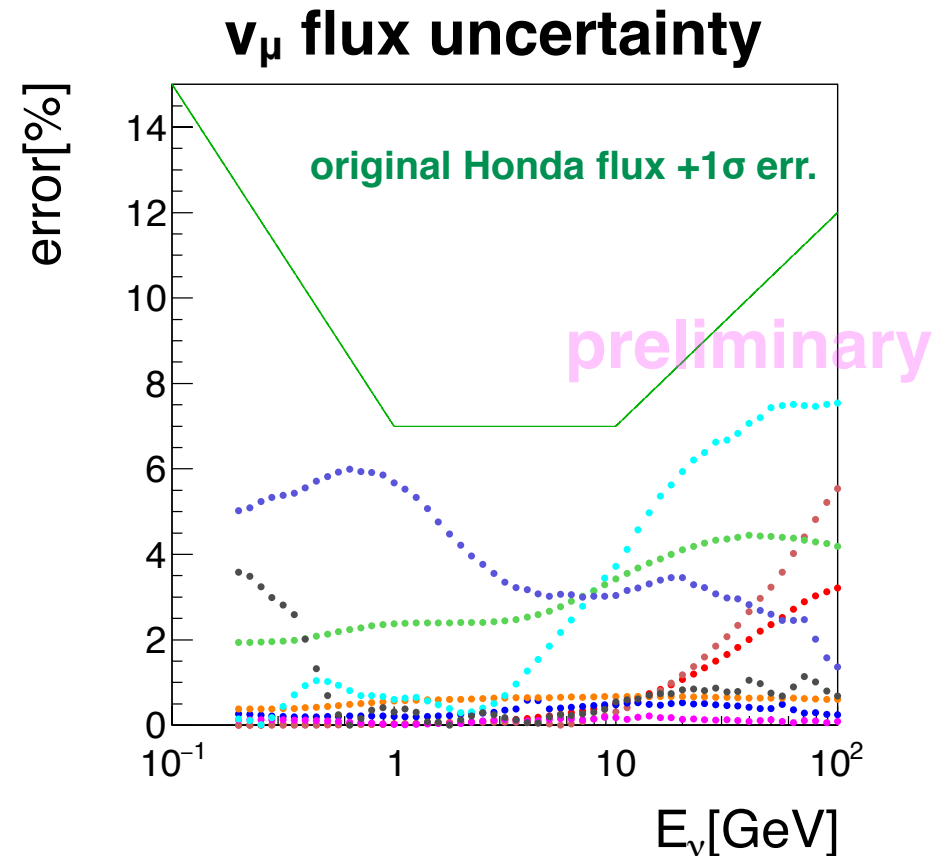
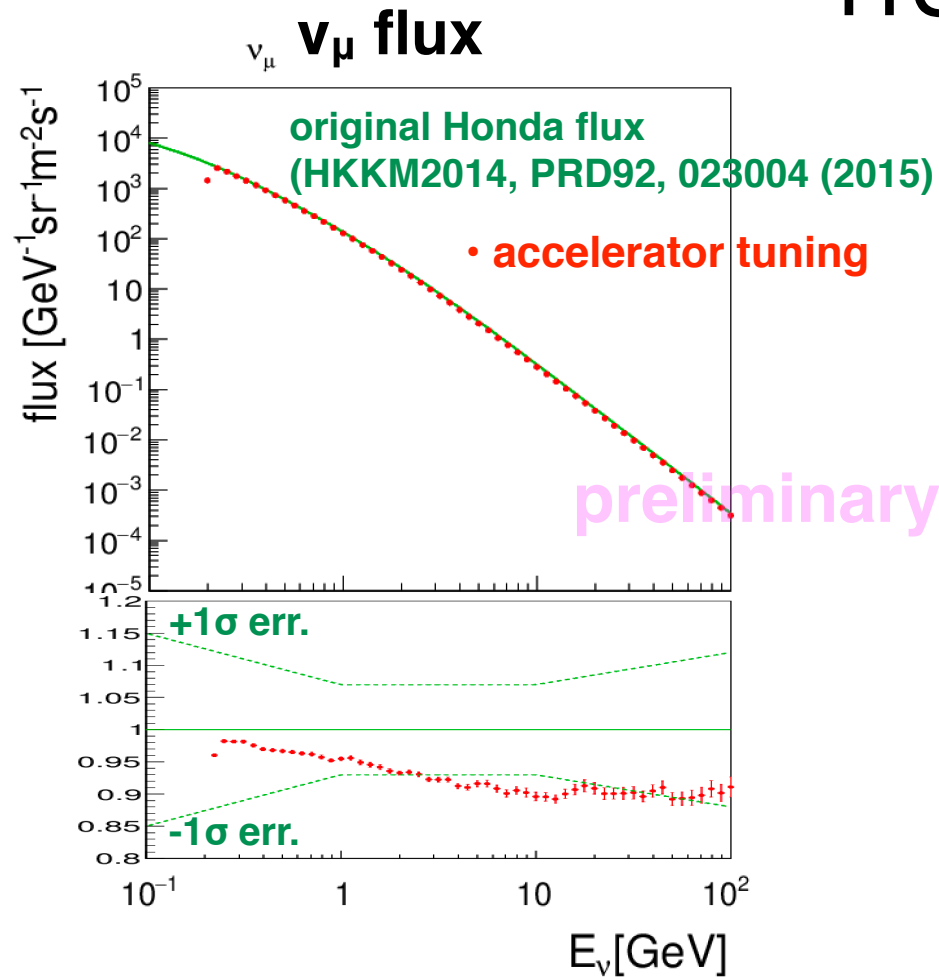
phase space coverage for ν_μ

- good ($\sim 80\%$) PS coverage for ~ 10 GeV ν
 - due to wide PS of NA61 & NA49
- lower coverage in $E_\nu < 1$ GeV
 - due to lack of $E_{beam} < 3\text{GeV}$ beam data

→ shortage of phase space is considered as systematic uncertainty of ν flux.



flux & uncertainty



- Honda flux uncertainty was originally evaluated using atm. μ data

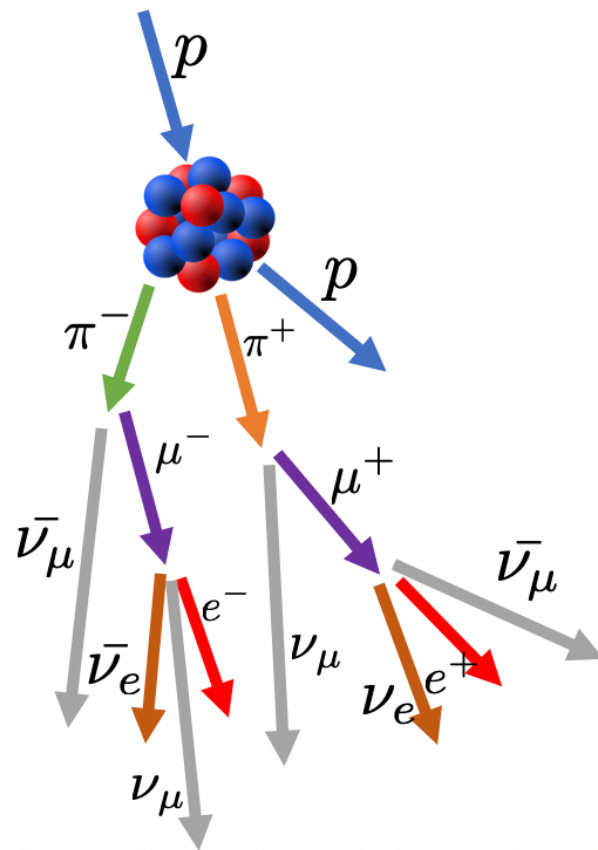
(M. Honda et.al., PRD75, 043005 (2007))

→ large Error in $< 1\text{GeV}$ & $> 10\text{GeV}$

- measurement error of beam data in each bin
- normalization of beam data
- parameterization
- Feynman scaling (x_F - p_T shape)
- Feynman scaling (normalization)
- coverage of phase space
- atomic mass dependence

→ will be able to reduce uncertainty of Honda flux (preliminary)

Tuning of the Bartol Atmospheric Neutrino Flux



- Tuning the Bartol Neutrino Flux to Pion and Kaon production datasets from fixed target experiments
- Reweighting neutrino flux based on ratio of meson multiplicity in data to multiplicity in Monte Carlo

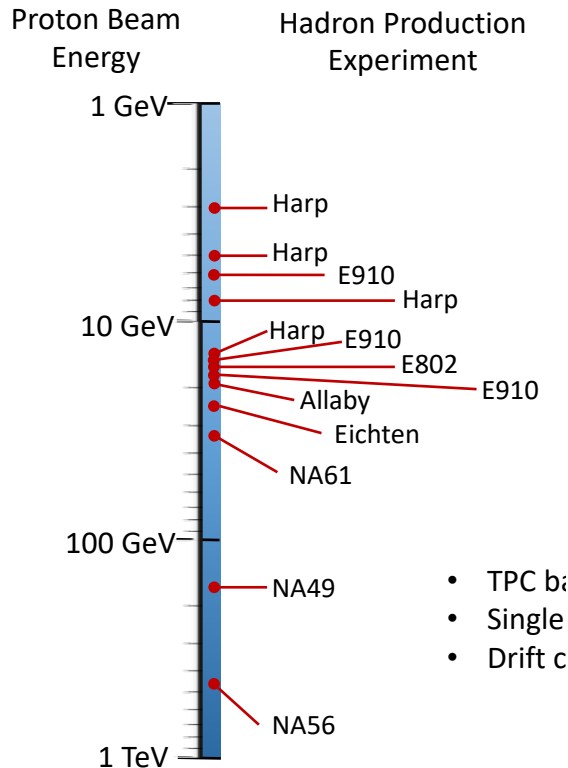
$$W = \frac{dn_{\text{data}}(\pi^+)}{dx_F dP_T} / \frac{dn_{\text{MC}}(\pi^+)}{dx_F dP_T}$$

- Consider interactions as described in terms of inclusive production cross sections e.g.

$$\sigma(pN \rightarrow \pi^+ + X)$$

data-driven tuning in Bartol flux

data set



→ grouped into 7 regions

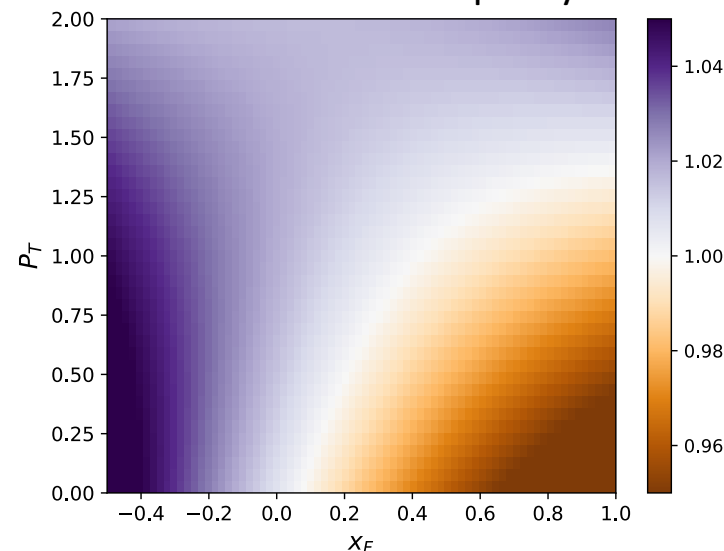
groups	
• 3 GeV	• 12, 12.3, 14.6 GeV
• 5, 6.4 GeV	• 17.5, 19.2, 24 GeV
• 8 GeV	• 31 GeV
	• 158 GeV

$$\frac{d^2\sigma(A)}{dx_F dP_T} = \frac{A^{\alpha(x_F, P_T)}}{2} \frac{d^2\sigma_{\text{BMPT}}}{dx_F dP_T}$$

A-scaling
(target atom dependence)

BMPT parameterization
Eur.Phys.J.C20,13 (2001)

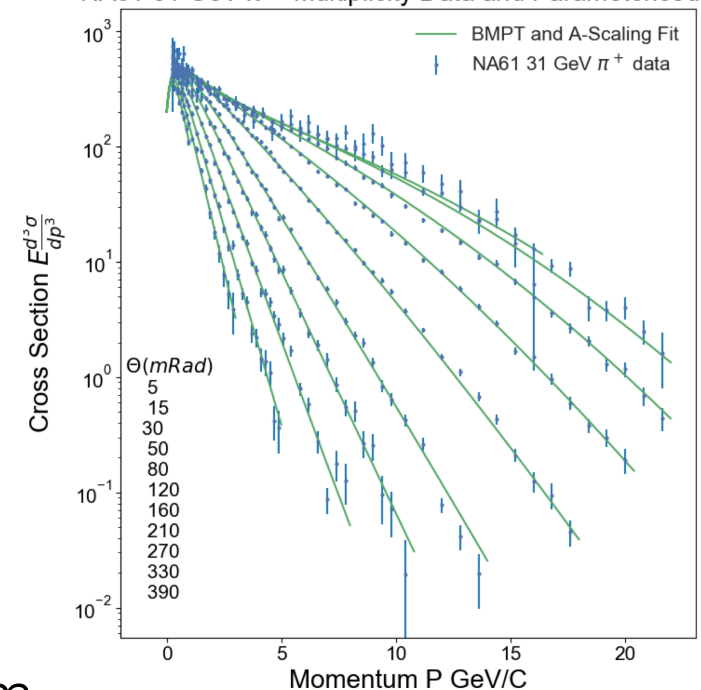
Ratio of Nitrogen to Carbon A-Scaling
On Pi Plus Multiplicity



- derive A-scaling from Be, C, & Al target data

NA61 π^+ fit result

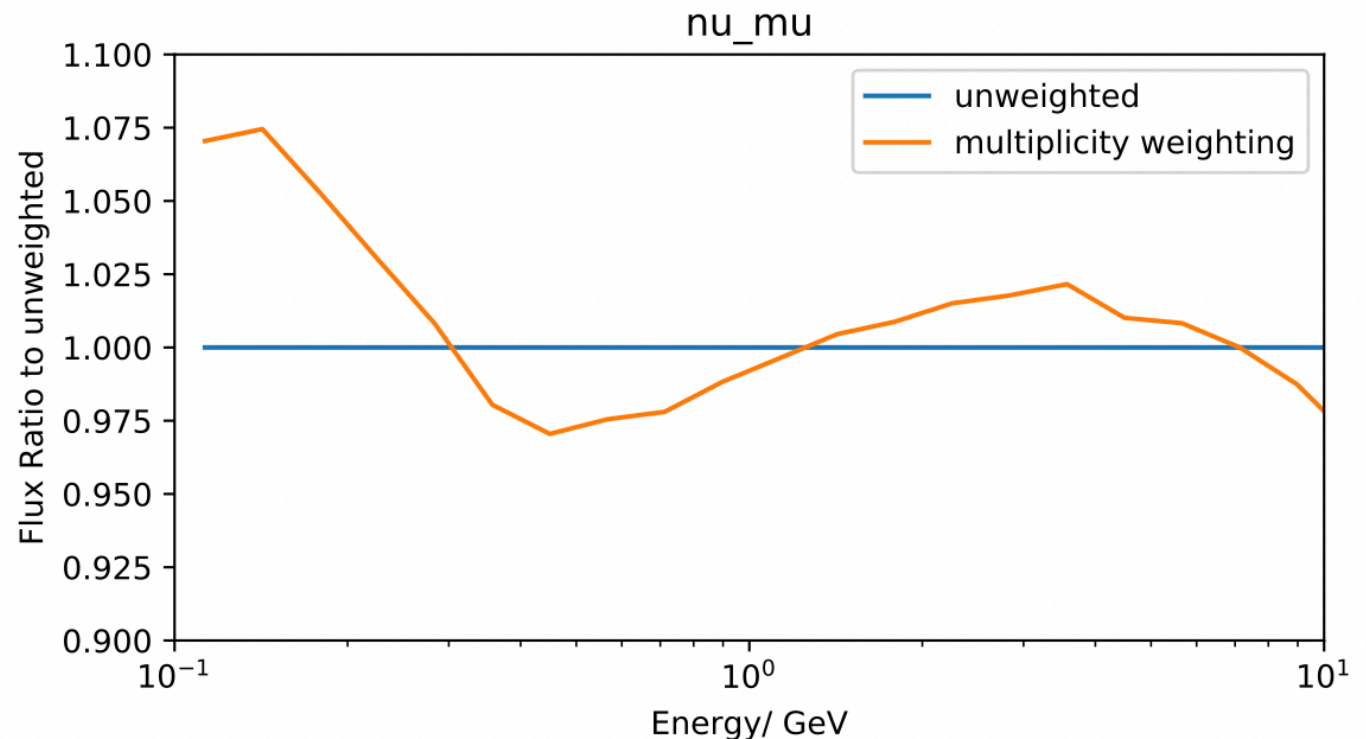
NA61 31 GeV π^+ Multiplicity Data and Parameterised Fit



- fit function well describes the data

Tuned neutrino flux results

- Within the previous 10% uncertainty
- Low energy increase from high angle dataset tuning
- Systematic Uncertainty on the tuned fluxes to be released shortly



Works in both groups are in progress

→ consistency checks between **Honda flux** and **Bartol flux** will be started soon.

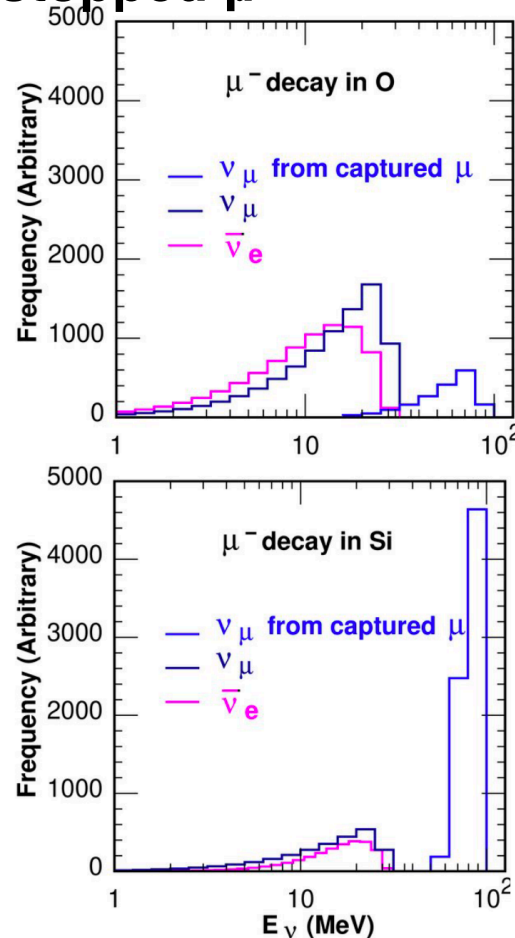
flux in $< 100 \text{ MeV}/c$

ref) Wan-Lei Guo, PRD99, 073007 (2019)

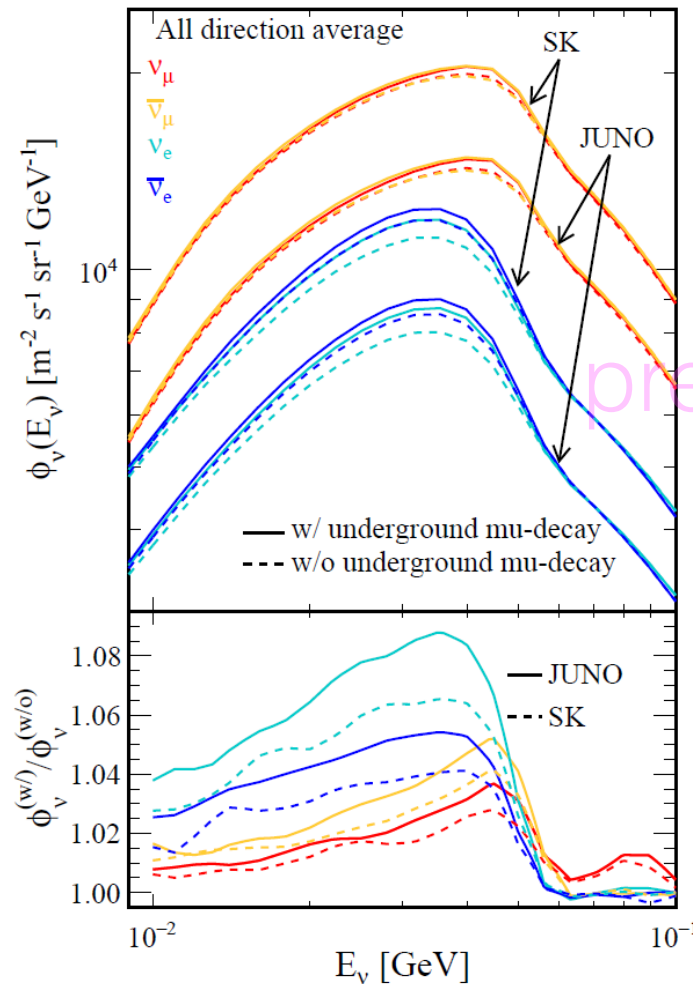
M. Honda's poster in Neutrino2020

- plot provided by Yu-Feng Li (JUNO collaboration)

neutrino energy from stopped μ



- need to consider decays of atm. μ stopped in rock or water



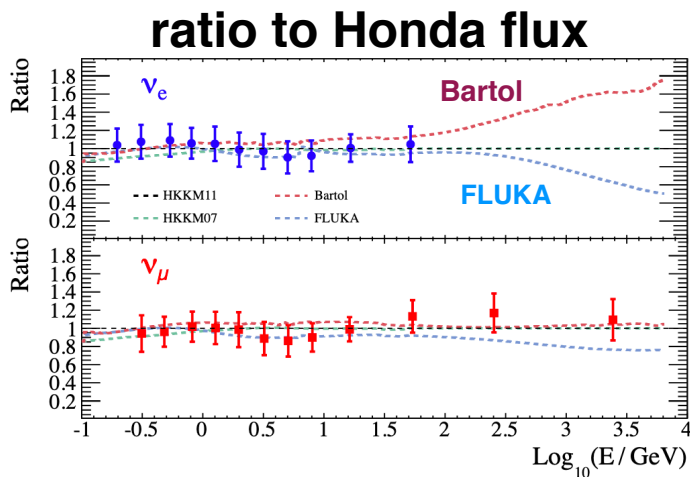
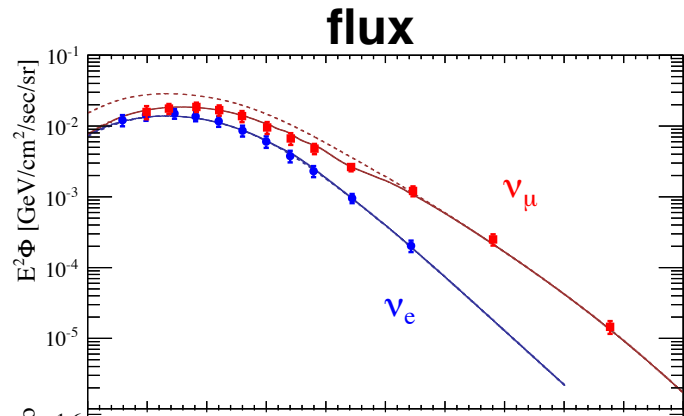
- ν from μ at rest
→ enhancement in $< 50 \text{ MeV}$ flux

- depends on geographical features of observation site

ν flux measurement

ν flux measurement in SK (ν_e : >158 MeV, ν_μ : >400 MeV)

ref) E. Richard et.al. (SK collaboration) , PRD 94, 052001 (2016)



i	$\log_{10}(E/\text{GeV})$	$\log_{10}(E_i/\text{GeV})$	$E_i^2 \Phi_i^\nu$ [GeV/cm ² /sec/sr]	$\Delta\Phi_i^\nu/\Phi_i^\nu$ [%]
ν_e				
1	-0.8 – -0.6	-0.71	1.21×10^{-2}	± 18
2	-0.6 – -0.4	-0.51	1.46×10^{-2}	± 17
3	-0.4 – -0.2	-0.27	1.50×10^{-2}	± 16
4	-0.2 – 0.0	-0.09	1.37×10^{-2}	± 15
5	0.0 – 0.2	0.10	1.16×10^{-2}	± 17
6	0.2 – 0.4	0.30	8.55×10^{-3}	± 17
7	0.4 – 0.6	0.50	6.09×10^{-3}	± 18
8	0.6 – 0.8	0.70	3.73×10^{-3}	± 19
9	0.8 – 1.0	0.90	2.32×10^{-3}	± 18
10	1.0 – 1.5	1.22	9.42×10^{-4}	± 15
11	1.5 – 2.0	1.72	2.03×10^{-4}	± 18

measurement
error : 16~20%

dominantly
 ν interaction
cross section

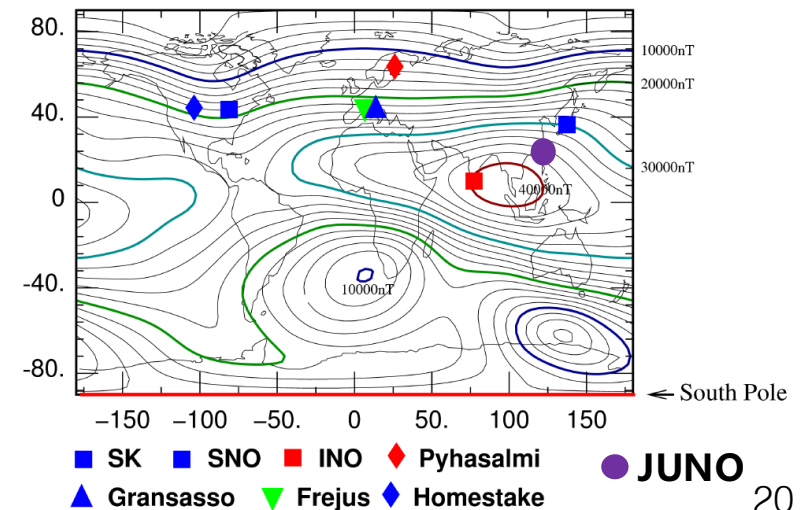
- important to constrain the prediction

- Measurement in different places

e.g.) JUNO, EPJ. C, 81 10 (2021) 887

will be interesting to varify the prediction

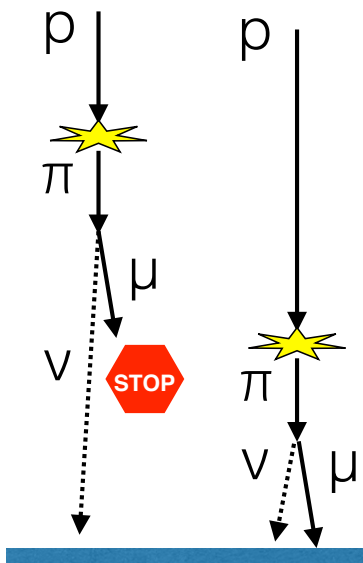
Geomagnetic field model



muon flux measurement

- atm. μ is useful for calibration/uncertainty evaluation of ν flux
- Honda flux is calibrated based on atm. μ

M. Honda et.al., PRD75, 043005 (2007)



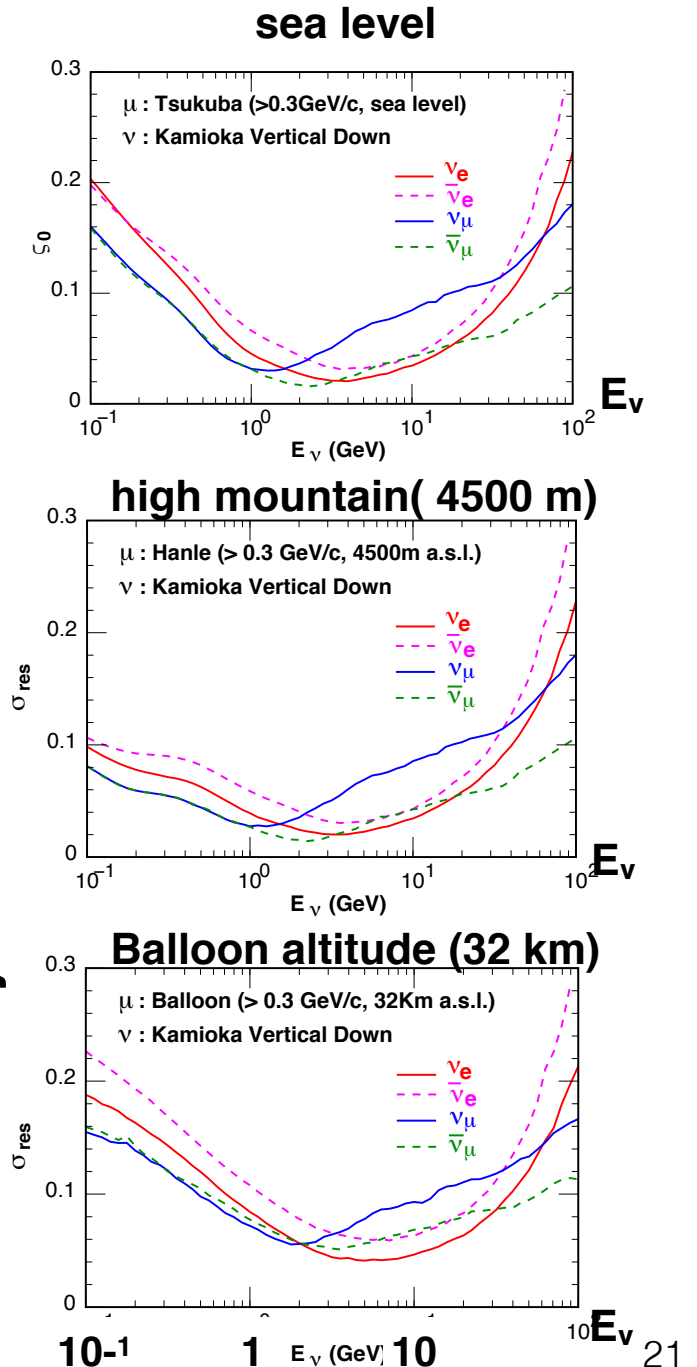
- Both ν and μ carry information of π production
- Phase space covered by μ data depends on detector altitude

Systematic study by Honda et.al.

M. Honda et.al., PRD 100, 123022 (2019)

→ measurement in high mountain is effective

uncertainty of neutrino flux with muon calibration



Summary

- atm. ν in low E region (0.1--100GeV)
 - important as both physics target and background
 - accurate prediction is key point
- uncertainties of ν flux prediction
 - flux of primary particle
 - good improvement from recent measurements
 - hadron production
 - accelerator-data-driven tuning is ongoing for both Honda flux & Bartol flux
- Measurements of atm. ν and μ will be useful to calibrate prediction