

Three neutrino phenomenology and global analyses

Neutrino 2022, 1 June 2022, Virtual Seoul



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Outline

- Global oscillation analysis in the three-neutrino framework
- Comment on neutrino mass ordering determination from cosmology
- Proposal for a model-independent test for T-violation

Neutrino mass implies physics beyond the SM

- effective low-energy description: $\mathcal{L}_{M_\nu} = \frac{1}{2} \overline{\nu}_{aL}^c m_{ab} \nu_{bL}$
- not gauge invariant, new physics origin of m_{ab}
- **low-energy phenomenology** encoded in m_{ab}
symmetric complex matrix \rightarrow 9 real physical parameters:
 - 6 **neutrino oscillation** params: $\Delta m_{21}^2, \Delta m_{31}^2, \theta_{12}, \theta_{13}, \theta_{23}, \delta_{CP}$ } good prospects to determine experimentally
 - 1 **absolute mass** observable: lightest neutrino mass m_0
 - 2 Majorana phases α, β (**neutrinoless double beta decay**) } absent for Dirac neutrinos

Three flavour oscillation parameters

global analysis **NuFIT 5.1 results** www.nu-fit.org

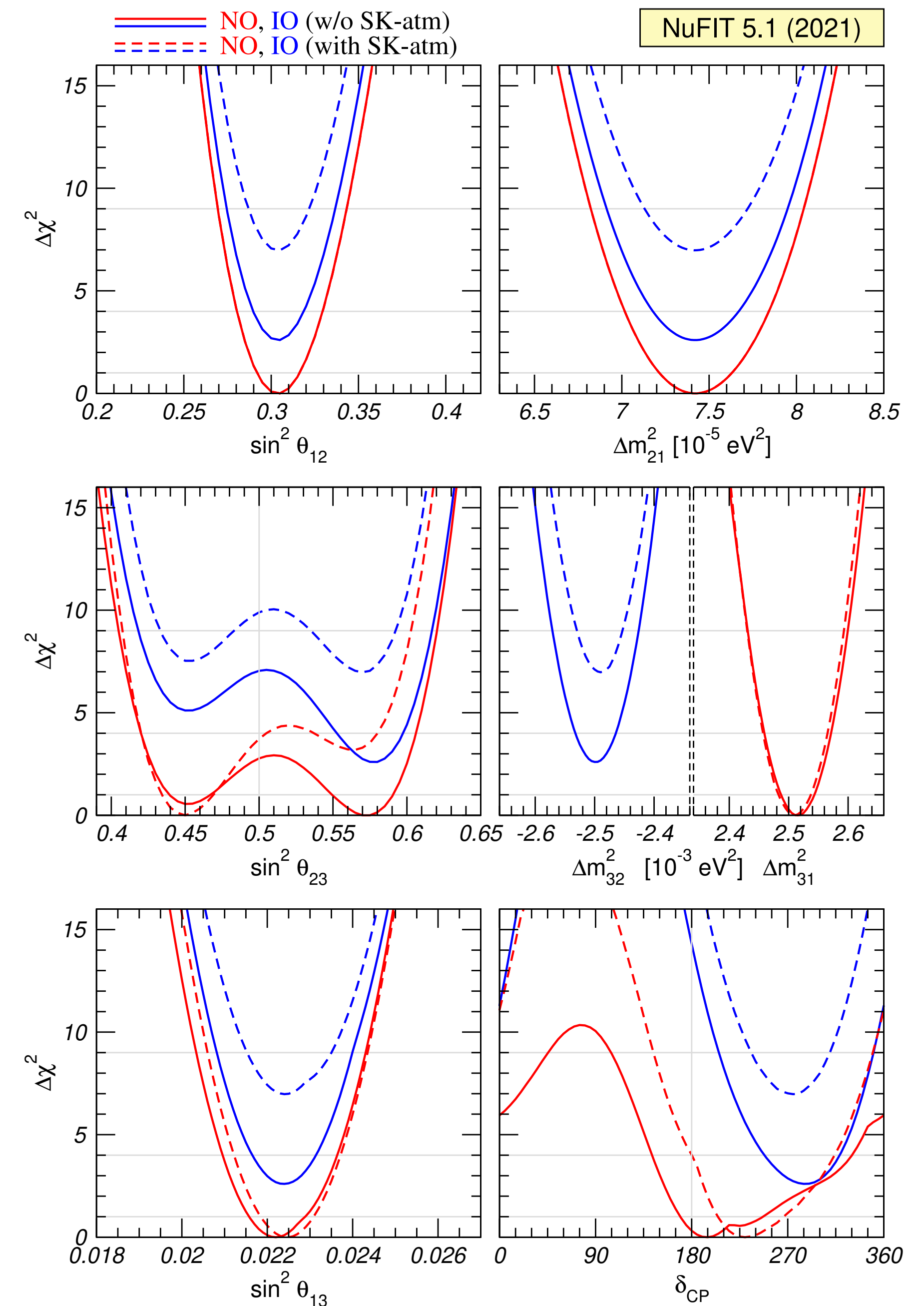
Esteban, Gonzalez-Garcia, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792]

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 7.0$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.45^{+0.77}_{-0.75}$	$31.27 \rightarrow 35.87$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.450^{+0.019}_{-0.016}$	$0.408 \rightarrow 0.603$	$0.570^{+0.016}_{-0.022}$	$0.410 \rightarrow 0.613$
	$\theta_{23}/^\circ$	$42.1^{+1.1}_{-0.9}$	$39.7 \rightarrow 50.9$	$49.0^{+0.9}_{-1.3}$	$39.8 \rightarrow 51.6$
	$\sin^2 \theta_{13}$	$0.02246^{+0.00062}_{-0.00062}$	$0.02060 \rightarrow 0.02435$	$0.02241^{+0.00074}_{-0.00062}$	$0.02055 \rightarrow 0.02457$
	$\theta_{13}/^\circ$	$8.62^{+0.12}_{-0.12}$	$8.25 \rightarrow 8.98$	$8.61^{+0.14}_{-0.12}$	$8.24 \rightarrow 9.02$
	$\delta_{CP}/^\circ$	230^{+36}_{-25}	$144 \rightarrow 350$	278^{+22}_{-30}	$194 \rightarrow 345$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.510^{+0.027}_{-0.027}$	$+2.430 \rightarrow +2.593$	$-2.490^{+0.026}_{-0.028}$	$-2.574 \rightarrow -2.410$

comparable results:

Bari: e.g. Capozzi et al., 2107.00532

Valencia: e.g. deSalas et al., 2006.11237



Evolution of global 3 flavour fit

Gonzalez-Garcia, Maltoni, TS [arXiv:2111.03086]

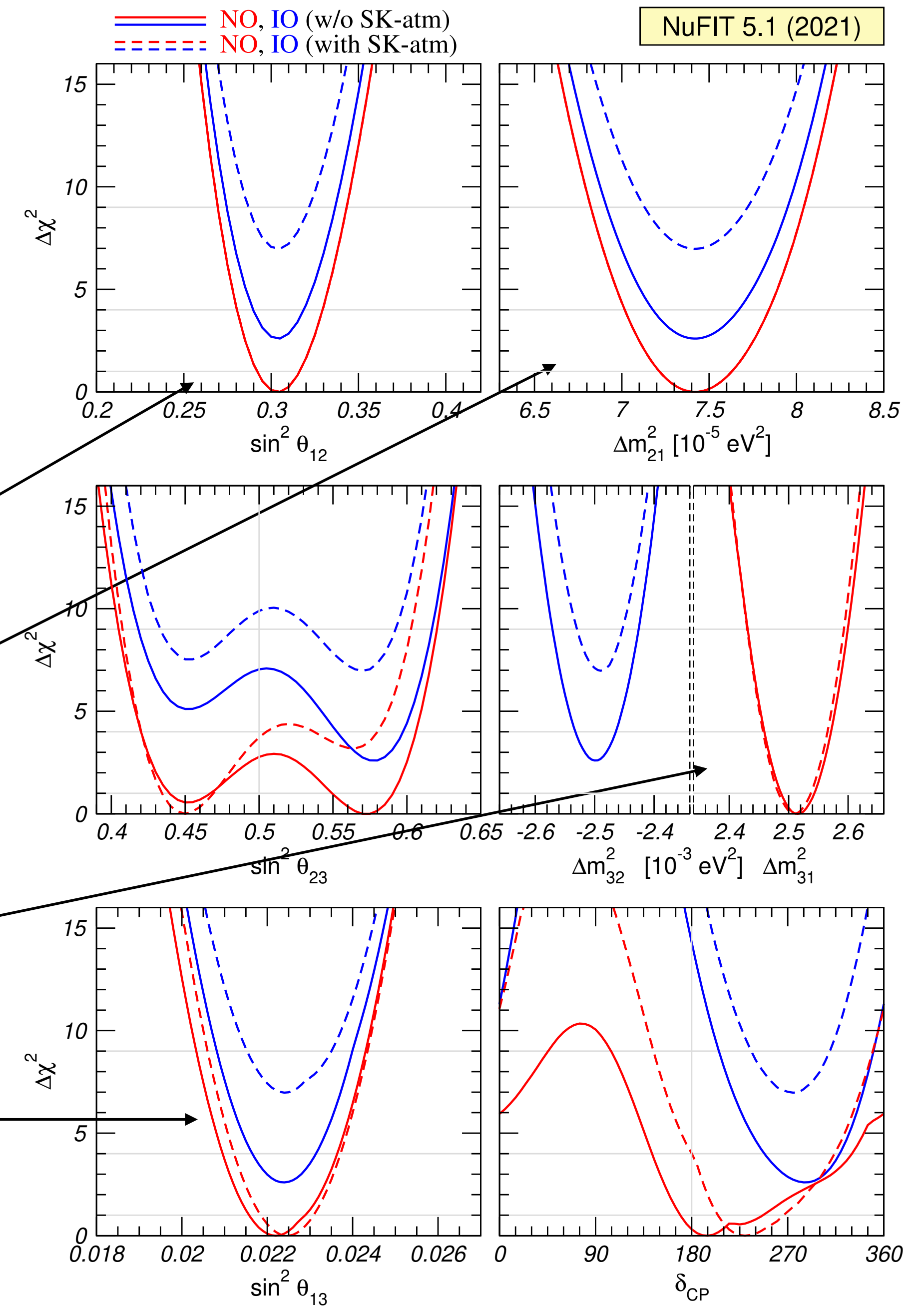
	2012	2014	2016	2018	2021	
	NuFIT 1.0	NuFIT 2.0	NuFIT 3.0	NuFIT 4.0	NuFIT 5.1	
θ_{12}	15%	14%	14%	14%	14%	1.07
θ_{13}	30%	15%	11%	8.9%	9.0%	3.3
θ_{23}	43%	32%	32%	27%	27%	1.6
Δm_{21}^2	14%	14%	14%	16%	16%	0.88
$ \Delta m_{3\ell}^2 $	17%	11%	9%	7.8%	6.7% [6.5%]	2.5
δ_{CP}	100%	100%	100%	100% [92%]	100% [83%]	1 [1.2]
$\Delta\chi^2_{\text{IO-NO}}$	± 0.5	-0.97	$+0.83$	$+4.7$ [$+9.3$]	$+2.6$ [$+7.0$]	
w/o [w] SK atm data						
relat. precision at 3σ : $\frac{2(x^+ - x^-)}{(x^+ + x^-)}$						
improvement factor from 2012 to 2021						

Four well-known parameters

NuFIT 5.1 results www.nu-fit.org

- robust determination
(relat. precision at 3σ)

θ_{12} (14%)
 Δm_{21}^2 (16%)
 $|\Delta m_{31}^2|$ (7%)
 θ_{13} (9%)



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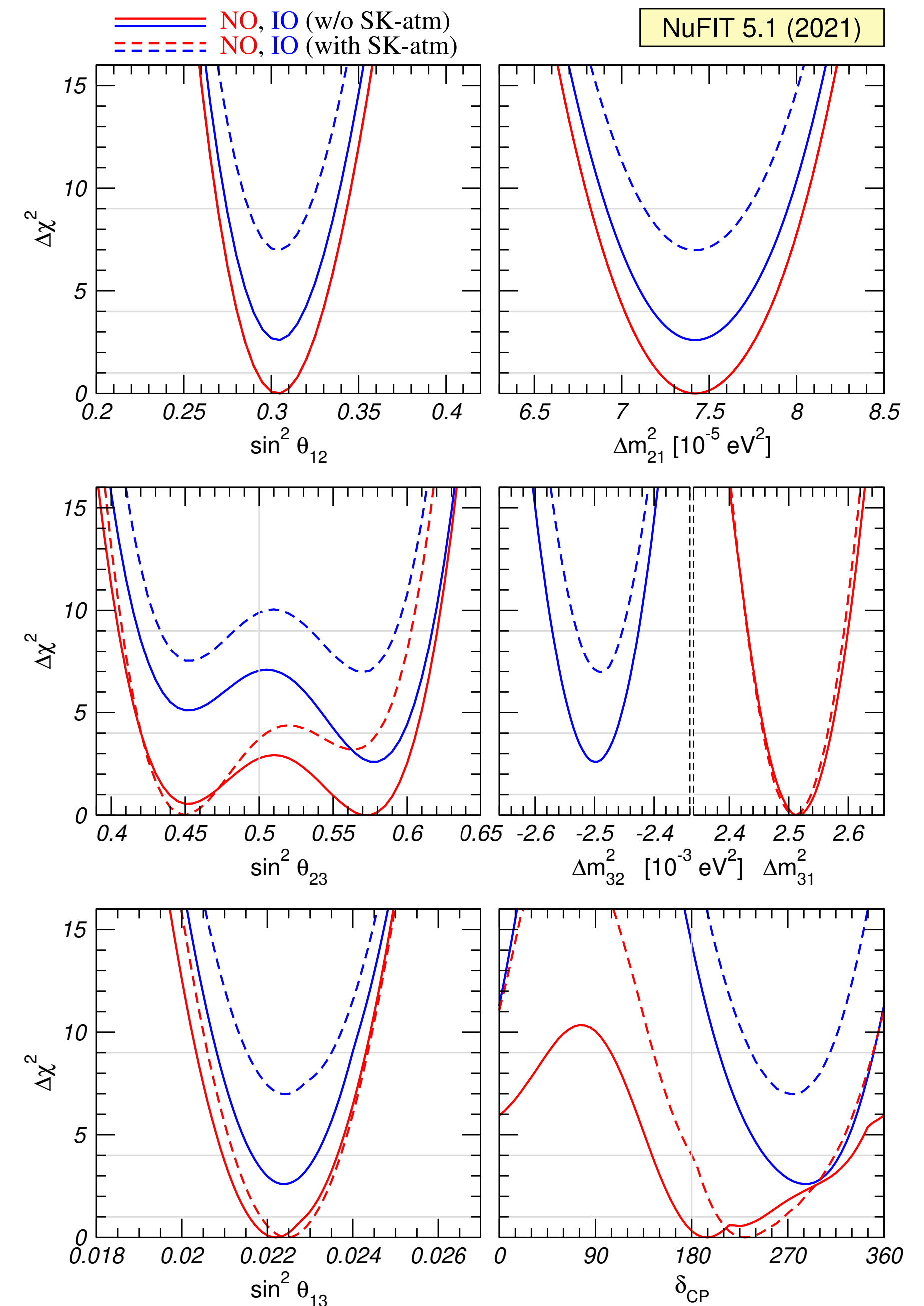
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for quarks



0.6 %

8.3 %



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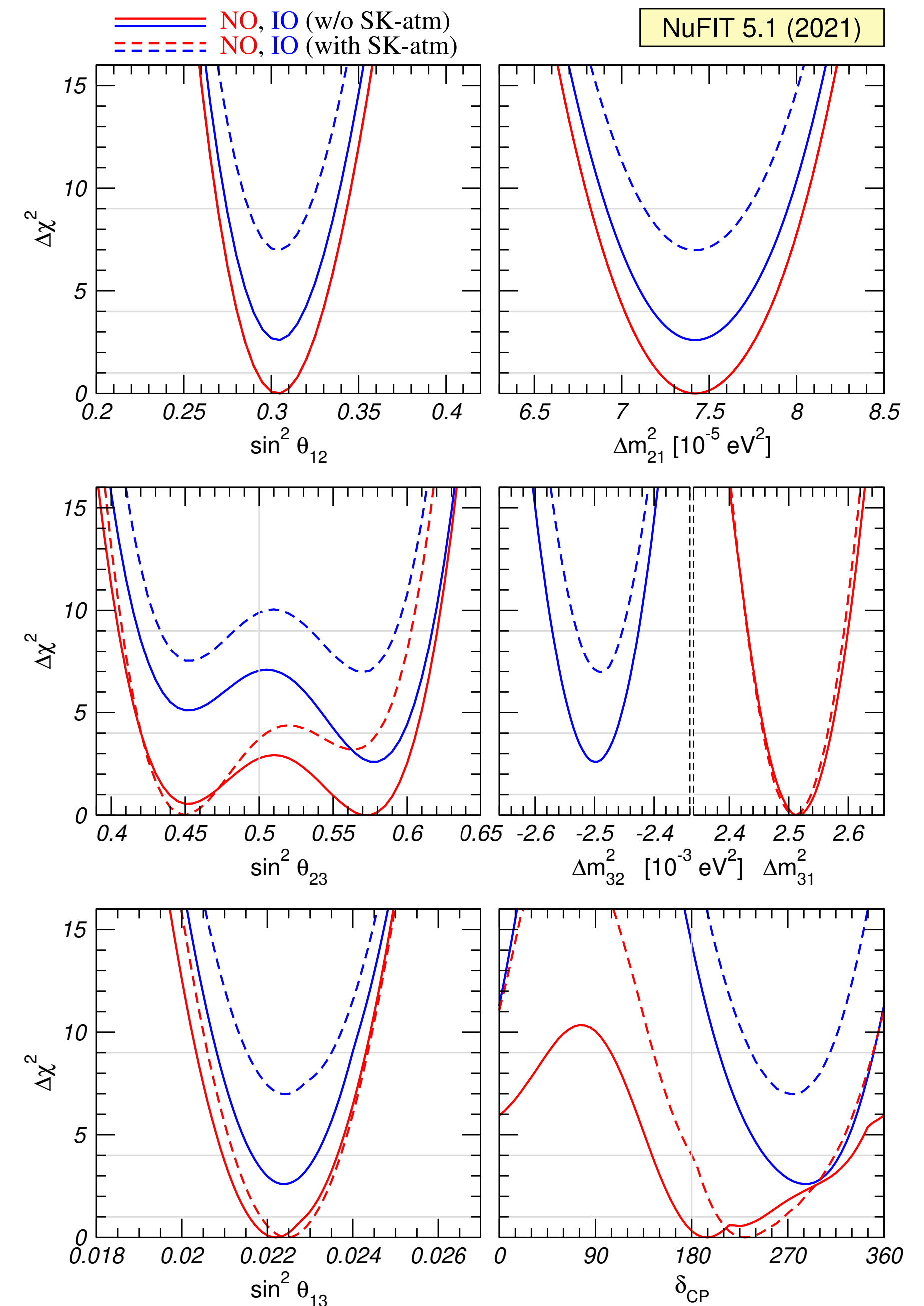
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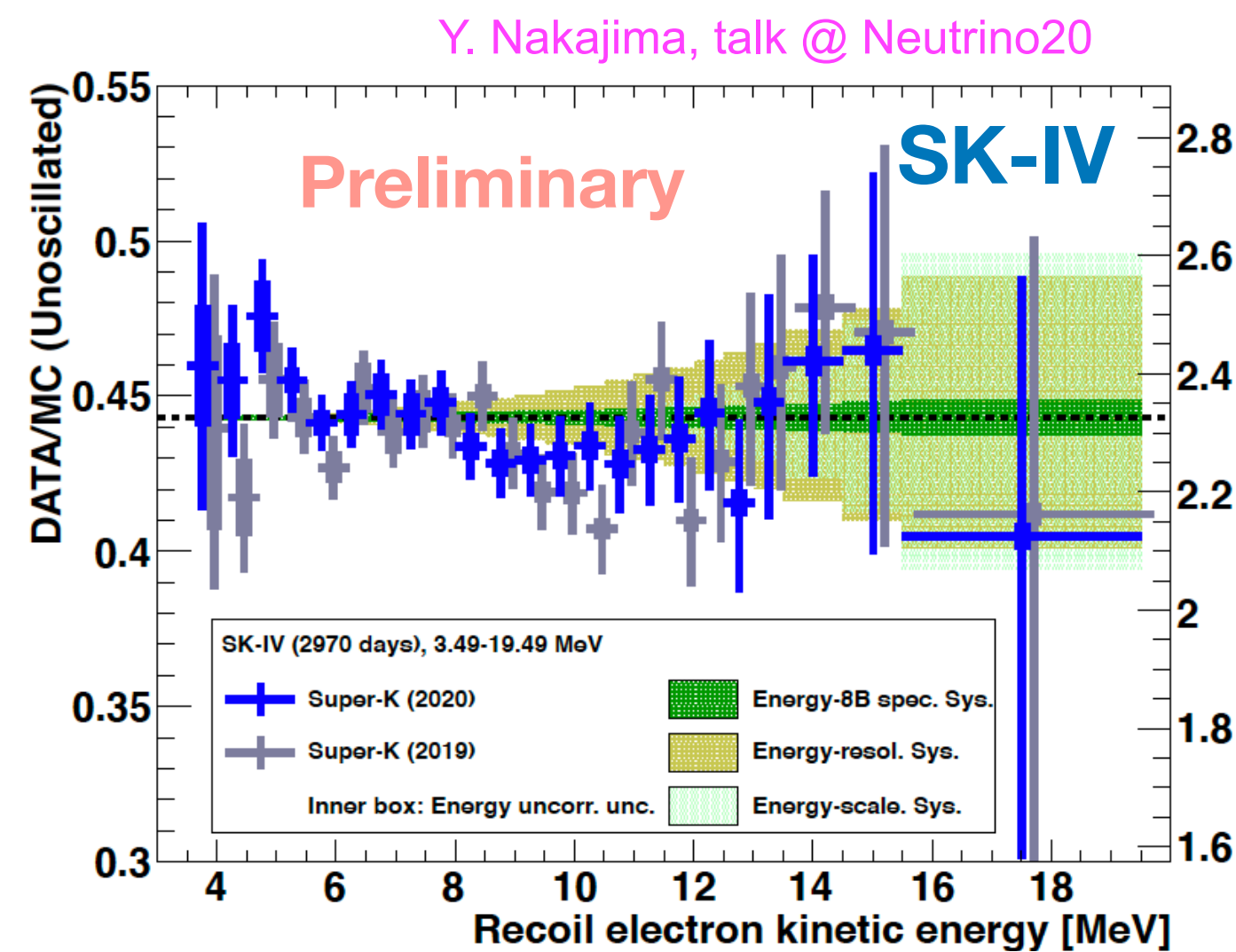
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today's result from Daya Bay $\theta_{13} \rightarrow 8.7 \%$



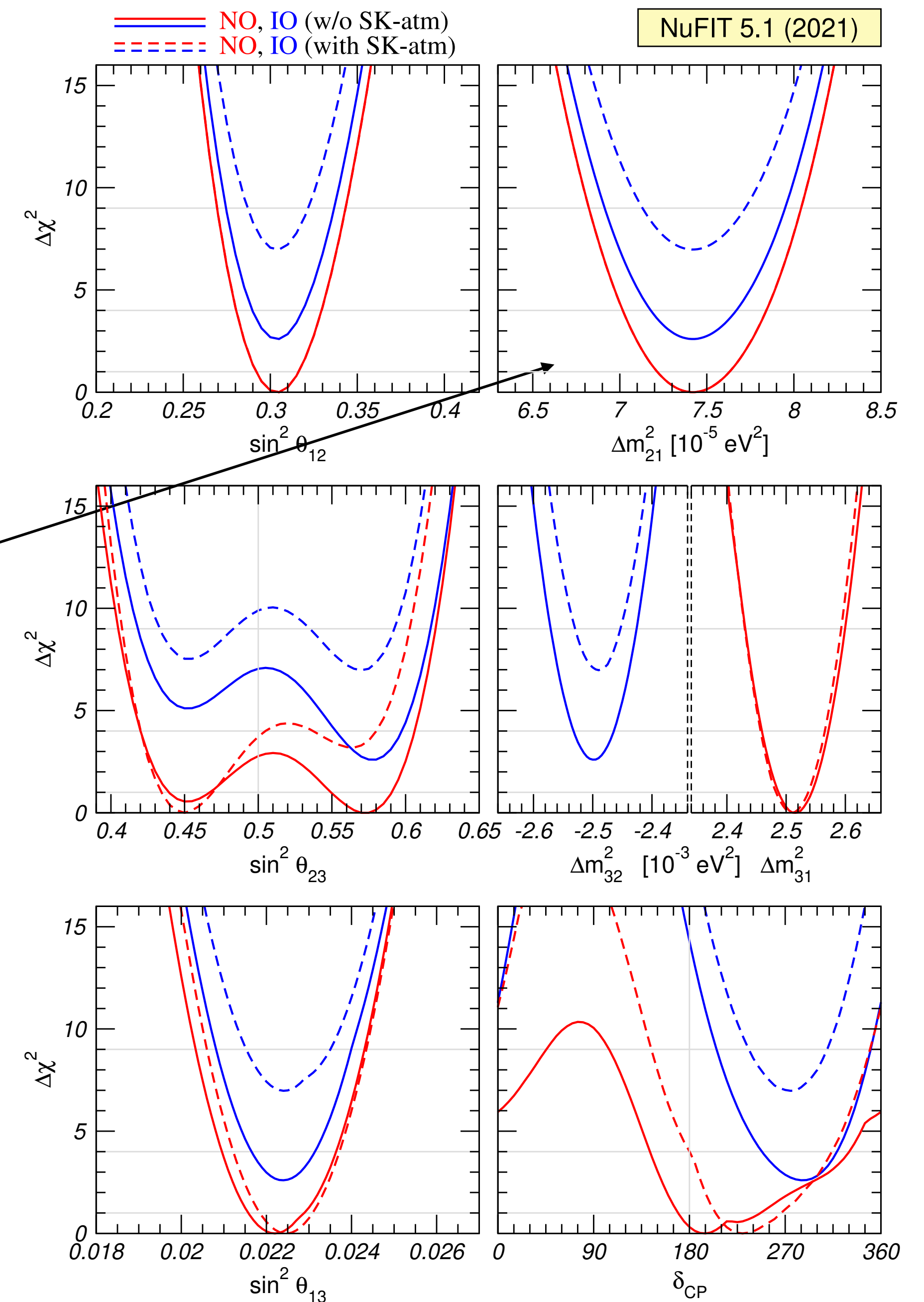
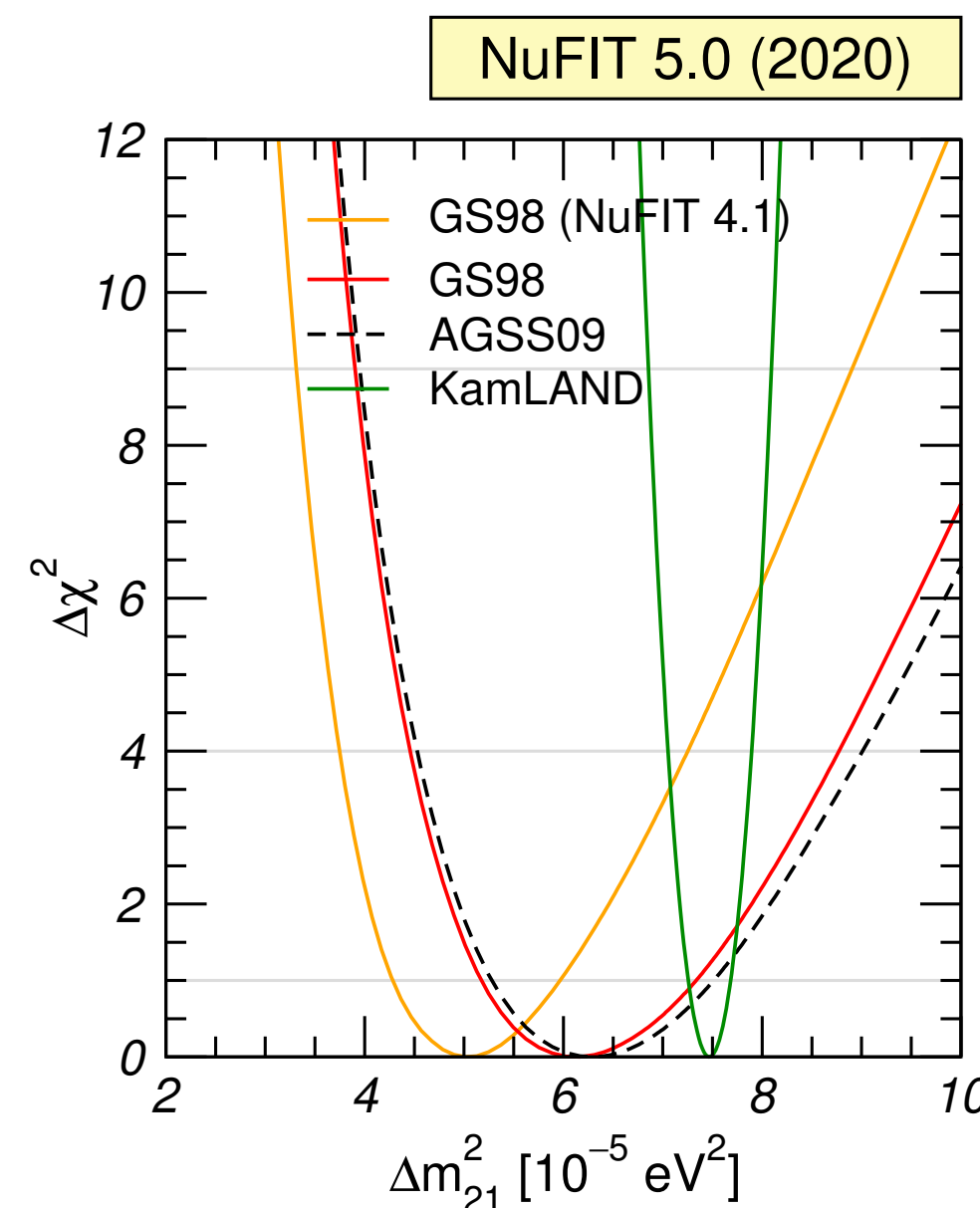
Four well-known parameters

- long-standing tension (2σ) between solar and KamL data resolved by latest SK-solar data



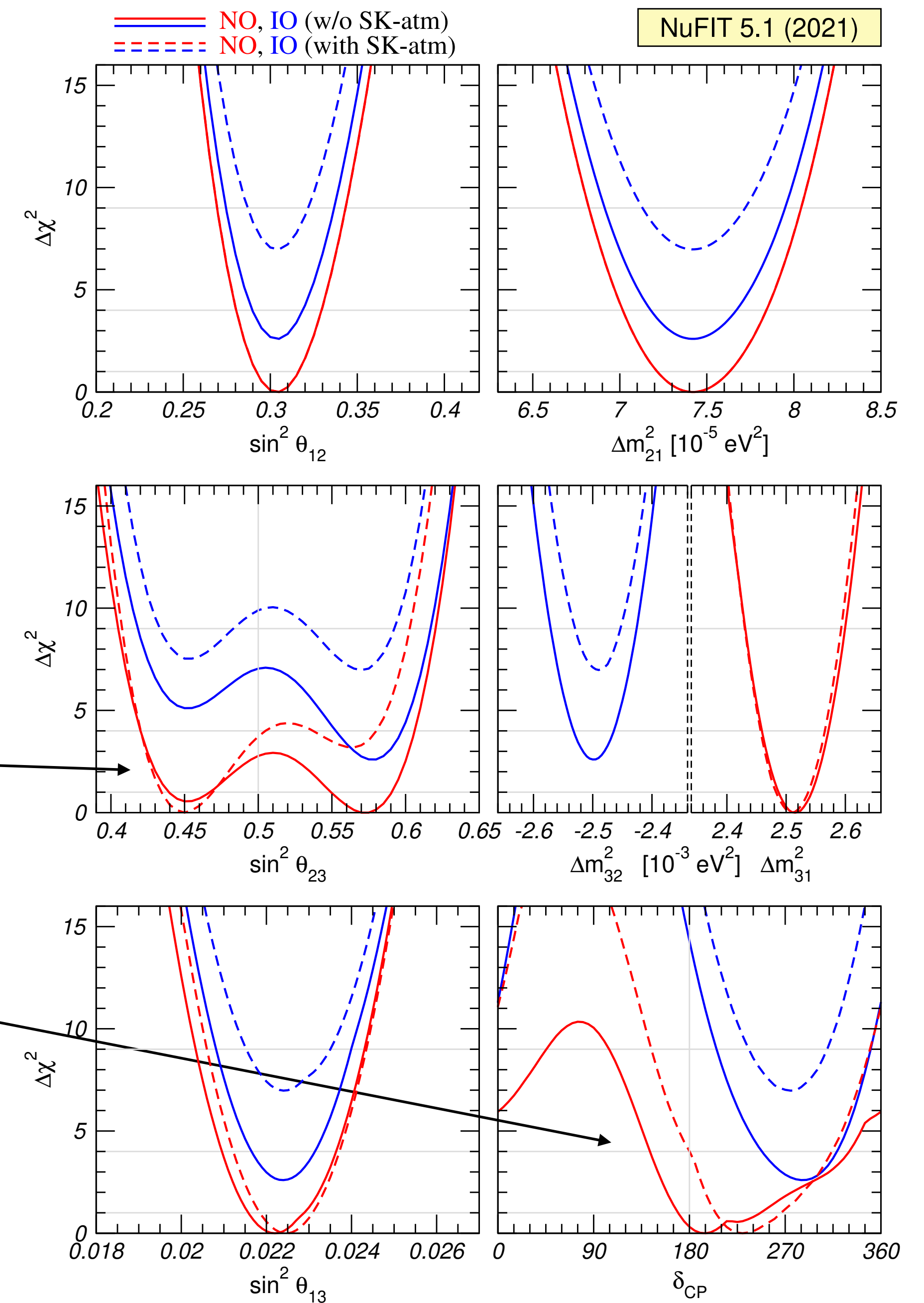
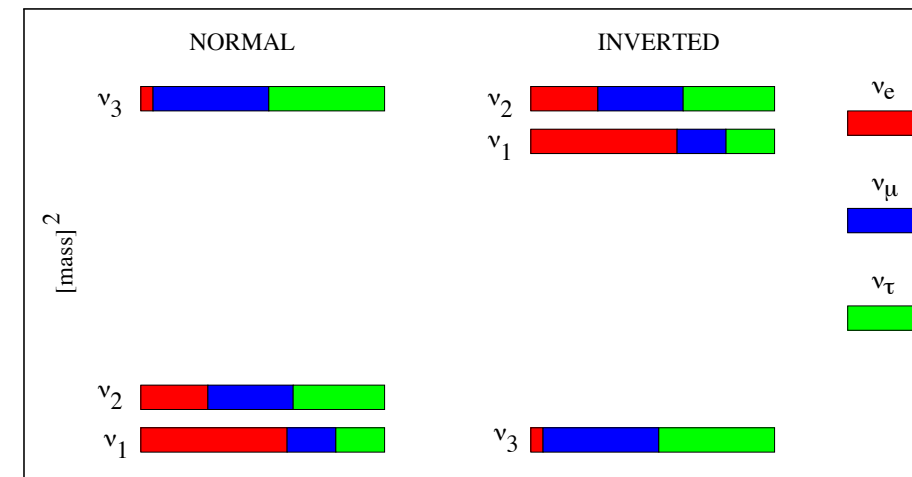
$$A_{DN}^{Fit} = (-3.6 \pm 1.6(stat) \pm 0.6(syst)) \% \rightarrow A_{DN}^{Fit} = (-2.1 \pm 1.1) \%$$

- solar neutrino and KamLAND data compatible at 1.1σ



The unknowns:

- neutrino mass ordering
(red vs blue curves)
- octant of θ_{23}
- status of leptonic CP violation

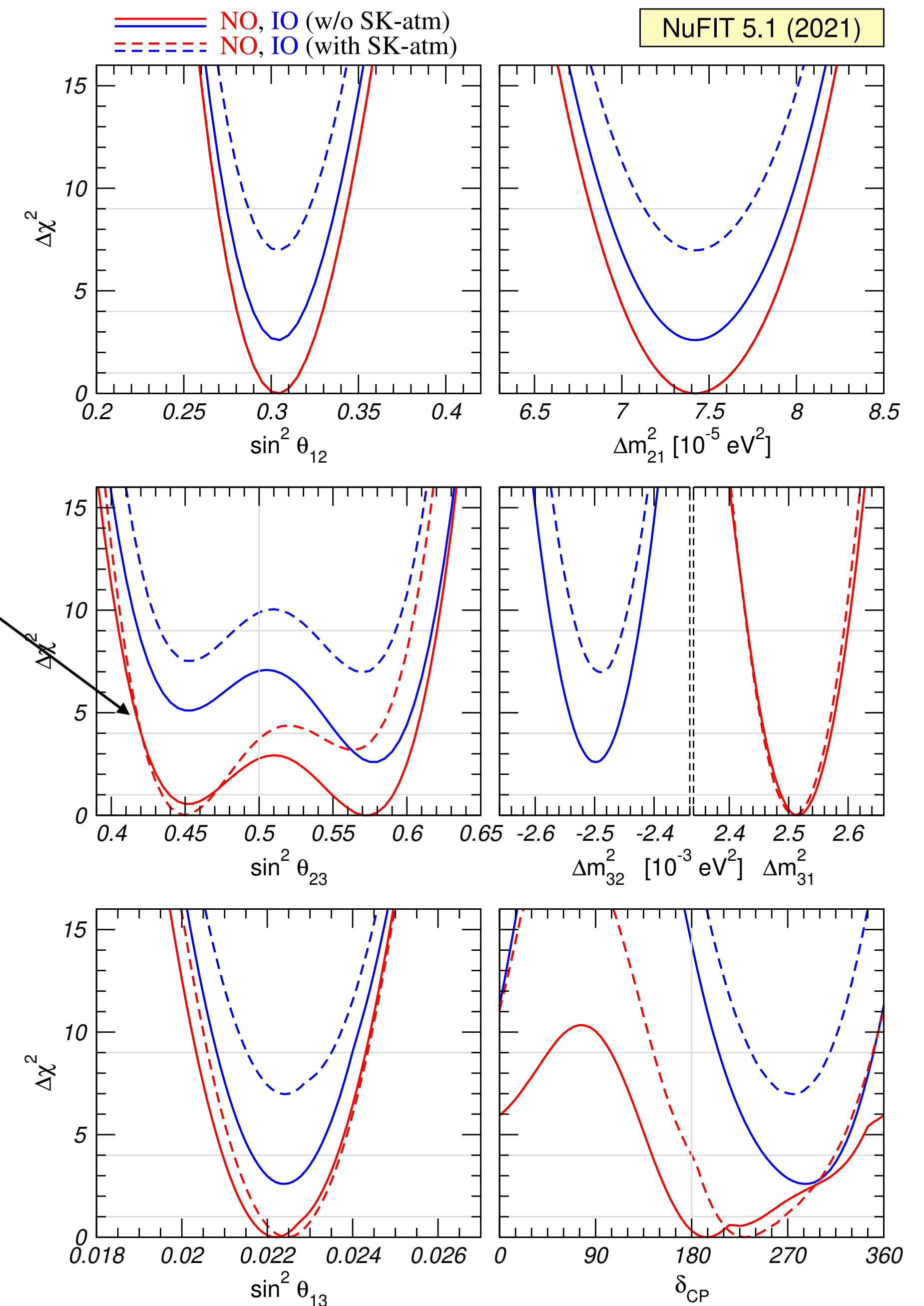


The least known mixing angle

NuFIT 5.1 results www.nu-fit.org

- broad allowed range for θ_{23} (24%)
for quarks: 5.2%

- ambiguity in the octant
- fragile with respect to atmospheric neutrino analysis and mass ordering

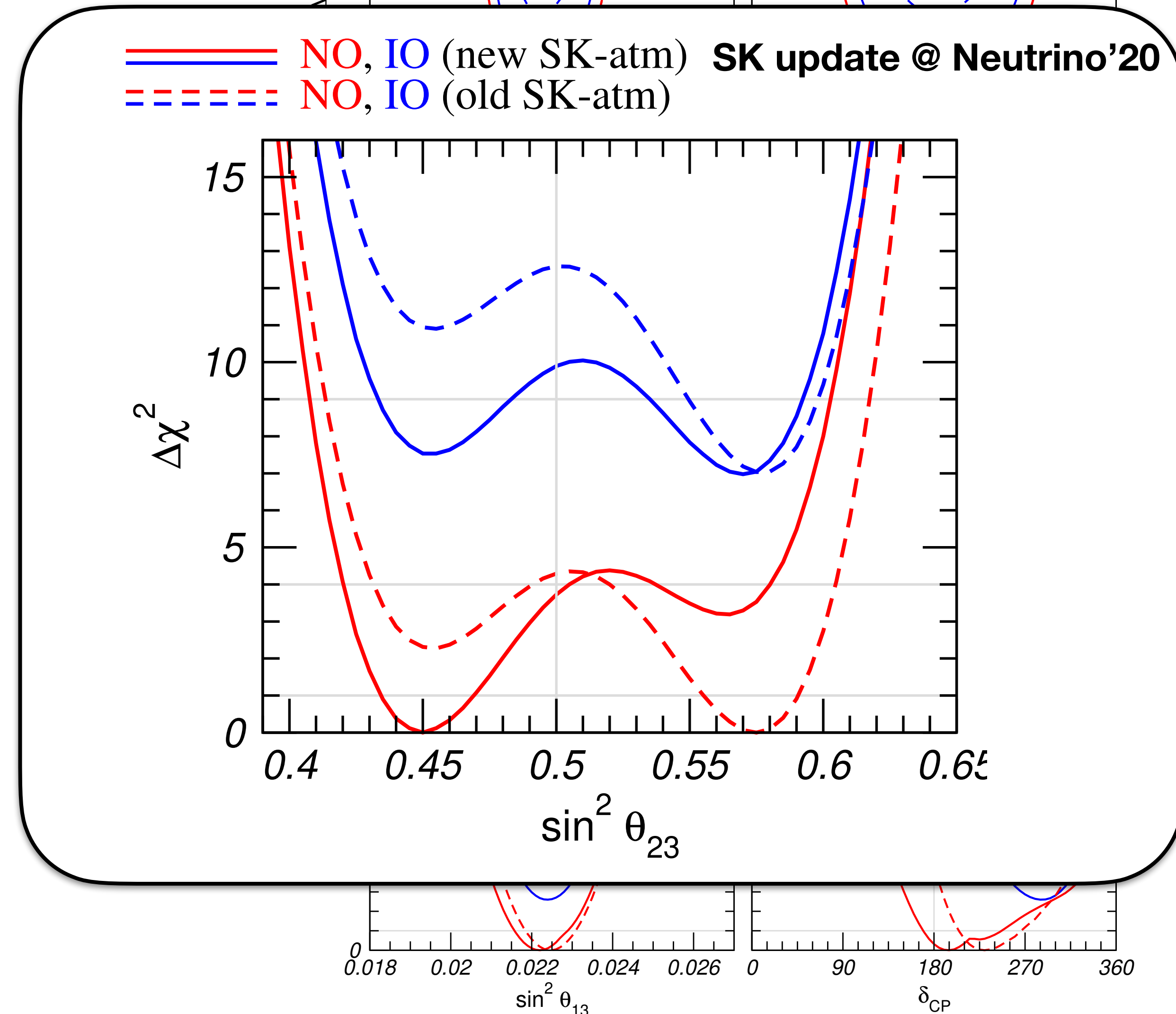


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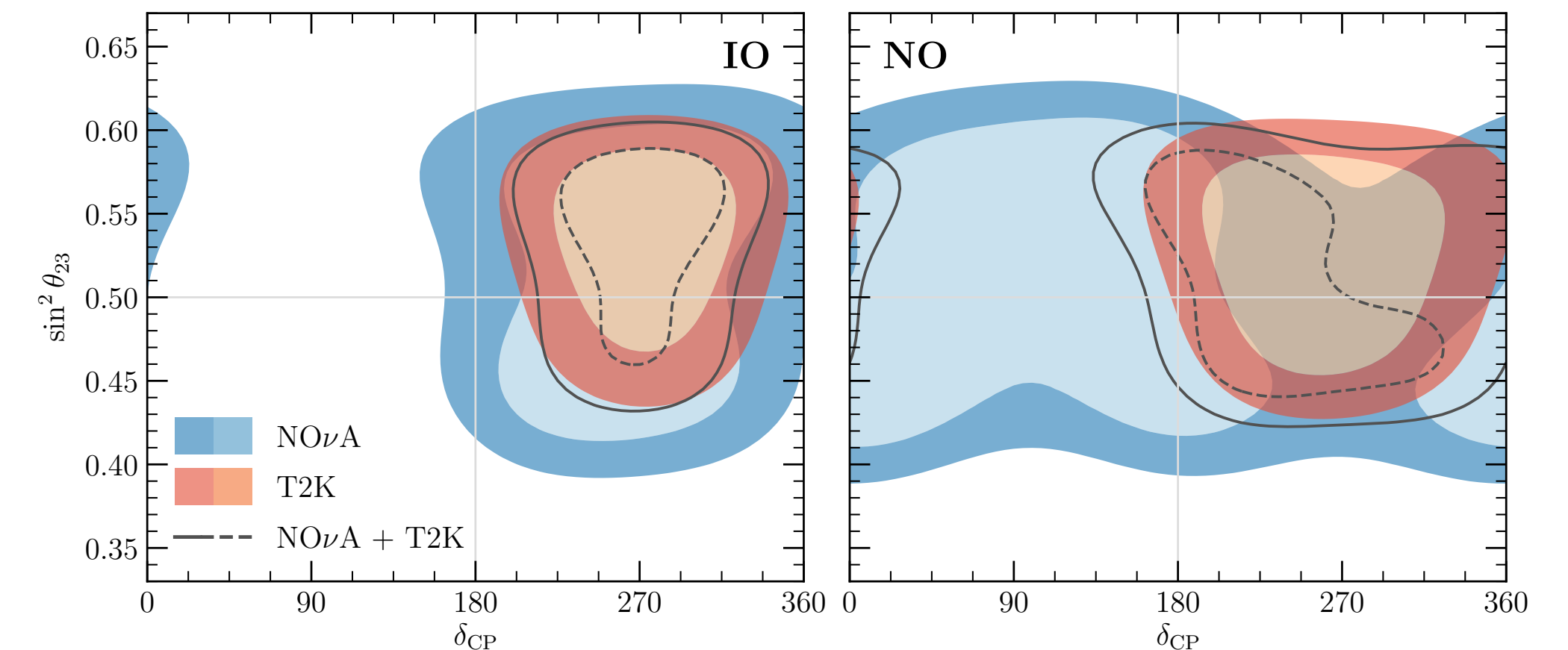
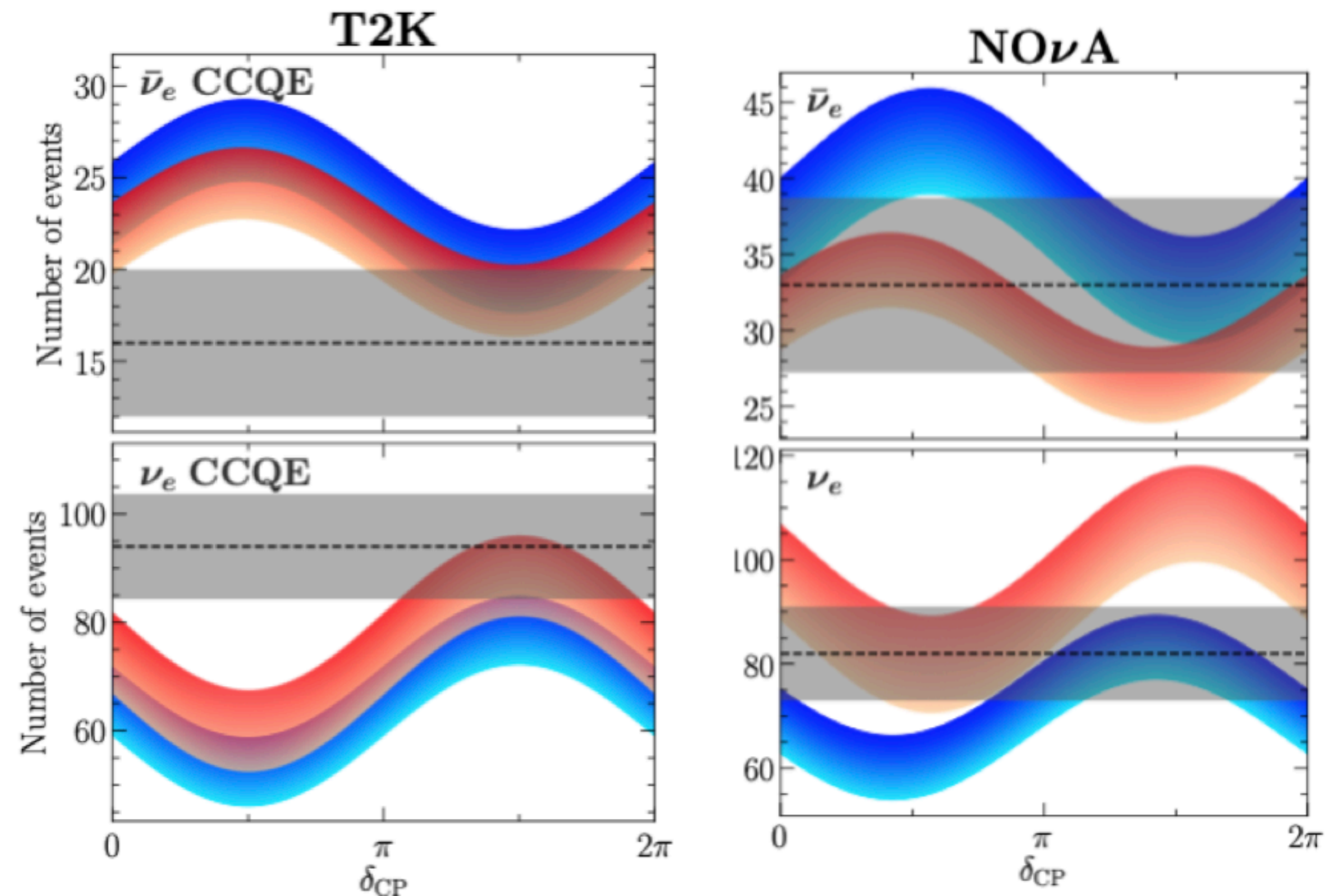
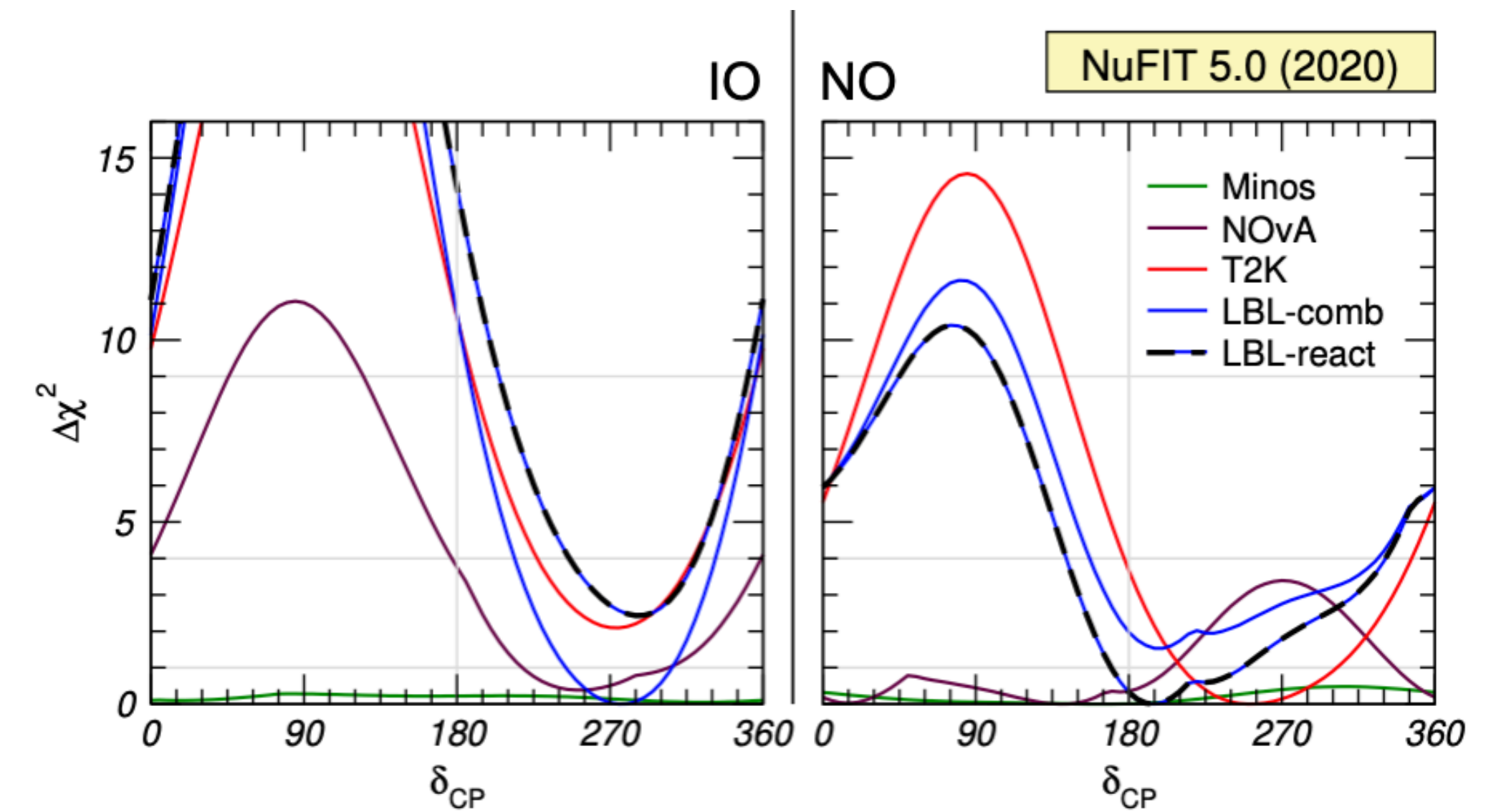
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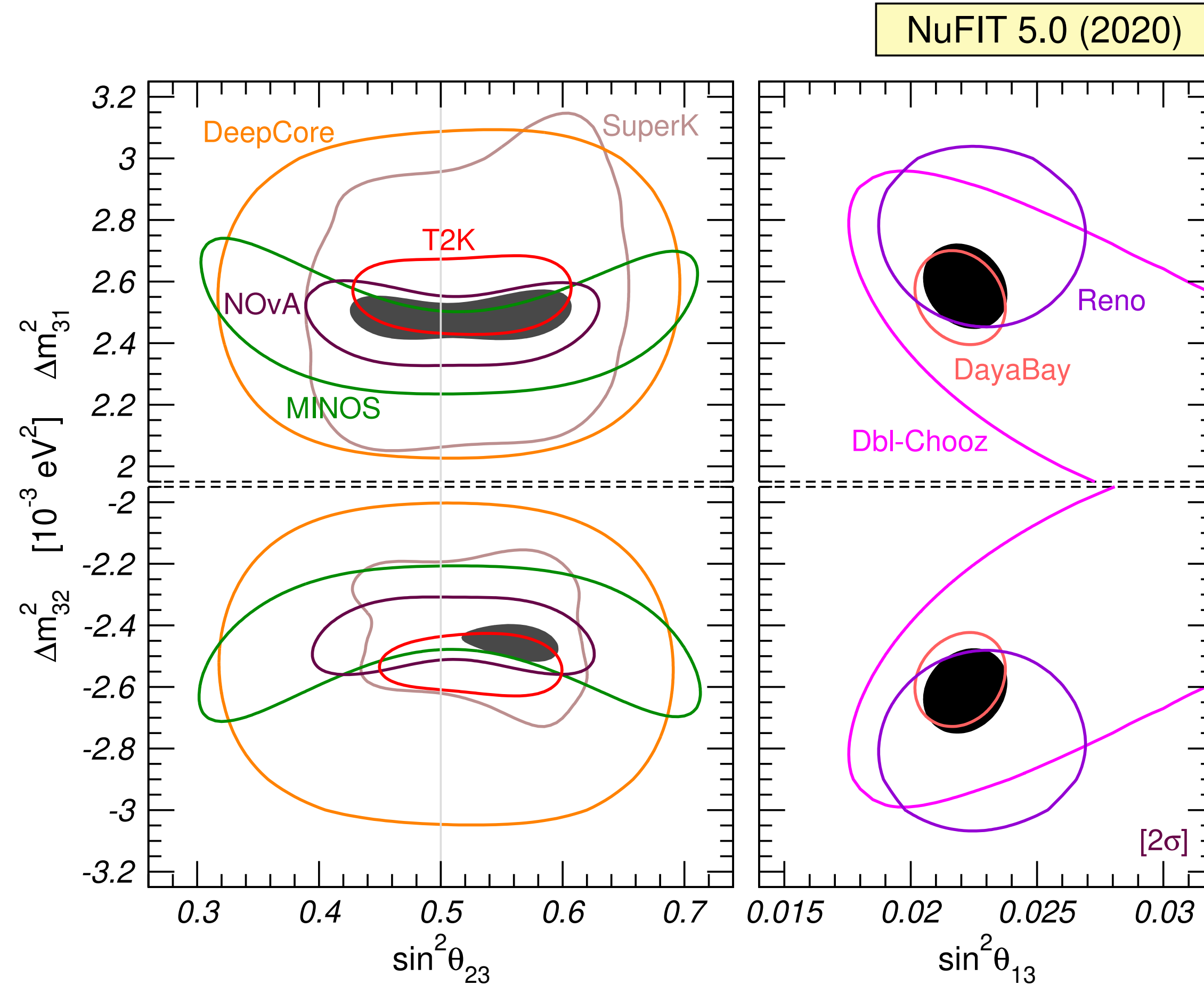


Mass ordering and CP phase

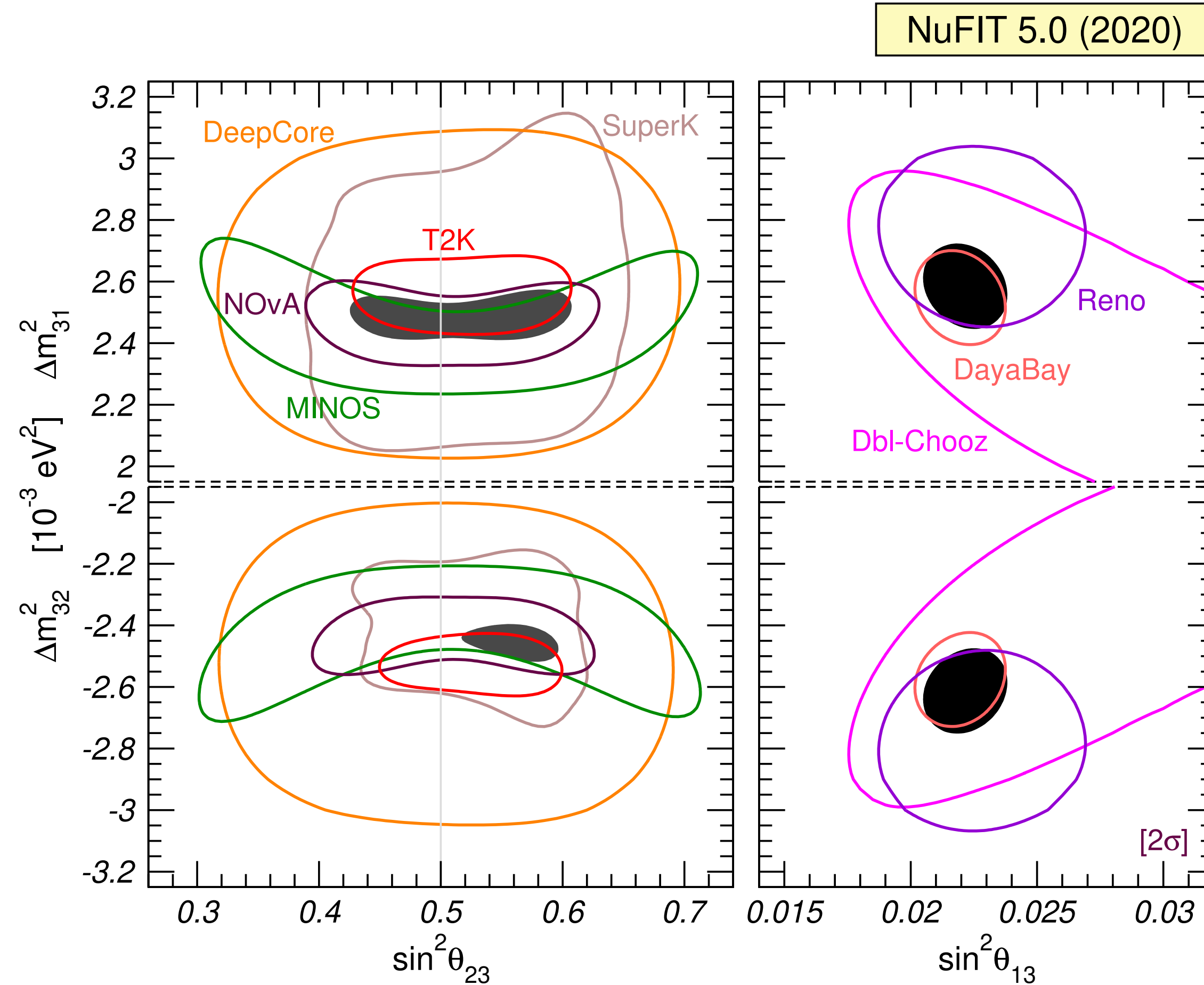
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 - LBL accelerator data: T2K & NOvA better compatible for IO



Consistency of μ and e disappearance



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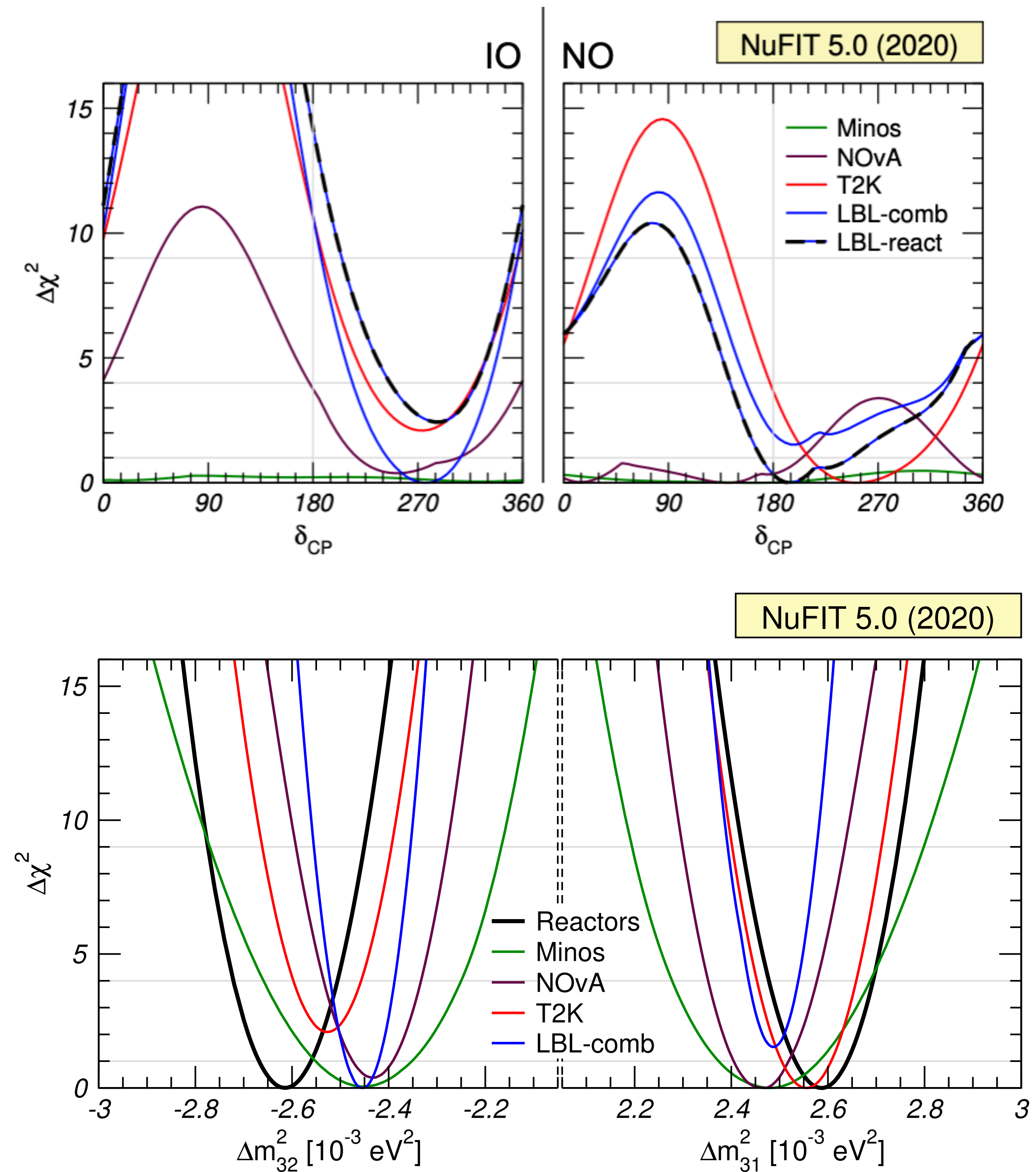


$$|\Delta m_{\mu\mu}^2| = |\Delta m_{ee}^2| \mp \Delta m_{21}^2 [\cos 2\theta_{12} - \cos \delta \sin \theta_{13} \sin 2\theta_{12} \tan \theta_{23}]$$

slightly different *effective* mass-squared differences: -/+ for NO/IO [Nunokawa, Parke, Zukanovich, 05](#)

Mass ordering and CP phase

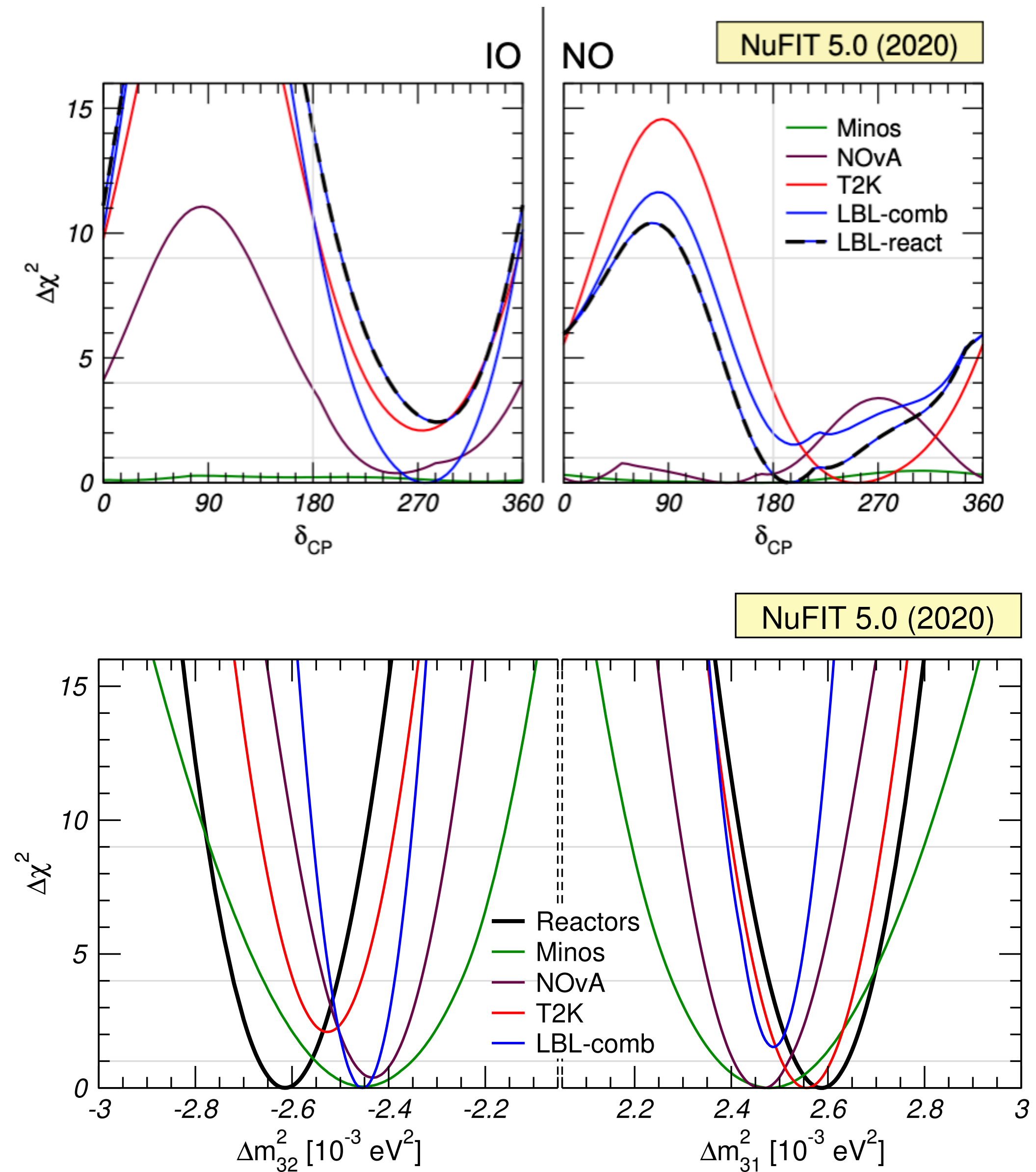
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T2K & NOvA better compatible for IO
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better agreement of $|\Delta m_{31}^2|$ for NO
- overall preference for NO with $\Delta\chi^2 = 2.7$ (was 6.2 in 2019)



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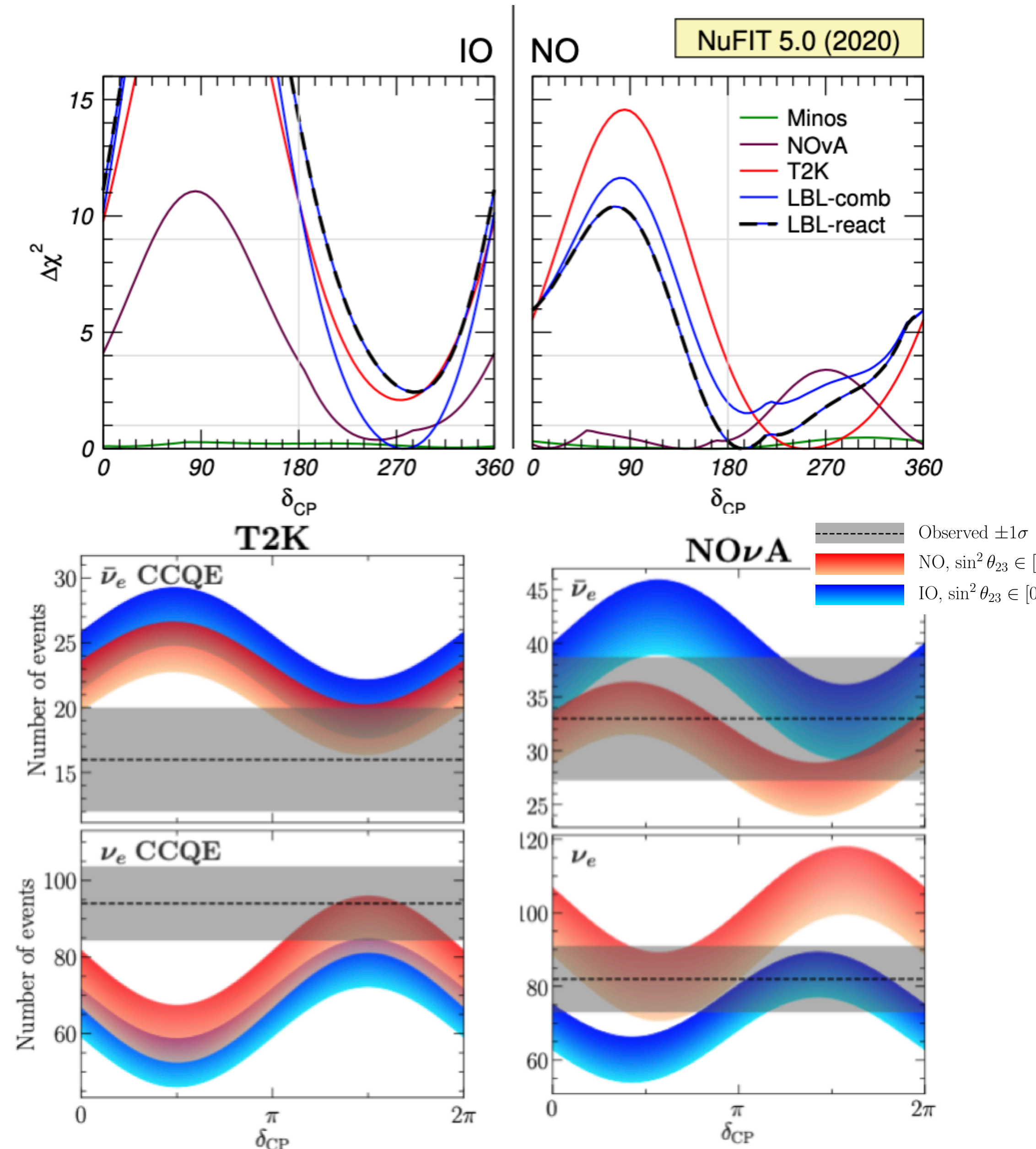
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very power full in the future [Blennow, TS, 2013]
combining reactor data from **JUNO** with
atmospheric data from **IceCube** [1911.06745] or
KM3NET/ORCA [2108.06293]



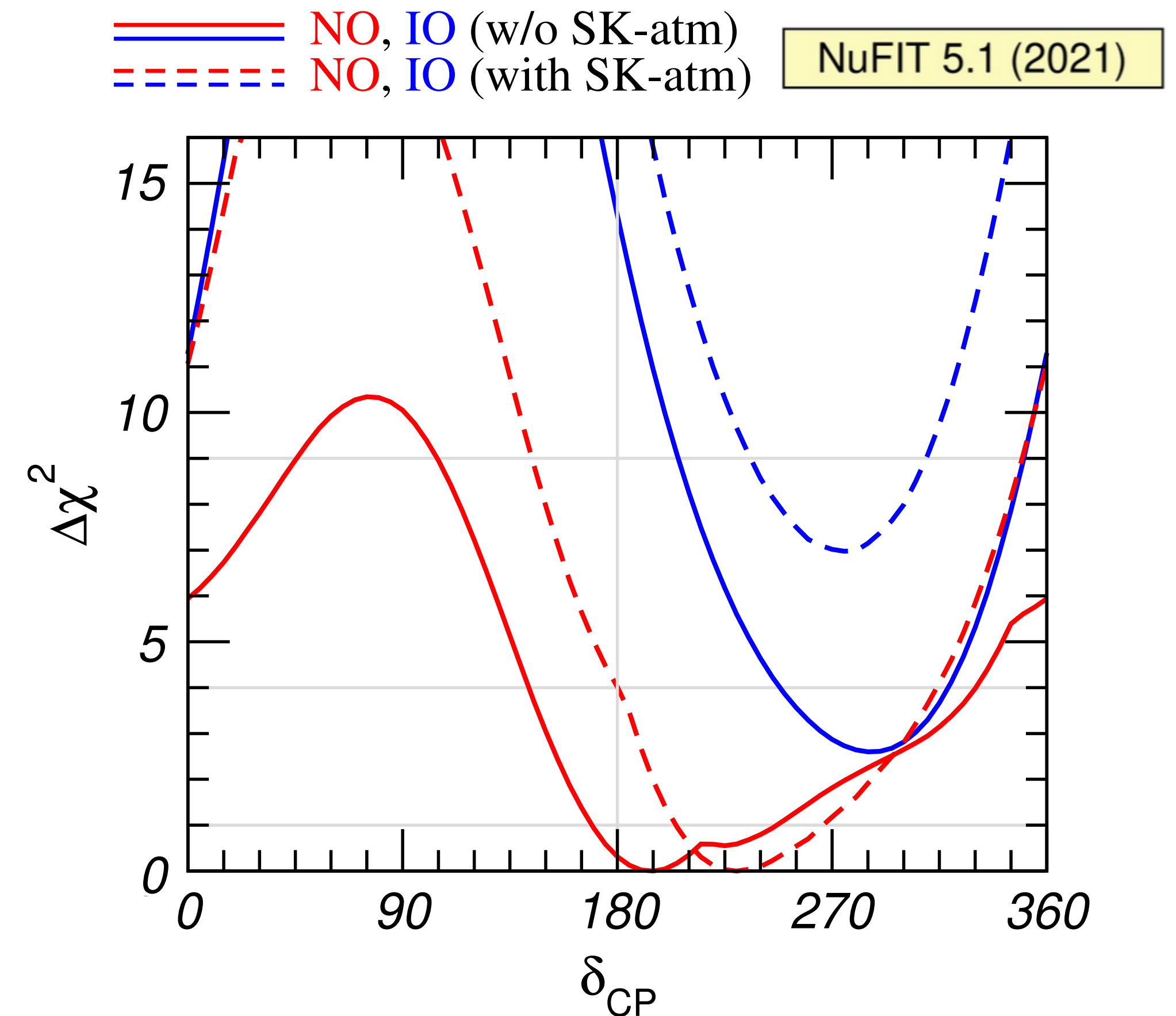
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better agreement of $|\Delta m_{31}^2|$ for NO
- overall preference for NO with $\Delta\chi^2 = 2.7$ (was 6.2 in 2019)
- CP phase best fit at $\delta=195^\circ \rightarrow$ CP conservation allowed at 0.6σ
- for IO: best fit close to $\delta=270^\circ$, CP conservation disfavoured at 3σ



Mass ordering and CP phase: atmospheric neutrinos

- NuFit 5.0 updated with SK I-IV analysis presented @ Neutrino'20
- improved sensitivity to MO:
 $\chi^2_{(\text{IO})} - \chi^2_{(\text{NO})} = 3.2$ (atm only)
pre-Neutrino'20: 4.3
- added to global fit via χ^2 table:
 $\chi^2_{(\text{IO})} - \chi^2_{(\text{NO})} = 2.7$ (no SK)
→ 7.1 (w SK) 2.7σ
- CP conservation @ 0.6σ (no SK)
→ 2σ (w SK)
best fit: $\delta_{\text{CP}} \approx 230^\circ$



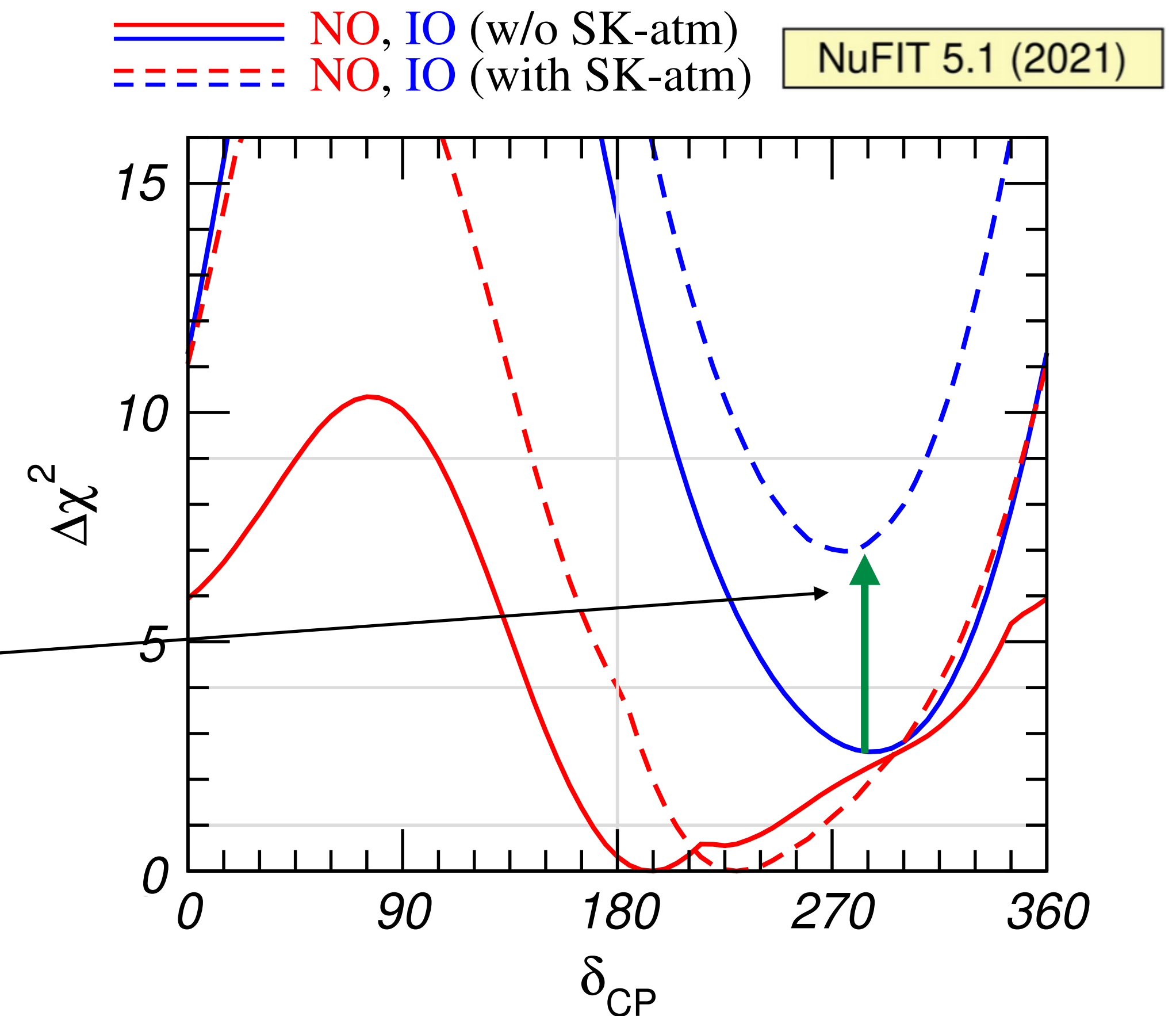
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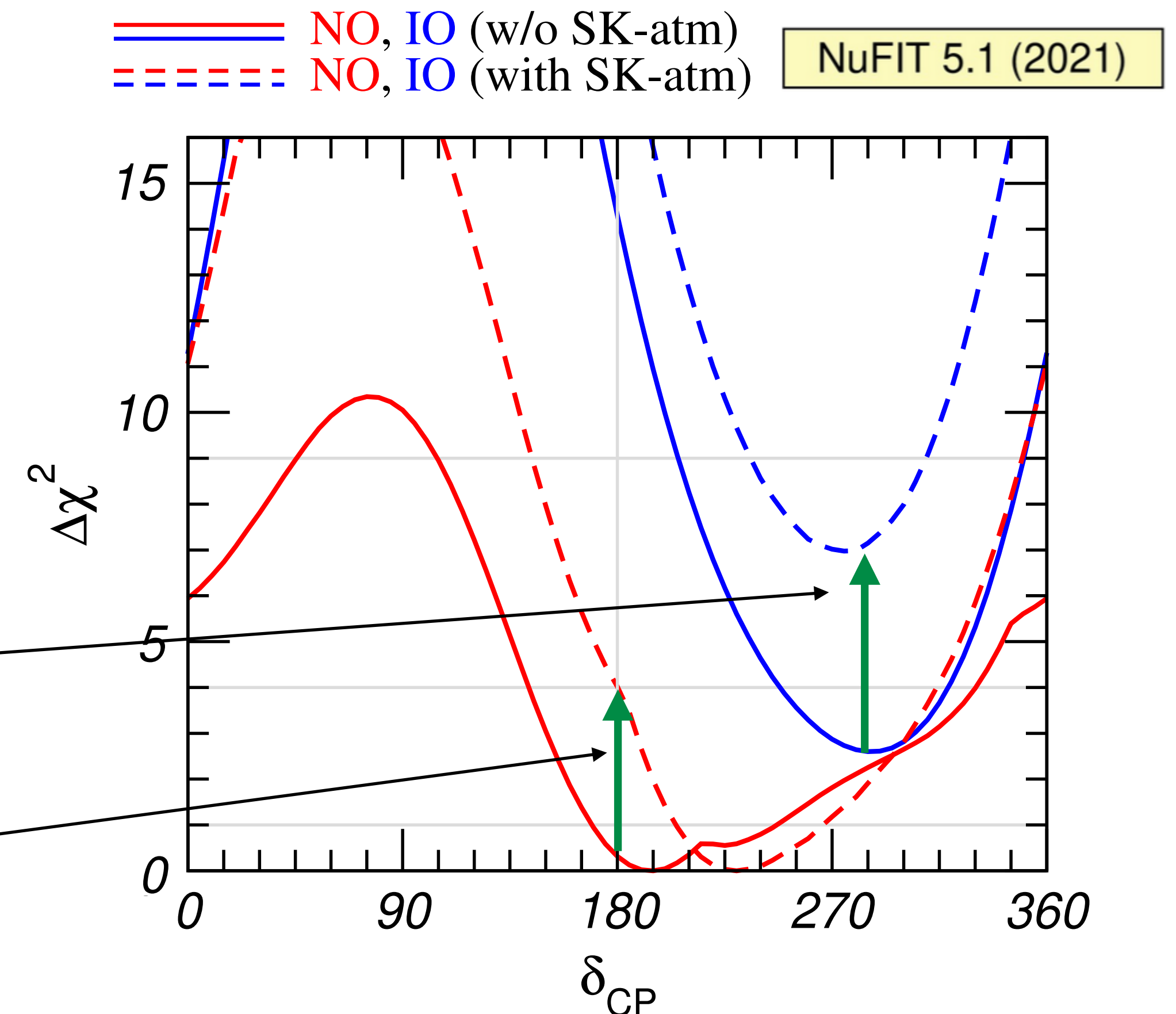
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Intermediate summary:

- results from **global 3-flavour oscillation fit**
 - robust determination of Δm_{21}^2 , $|\Delta m_{31}^2|$, θ_{12} , θ_{13}
 - determination of mass-ordering, θ_{23} -octant, CP phase depends on sub-leading three-flavour effects — not yet statistically significant
 - interplay of **accelerator / reactor / atmospheric data**

	best fit MO	$\Delta\chi^2(\text{MO})$	best fit δ_{CP}	$\Delta\chi^2(\text{CPC})$	oct. θ_{23}	$\Delta\chi^2(\text{oct.})$
accelerator	IO	1.5	275°	2.0	2nd	2.2
+ reactors	NO	2.7	195°	0.4	2nd	0.5
+ atmospheric	NO	7.1	230°	4.0	1st	3.2

Neutrino mass from cosmology

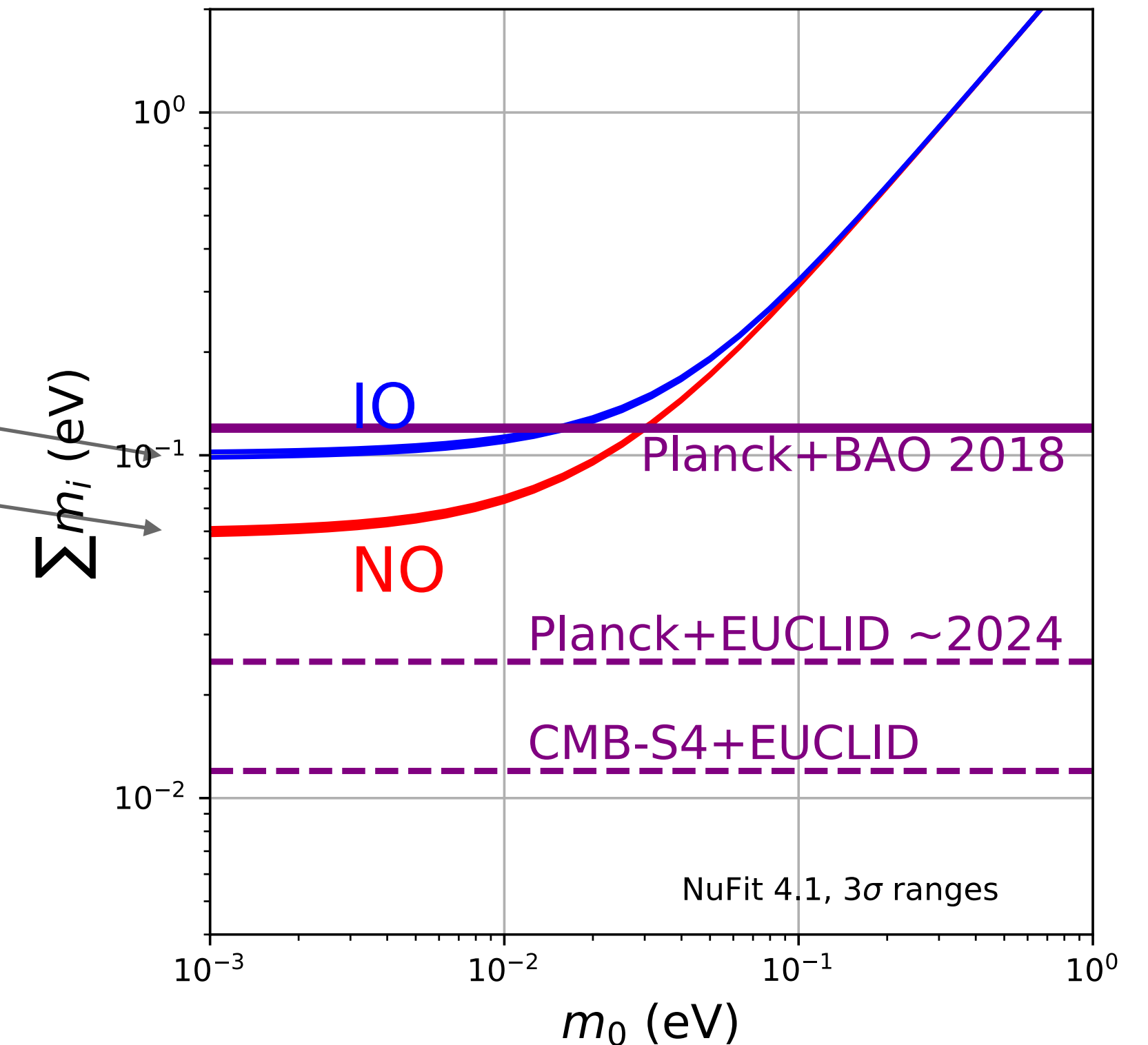
talks by J. Lesgourgues, O. Mena

$$\Sigma \equiv \sum_{i=1}^3 m_i = \begin{cases} m_0 + \sqrt{\Delta m_{21}^2 + m_0^2} + \sqrt{\Delta m_{31}^2 + m_0^2} & \text{(NO)} \\ m_0 + \sqrt{|\Delta m_{32}^2| + m_0^2} + \sqrt{|\Delta m_{32}^2| - \Delta m_{21}^2 + m_0^2} & \text{(IO)} \end{cases}$$

- minimal values predicted from oscillation data for $m_0 = 0$:

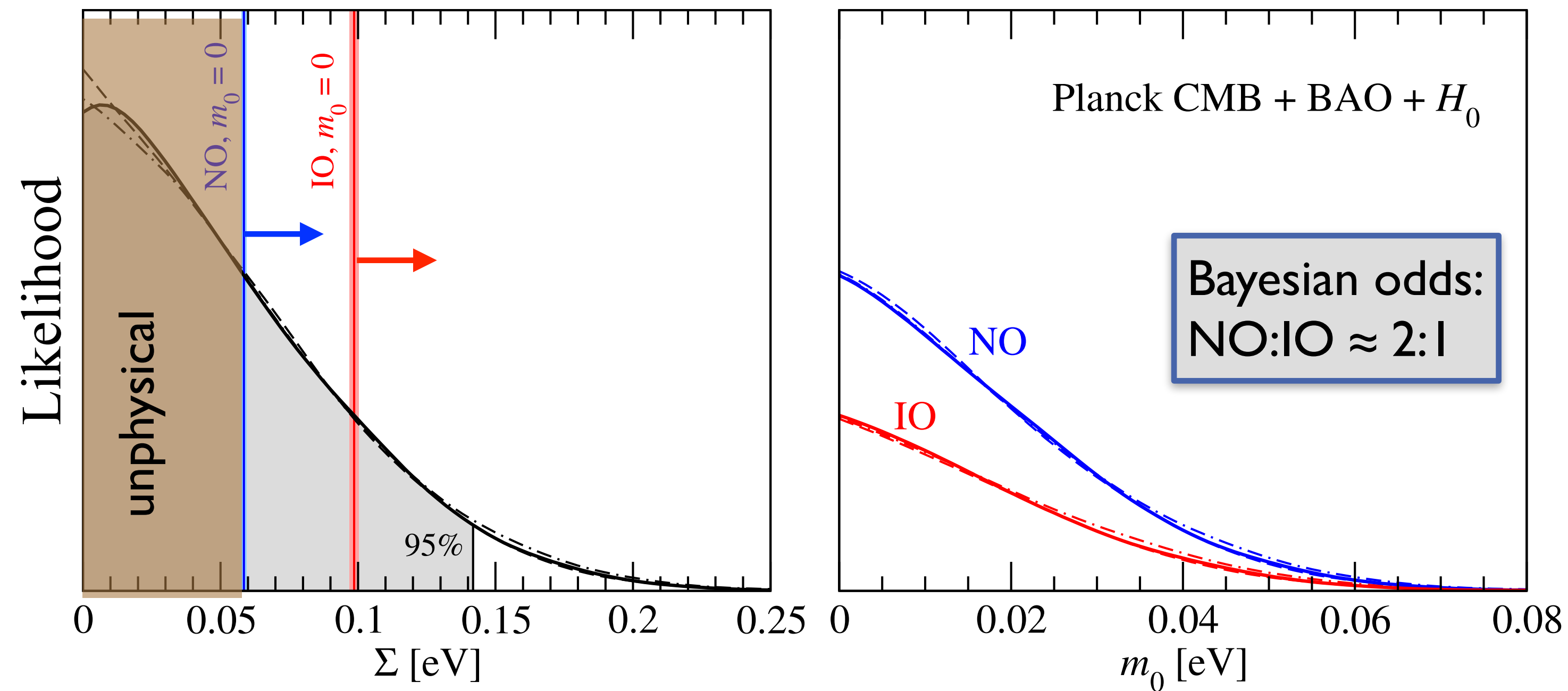
$$\Sigma_{\min} = \begin{cases} 98.6 \pm 0.85 \text{ meV} & \text{(IO)} \\ 58.5 \pm 0.48 \text{ meV} & \text{(NO)} \end{cases}$$

- **detection of non-zero neutrino mass expected soon!**
- **current limit close to IO minimum**



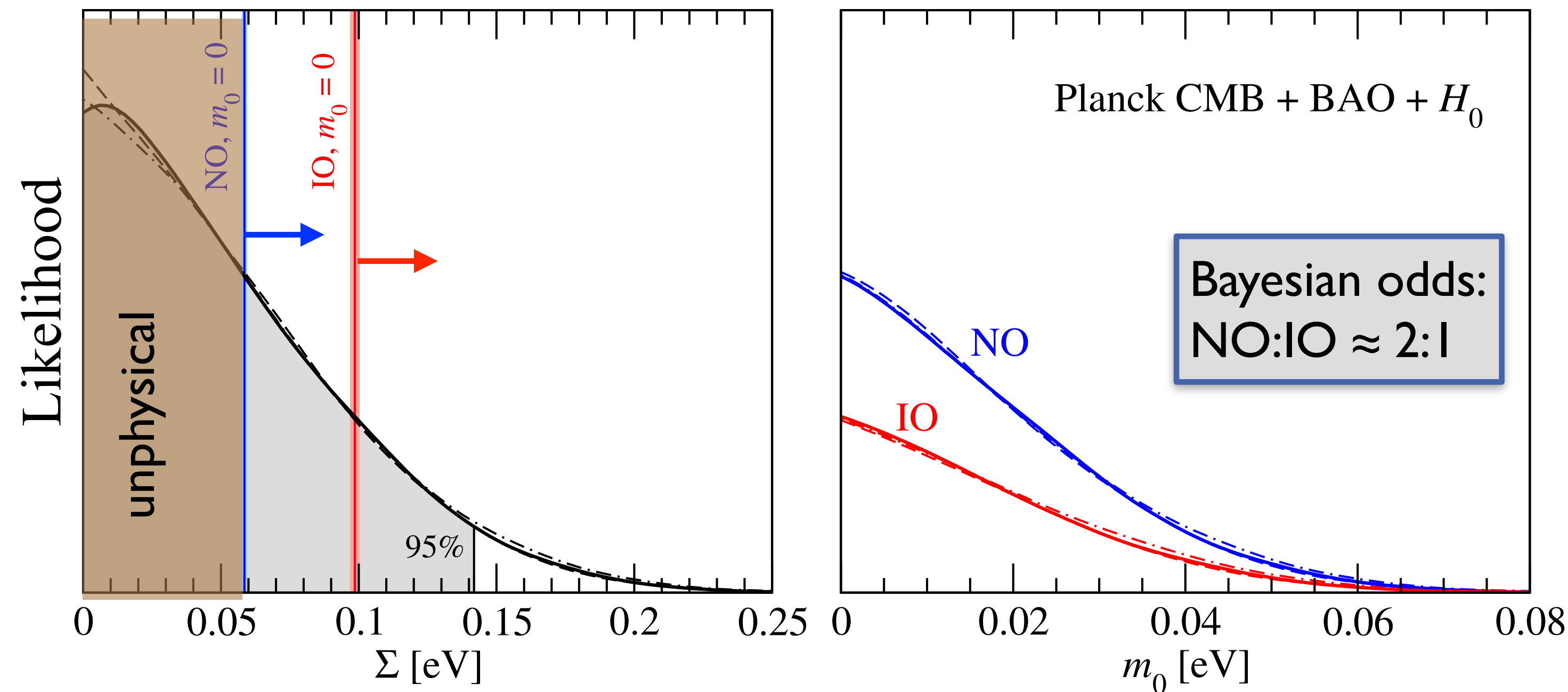
Excluding inverted ordering with cosmology?

Hannestad, Schwetz, [606.0469]



Excluding inverted ordering with cosmology?

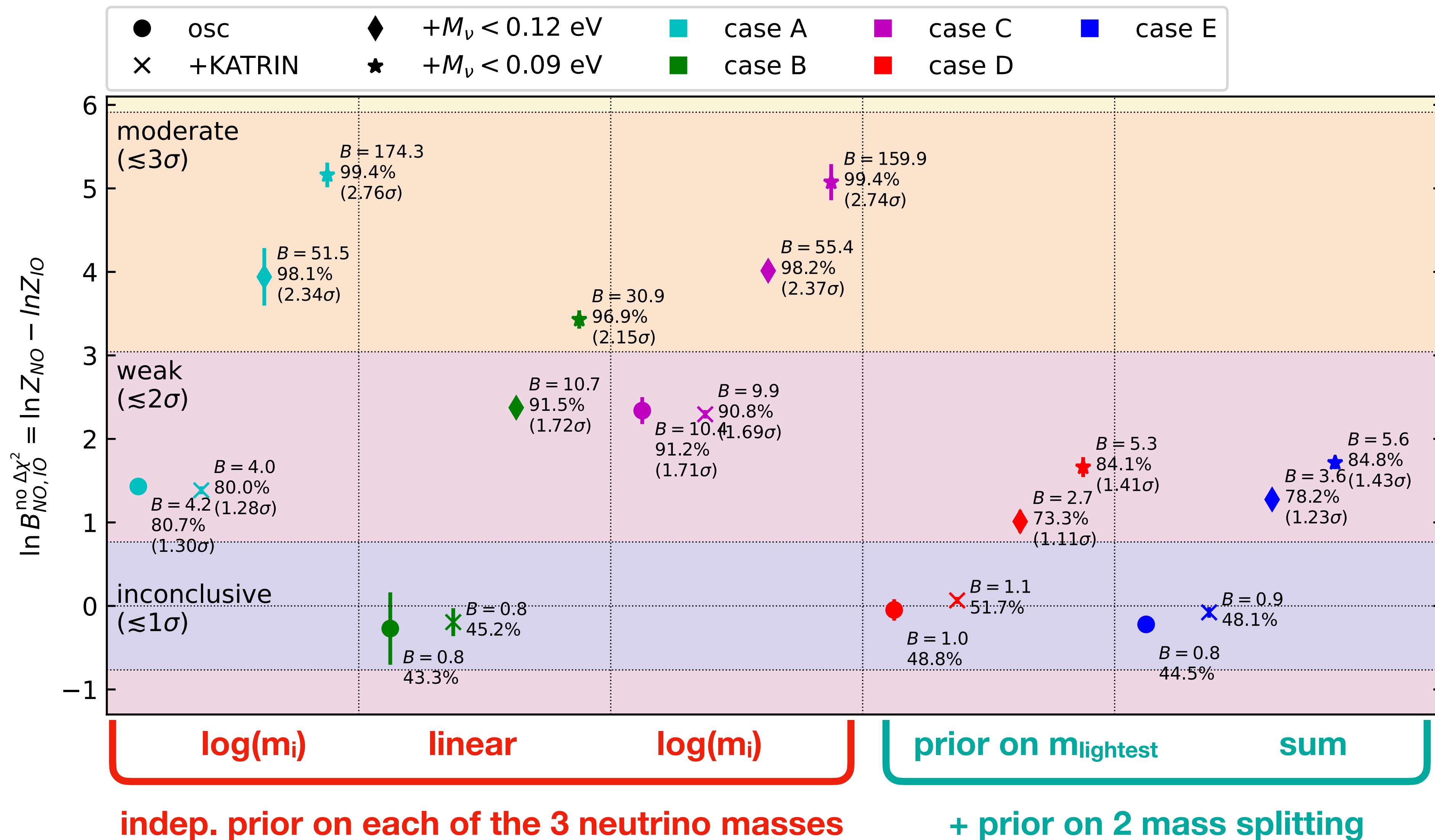
Hannestad, Schwetz, [1606.04691](#)



- **Strong Bayesian Evidence for the Normal Neutrino Hierarchy** [Simpson et al., 1703.03425](#); [Jimenez et al., 2203.14247](#)
- **No conclusive evidence for normal ordering:** [TS et al. 1703.04585](#); [Vagnozzi et al., 1701.08172](#); [Gariazzo et al., 1801.04946](#); [Heavens, Sellentin, 1802.09450](#); [deSalas et al., 1806.11051](#); [Mahony et al., 1907.04331](#); [Hannestad, Roy Choudhury, 1907.12598](#); [Gariazzo et al., 2205.02195](#)

Preference for normal ordering (w/o $\Delta\chi^2_{\text{IO/NO}}$ from oscillation)

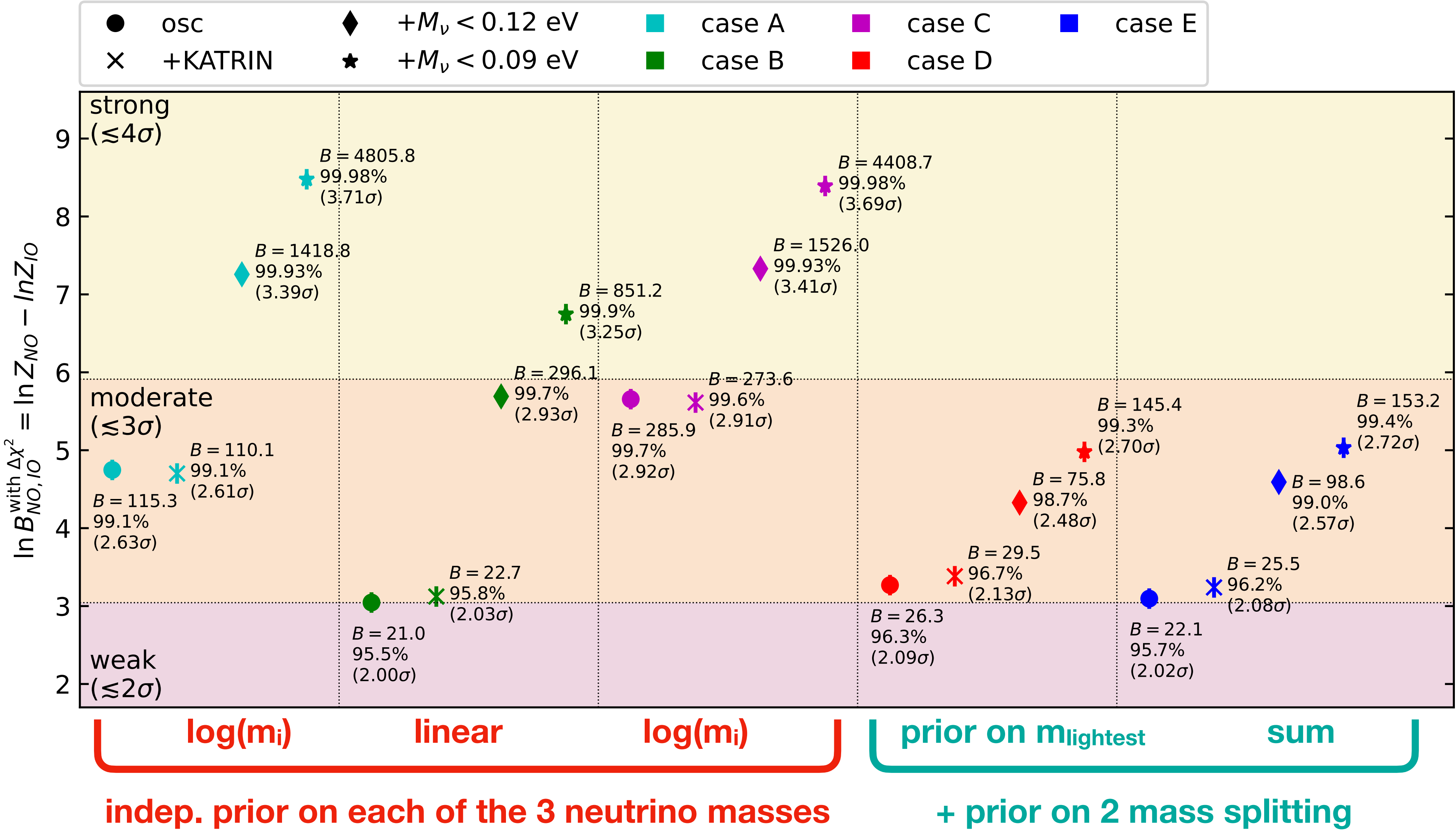
log Bayesian evidence ratio



Gariazzo et al., 2205.02195

Preference for normal ordering (including $\Delta\chi^2_{\text{IO/NO}}$ from oscillation)

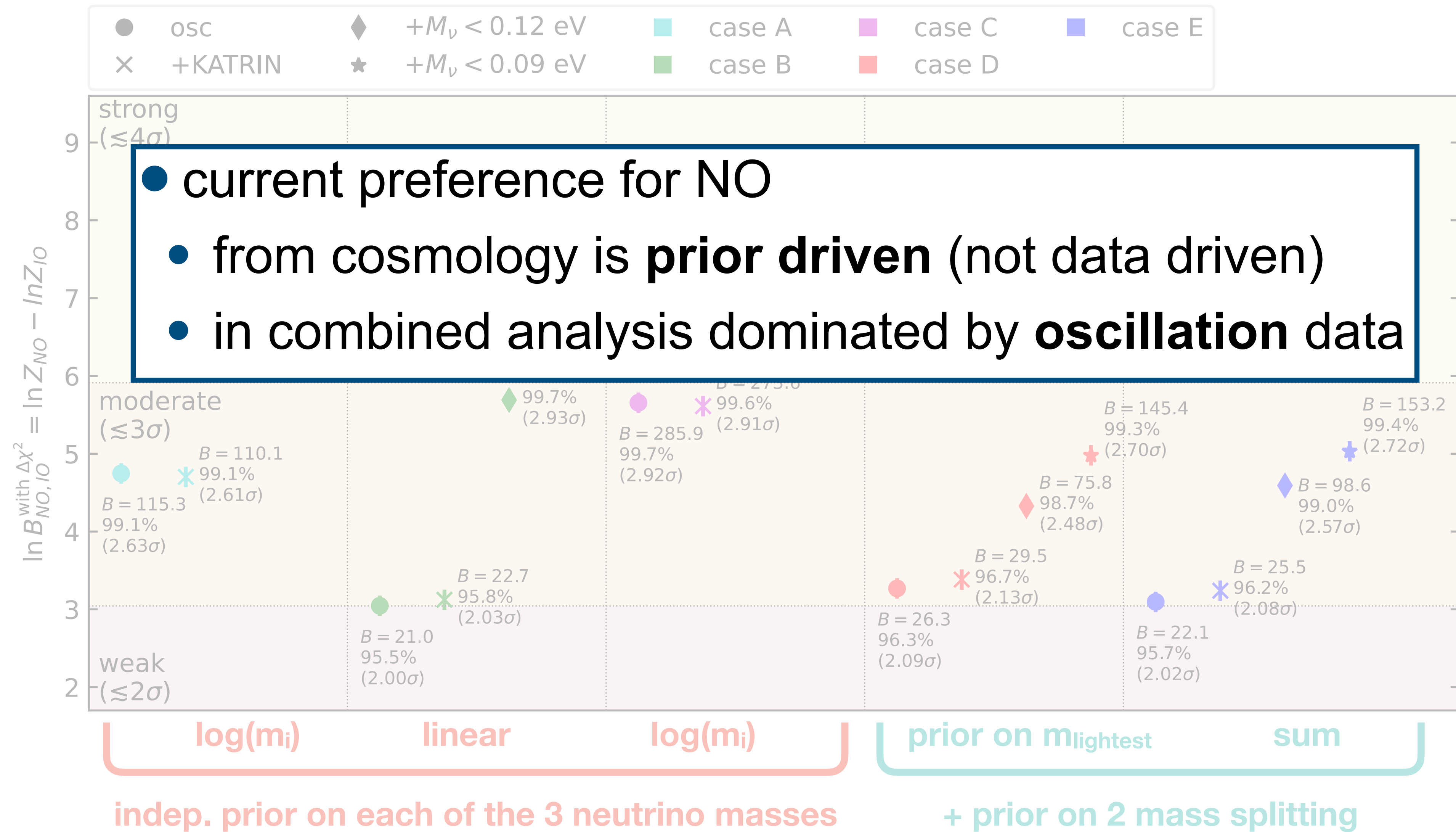
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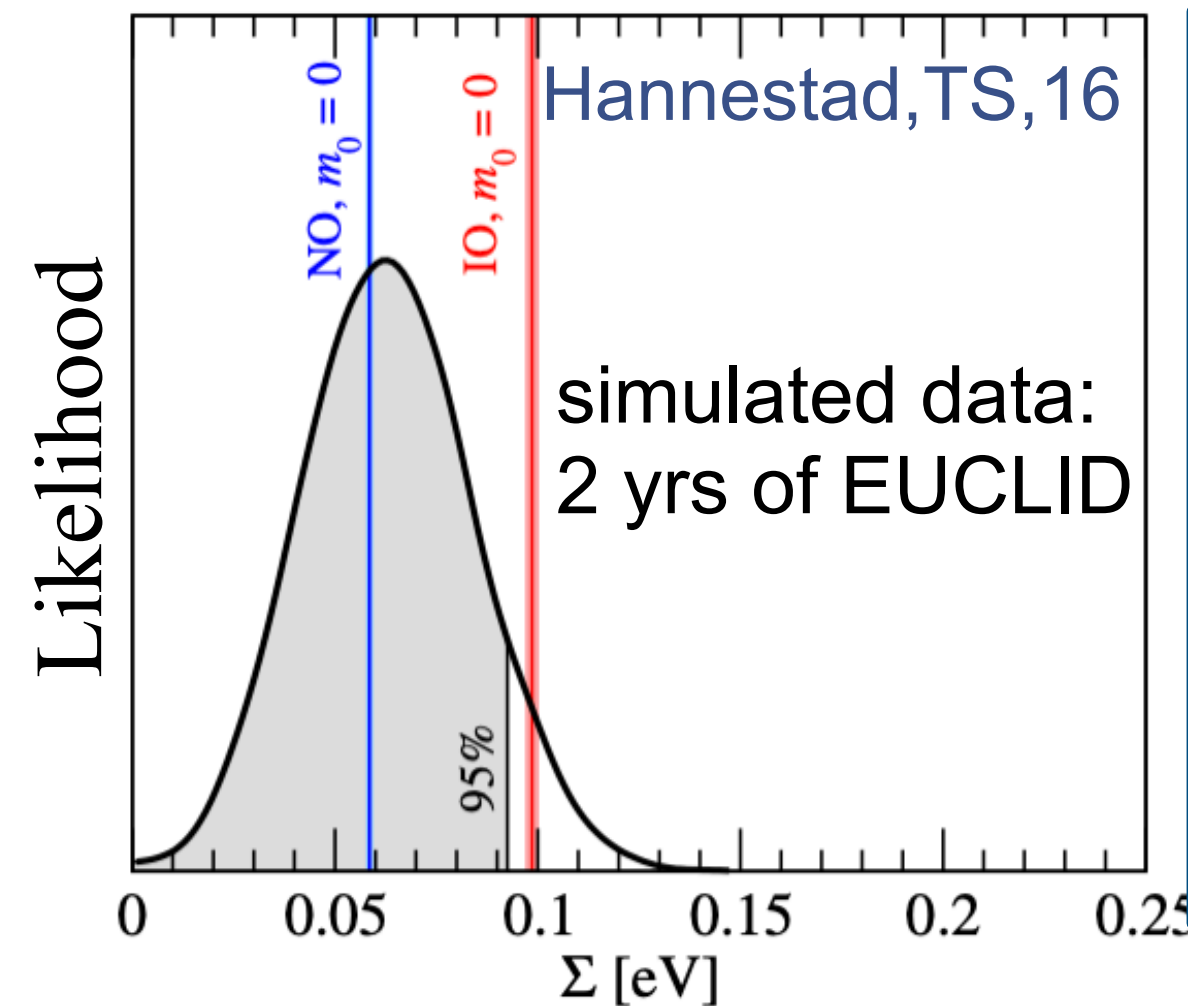
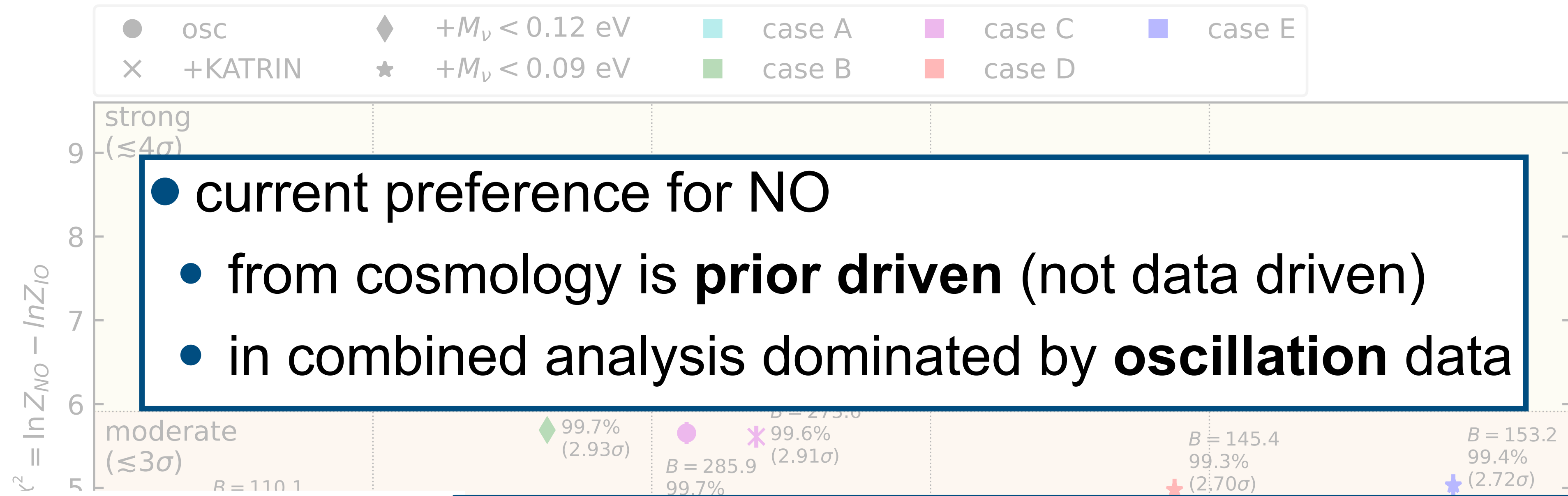


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Preference for normal ordering (including $\Delta\chi^2_{\text{IO/NO}}$ from oscillation)

log Bayesian evidence ratio

Gariazzo et al.,



But cosmology may become powerful in the future:

- need **accuracy better than 0.02 eV** to exclude 0.1 eV against 0.06 eV at 2σ
- this would imply a **3σ evidence for non-zero neutrino mass** (for $\Sigma = 0.06$ eV)

Comment on the search for CP violation

The „standard approach“ is highly model dependent:

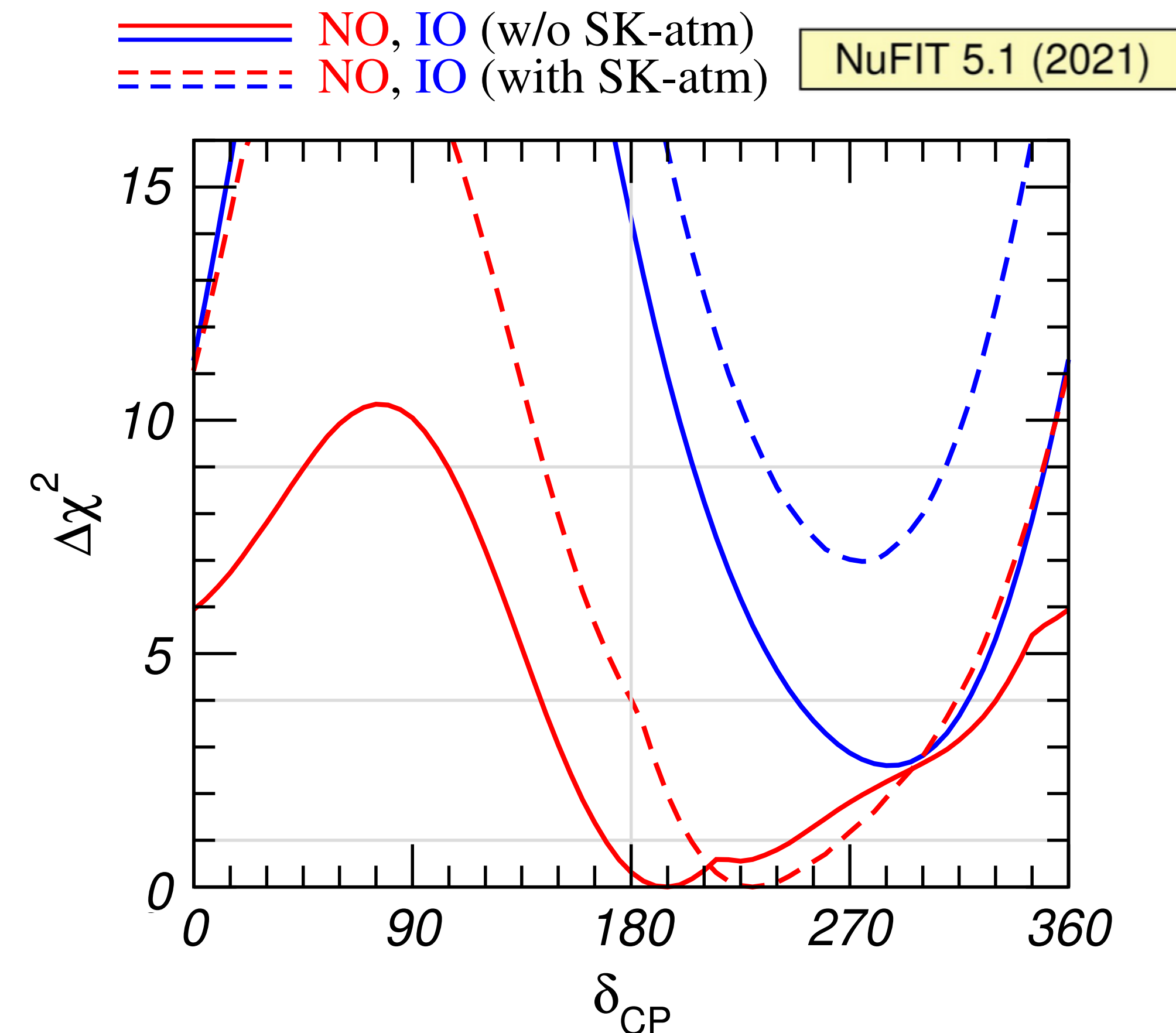
no model-indep. CPV observable \rightarrow assume:

- minimal three-flavour (unitary) scenario
- standard neutrino production and detection
- standard matter effect

talk by P. Denton

perform a parametric fit of combined accelerator/reactor data

- determine allowed range for δ_{CP}
- CPV \Leftrightarrow excluding values of 0 and π for δ_{CP}



Model-independent test of T-violation

with Alejandro Segarra:

Phys. Rev. Lett. **128** (2022) 091801 [arXiv:2106.16099]

Phys. Rev. D **105** (2022) 055001 [arXiv:2112.08801]

- measure oscillation probabilities at several distances but at the **same energy**
- search for a **T-odd component** of the oscillation probability
- works already with **3 experiments** but need to cover **1st and 2nd oscillation maxima**
- works without assuming unitarity, and allowing for non-standard physics in production, propagation, and detection
- insensitive to (std or non-std) matter effect (for symmetric density profile)

- general parameterisation of the transition probabilities:

$$P_{\mu\alpha} = \left| \sum_{i=1}^3 c_i^\alpha e^{-i\lambda_i L} \right|^2$$
$$= \sum_i |c_i^\alpha|^2 + 2 \sum_{j<i} \text{Re}(c_i^\alpha c_j^{\alpha*}) \cos(\omega_{ij} L) - 2 \sum_{j<i} \text{Im}(c_i^\alpha c_j^{\alpha*}) \sin(\omega_{ij} L)$$
$$c_i^\alpha \equiv (N_{\alpha i}^{\text{det}})^* N_{\mu i}^{\text{prod}}$$

Model-independent test of T-violation

A. Segarra, TS, 2106.16099

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T-even

$$= \sum_i |c_i^\alpha|^2 + 2 \sum_{j<i} \text{Re}(c_i^\alpha c_j^{\alpha*}) \cos(\omega_{ij} L) - 2 \sum_{j<i} \text{Im}(c_i^\alpha c_j^{\alpha*}) \sin(\omega_{ij} L)$$

T-odd

$$c_i^\alpha \equiv (N_{\alpha i}^{\text{det}})^* N_{\mu i}^{\text{prod}}$$

complex phases in c_i^α lead to T violation; more sources for TV due to new physics

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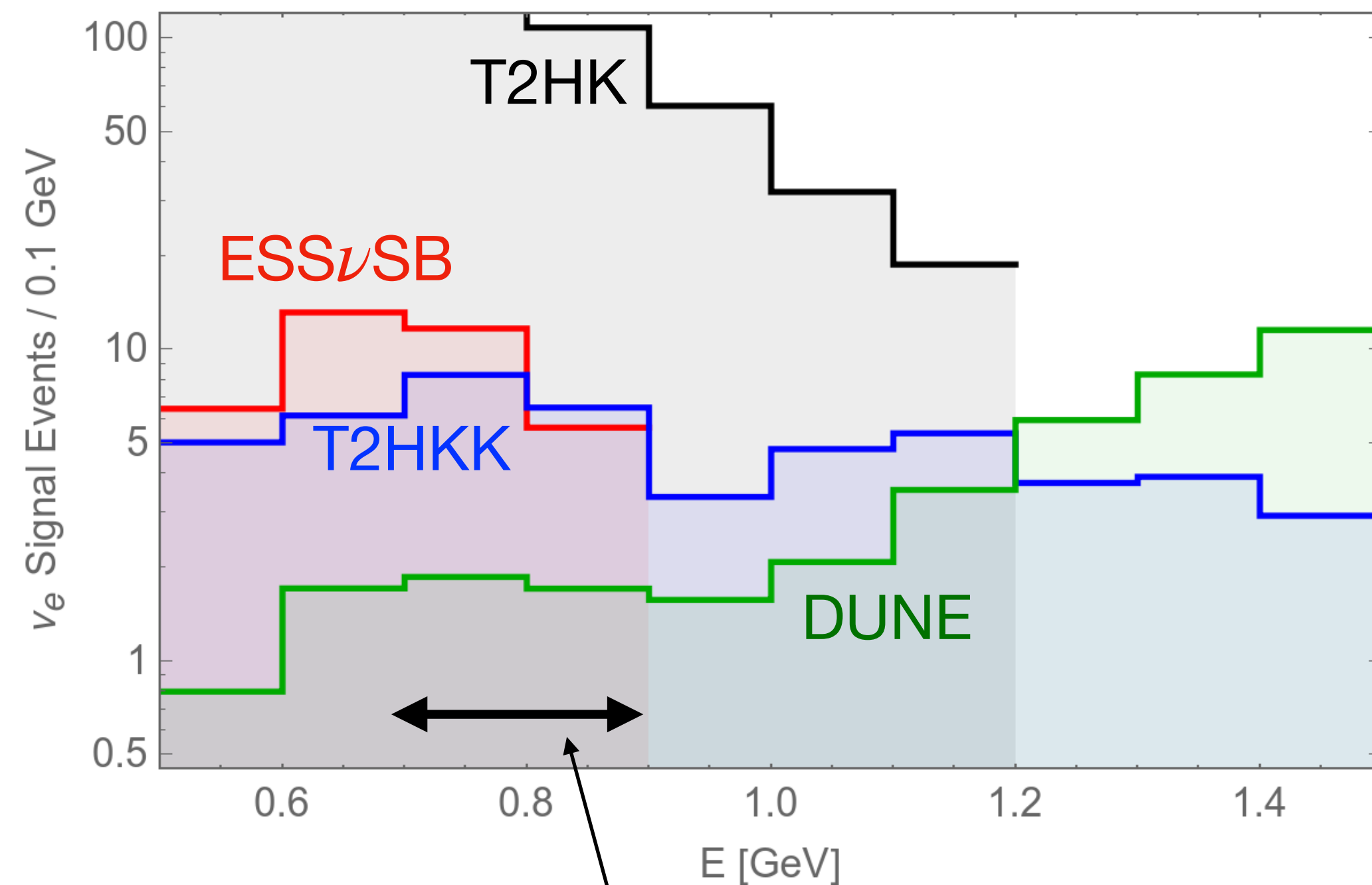
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T-odd

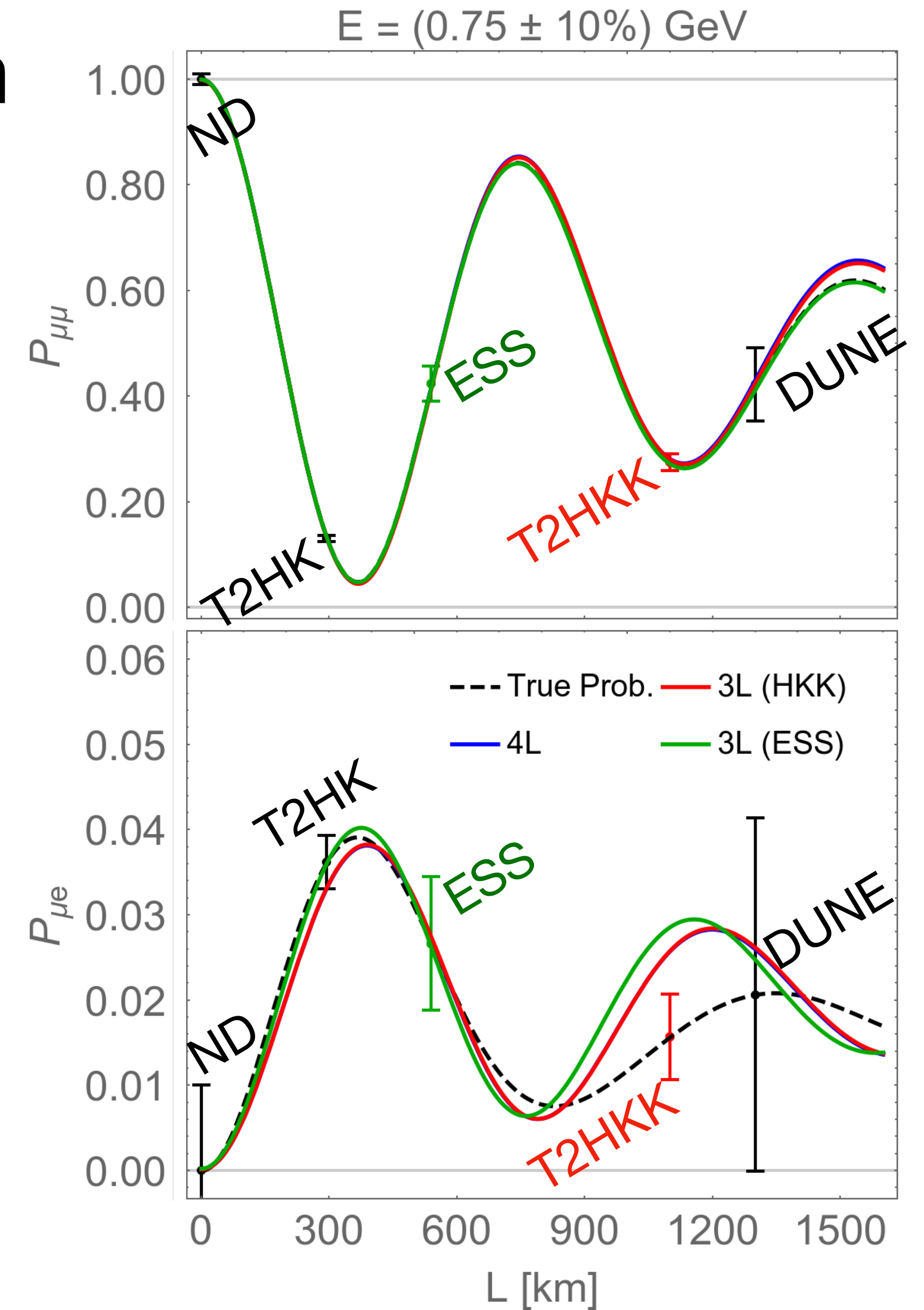
if data cannot be fitted only with the L -even part,
fundamental T violation is established model-independently

Model-independent test of T-violation

Does it work in real life?

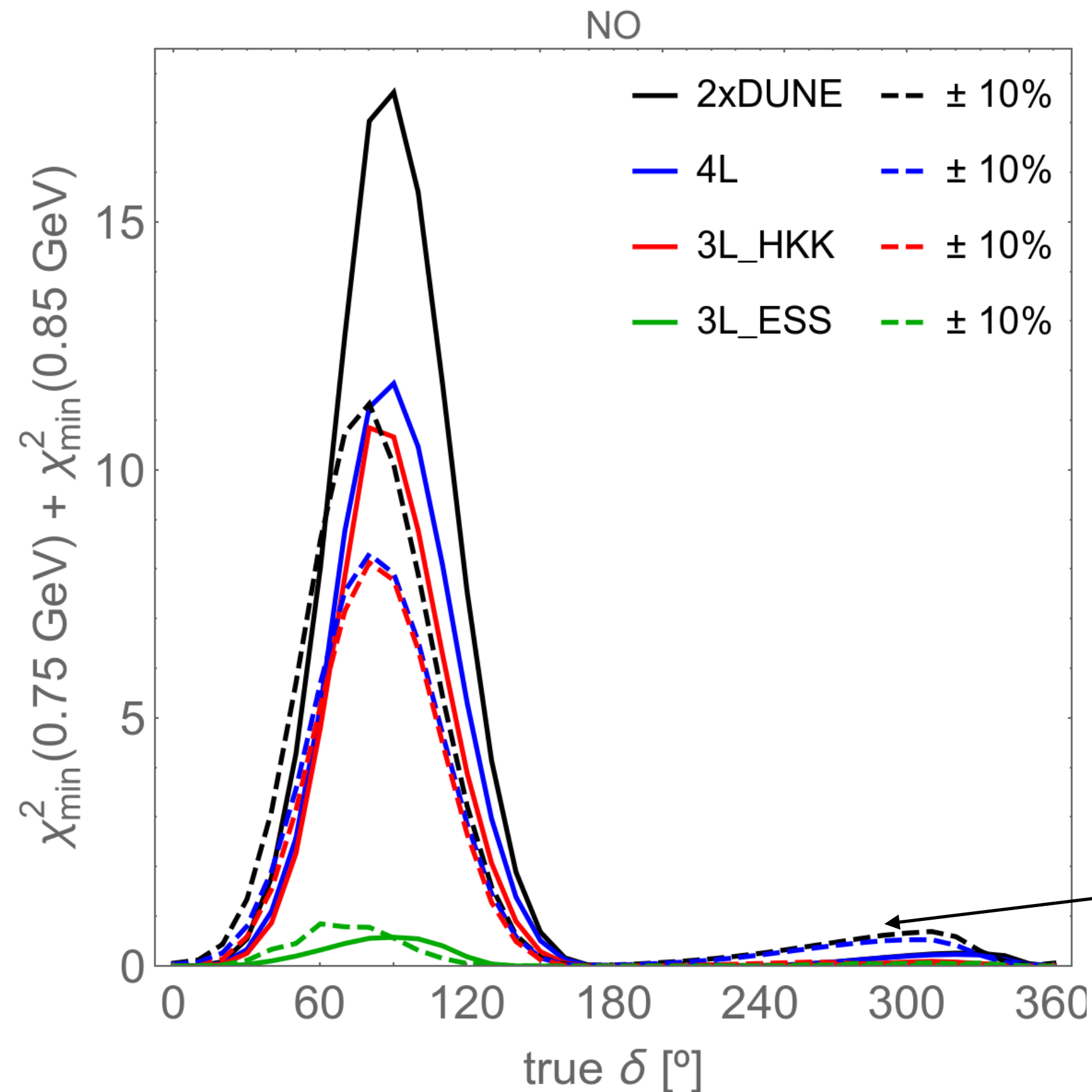


most sensitive energy interval



Model-independent test of T-violation

Does it work in real life?



- $\sim 3\sigma$ sensitivity seems possible with DUNE & T2HK & T2KK
- **good energy resolution** crucial
- uses **low-energy tail of DUNE**
- **detector in Korea needed** to cover 2nd osc. max.
- $\delta_{\text{CP}} \sim 270^\circ$ can be tested with antineutrino data (not shown)

Summary

- great progress in 3-flavour oscillation parameters
- hint for CP violation below 2σ
- slight preference for normal ordering from oscillations ($\Delta\chi^2_{\text{IO/NO}} \approx 7$)
- cosmology sensitivity to neutrino mass very exciting
- current cosmo preference for normal ordering is strongly prior dependent (for ordering-agnostic prior the preference is dominated by oscillation data)
- propose model-independent test for T-violation
combining data from 3 LBL experiments at the same energy
- requires detector at 2nd osc. max. (T2KK), good energy resolution,
low-energy tail of beam in DUNE

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Thank you for your attention!