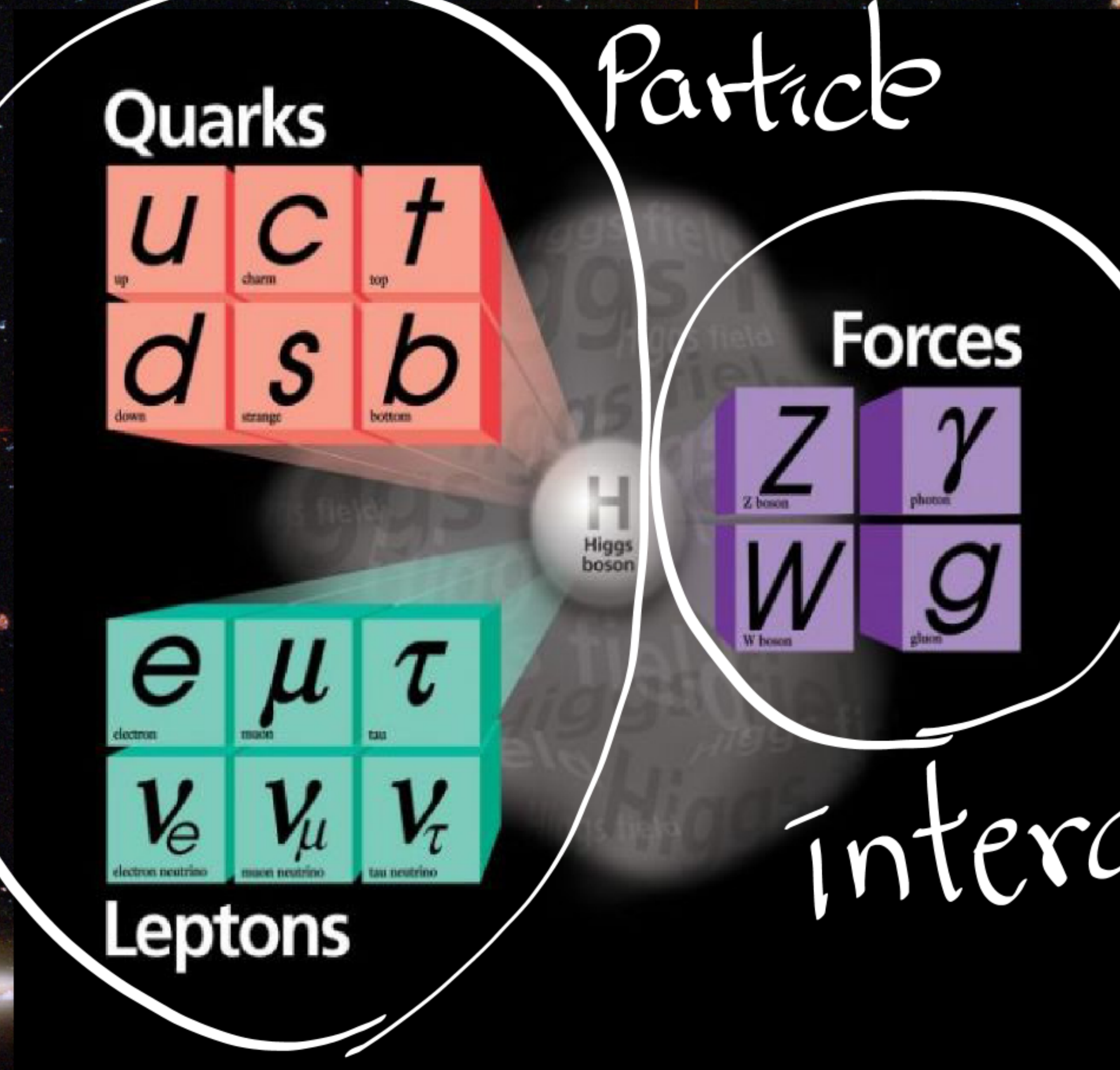


물질의 근원과 힘



interactions

거시 $\rightarrow$ 미시.
(D.M.) 빛 (입자)
 e (파동)

$\psi(\mathbf{r})$: Maxwell eq. $m=0$
 $L, k \sim 10^6 \text{ eV}$

e^- (mass problem)

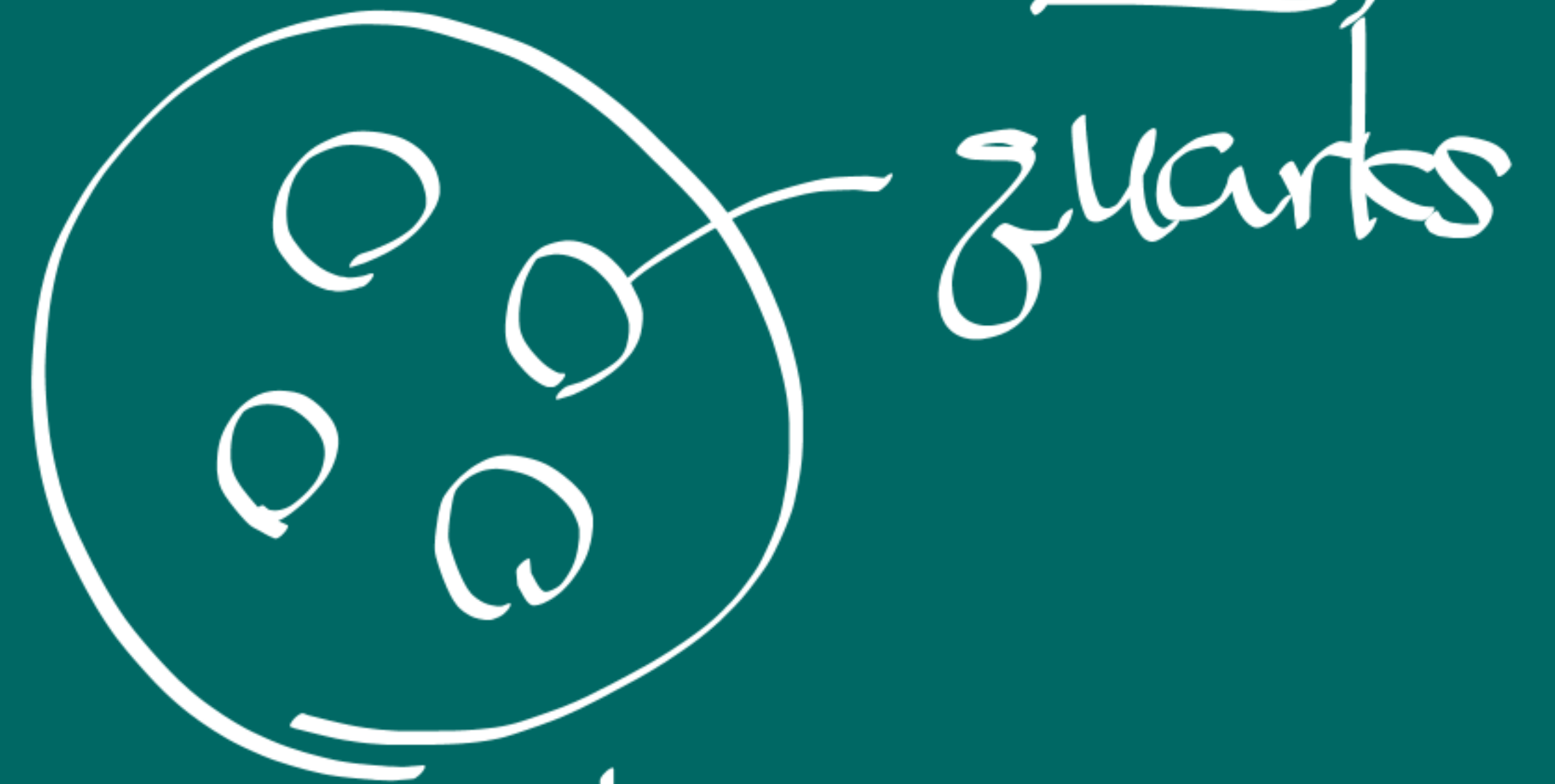
$\rightarrow e^+$ (anti-particle)

L , Vacuum: $\Delta E \cdot \Delta t \geq \hbar$

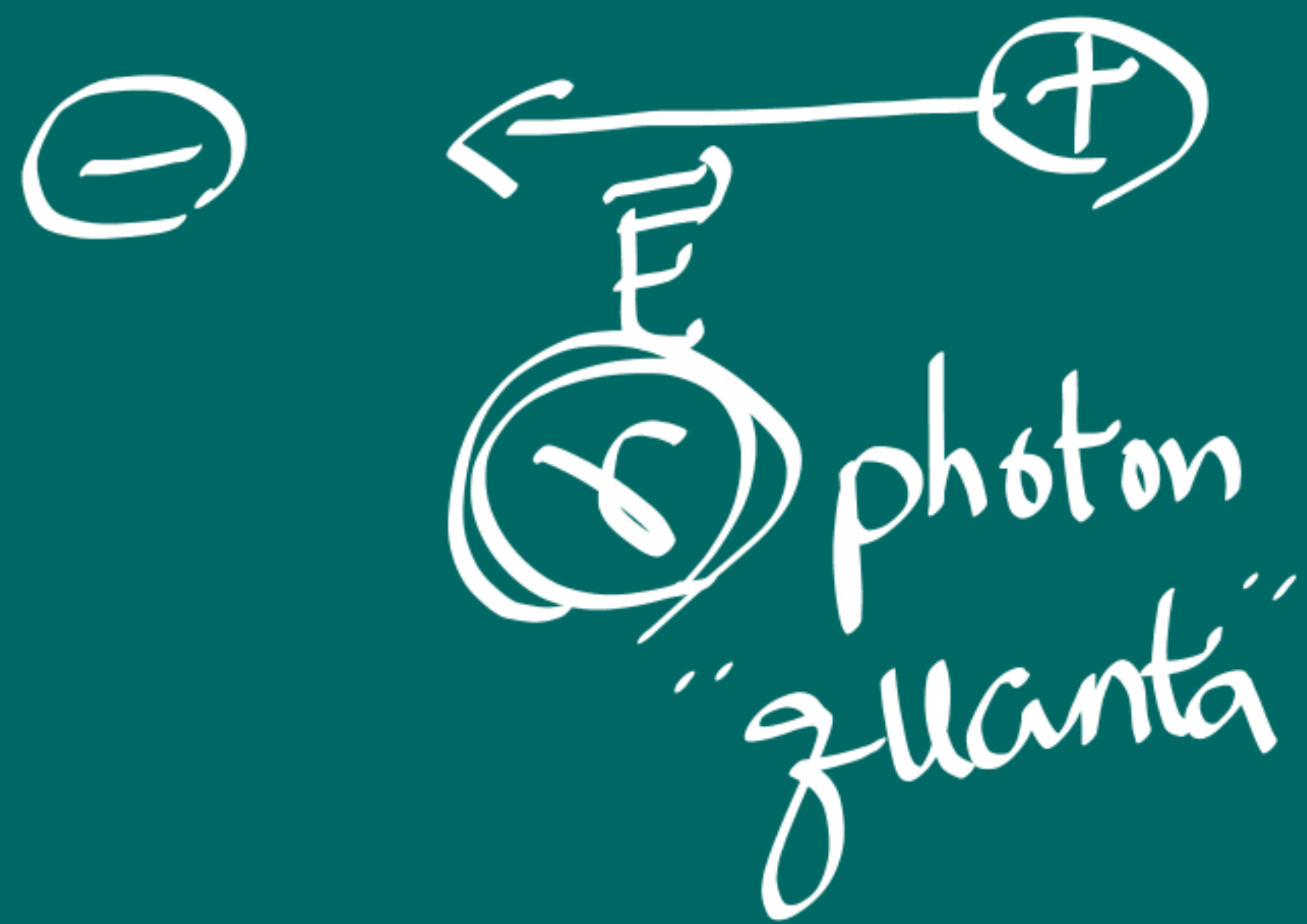
Virtual Work: $\Delta E < \hbar / \Delta t$
 $1 \text{ MeV} \sim 10^{-21} \text{ s}$

$n \rightarrow p e^- + \gamma$
 $314 \Rightarrow \text{LN cons.}$
 $m_\nu = 0$ ($\vec{\sigma} \cdot \vec{p}$: ant, "Left-H")

Inelastic $e-p$



3: u, d, s
 $+3$



Pion discovery.
 $m_\pi = 140 \text{ MeV}/c^2$

$$\Delta p \cdot \Delta x \geq \hbar$$

(e.m.)

$$\frac{\Delta p c}{mc^2} \sim \frac{\hbar c}{\Delta x} = \frac{1.24 \text{ keV} \cdot \text{nm}}{6\pi \cdot 10^{-15} \text{ m}} \sim 200 \text{ MeV}$$

$$\nabla^2 \psi - \frac{1}{c^2} \frac{\partial^2 \psi}{\partial t^2} = \left(\frac{mc}{\hbar} \right)^2 \psi ; \text{K.G}$$

$m(x) = 0$

Time-ind. ψ

$$\psi = U(r) = \frac{g_0}{4\pi r} e^{-r/R}$$

$$R = \frac{\hbar}{mc}$$

$$10^{-15} \text{ m} \leftrightarrow \hbar = 200 \text{ MeV}$$

$$\Leftrightarrow \frac{e}{4\pi\epsilon_0 r}$$

e.m.

e.m. self interaction.

$$e^- \left(e^- \frac{e^2}{4\pi\epsilon_0 r} \right)$$

α_{em} (strength)

$$= \frac{e^2}{4\pi\epsilon_0 \hbar c} = \frac{1}{137}$$

" $\alpha_{em} \sim 0.01$ "

Weak interaction.

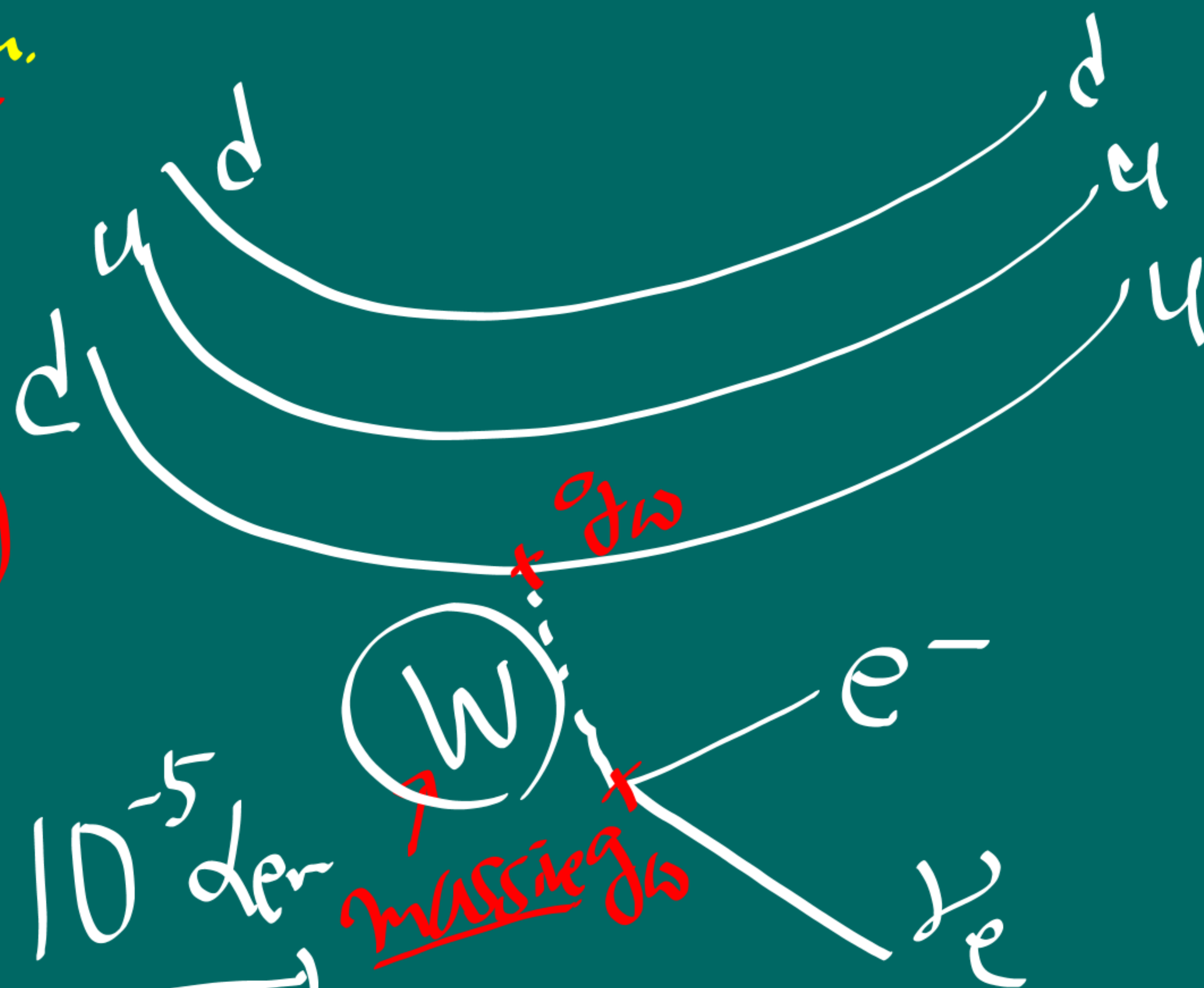


$n: ddu$
 $p: uud$

Contact int: $(10^{-5}) \alpha_{em.}$
 + quarks

$\alpha_{weak} \sim \frac{g_w^2}{4\pi}$ (x)

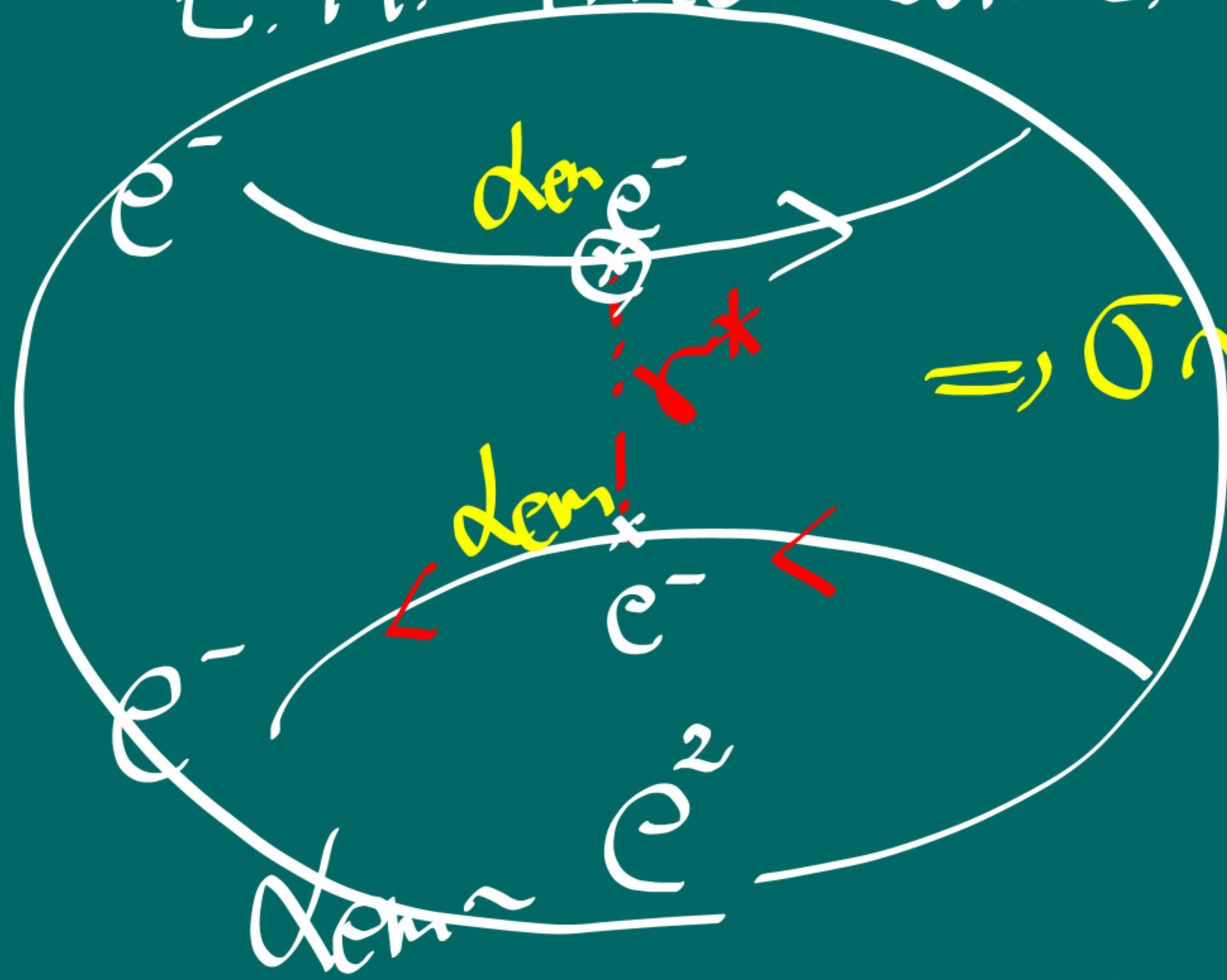
$\sim \frac{g_w^2}{M_W^2} \sim 10^{-5} \alpha_{em.}$



$\Delta p \Delta x \sim \hbar$

$\Delta x \sim 10^{-18} m. \Leftrightarrow \Delta p \cdot c \sim 200 GeV$

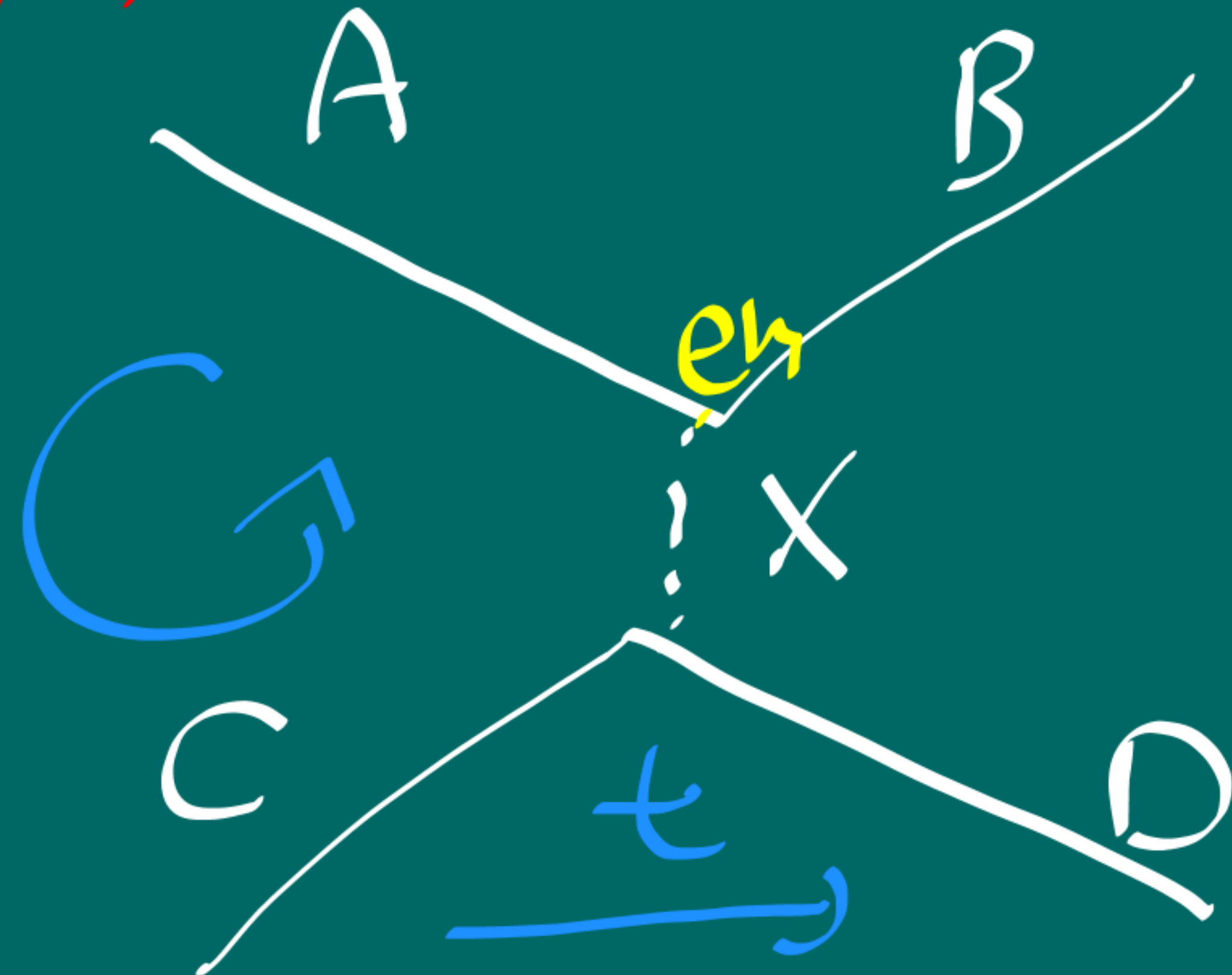
E.M. Interactions.



$$e^{-i(Pz - Et)/\hbar} \quad (E) \quad (1-\gamma)$$

$$e^-e^- \rightarrow e^-e^-$$

$$e^-e^+ \rightarrow e^-e^+$$

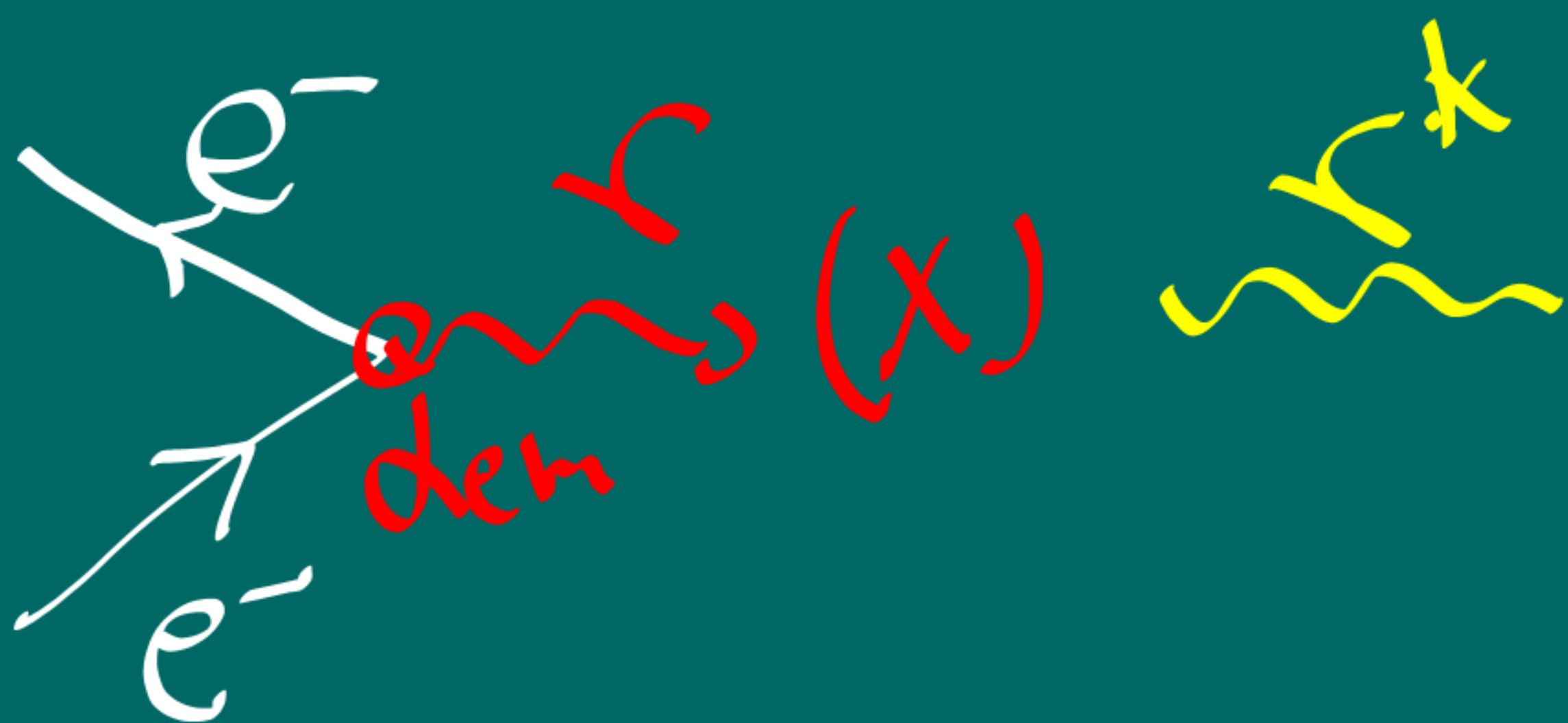


$$A + C \rightarrow B + D$$

(Dynamics: all possible if kinematics are allowed.)

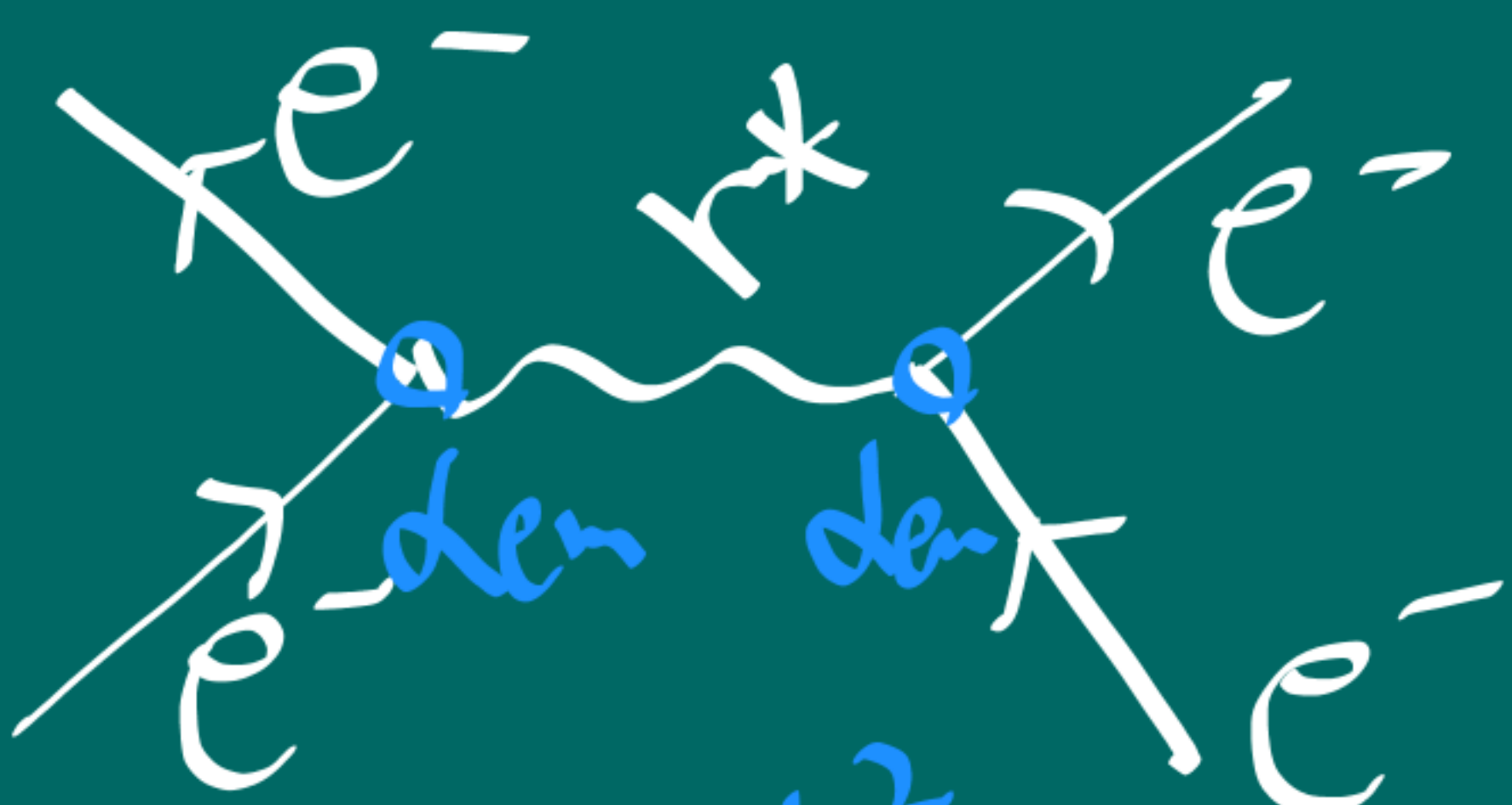
Scattering. amp = $M = \frac{\alpha_{em}}{q^2 + m^2} = M$

$$\sigma(\text{prob}) \sim |M|^2 = \frac{\alpha_{em}^2}{q^4}$$



$$e^-e^+ \rightarrow \gamma(x), \gamma\gamma(0)$$

$$\rightarrow \gamma^* (m_{\gamma^*} \neq 0), L(T)$$



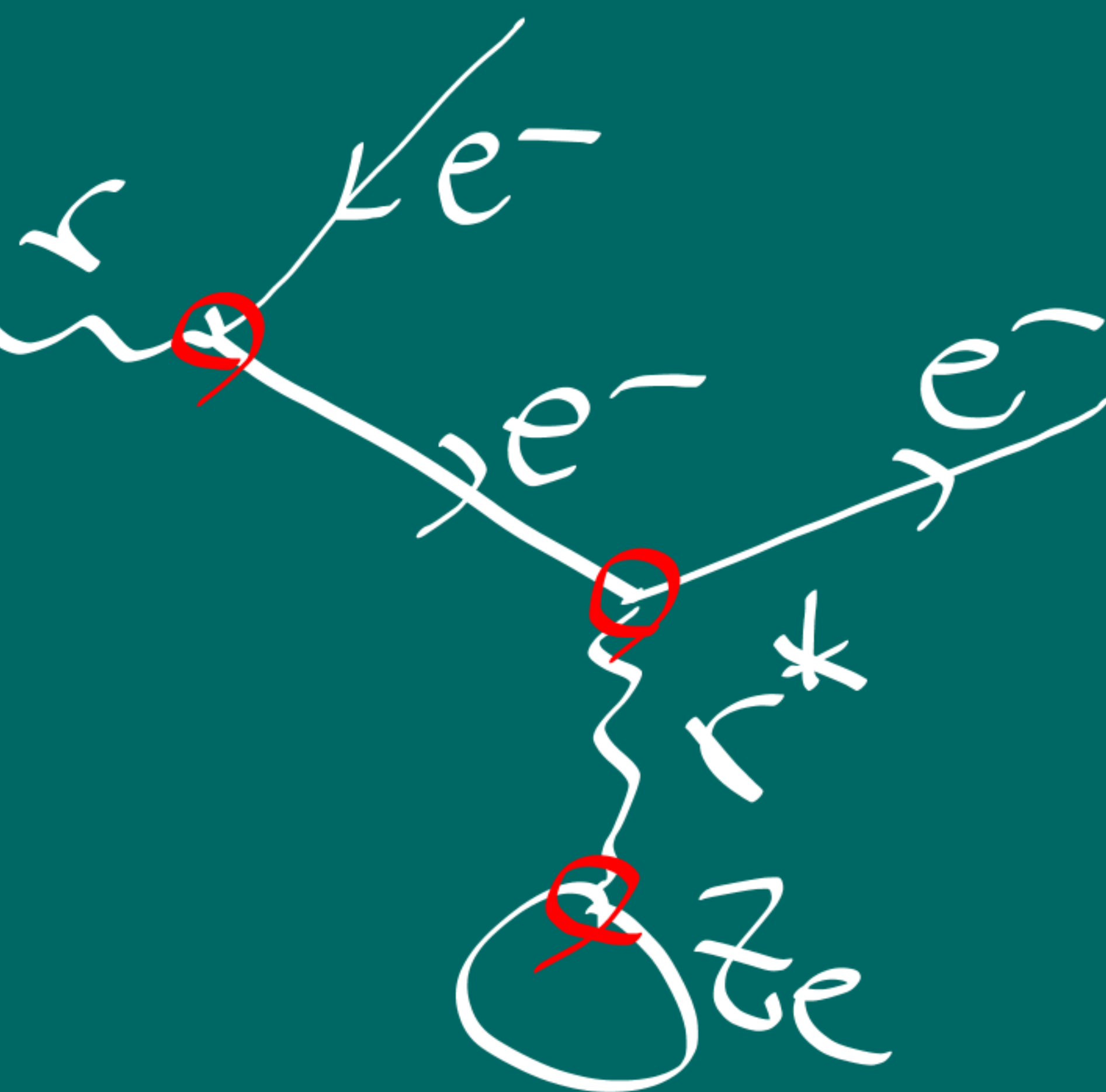
$$\alpha_{em} = \frac{e^2}{4\pi\epsilon_0\hbar c}$$

$$\sigma \sim \alpha_{em}^2$$

$$\sigma \sim \alpha_{em}^2 \alpha_{em} Z$$

$$\sim \alpha_{em}^3 Z$$

$$(\alpha_{em})^2 Z$$

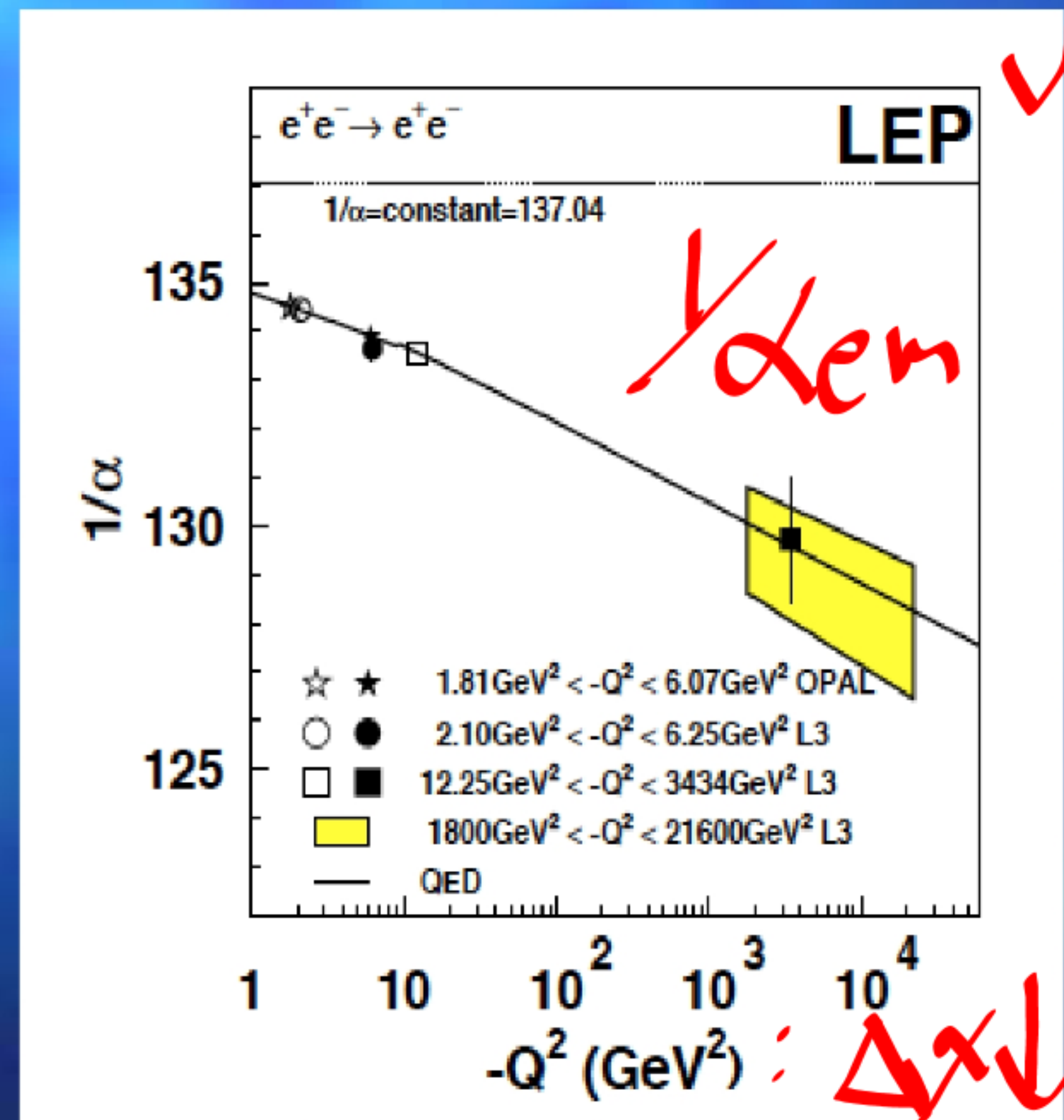


$$1 \text{ GeV}/c$$

$$\lambda \sim 10^{-15} \text{ m}$$

Electromagnetic Coupling

- Electromagnetic constant is increased as λ is decreased.
- Coupling constant is running



$$\alpha_{\text{em}} \sim \frac{1}{137} \sim \frac{g_e^2}{4\pi\epsilon_0 \hbar c}$$

$$\alpha_{\text{weak}} \sim G_F \sim 10^{-5} \cdot \alpha_{\text{em}}$$

$$\sim \frac{g_w^2}{4\pi}$$

$$g_w \sim 0.6$$

$$M_W^2 \sim 6400 \text{ GeV}^2$$

$$n \rightarrow p e^- \bar{\nu}_e \text{ (weak)}$$

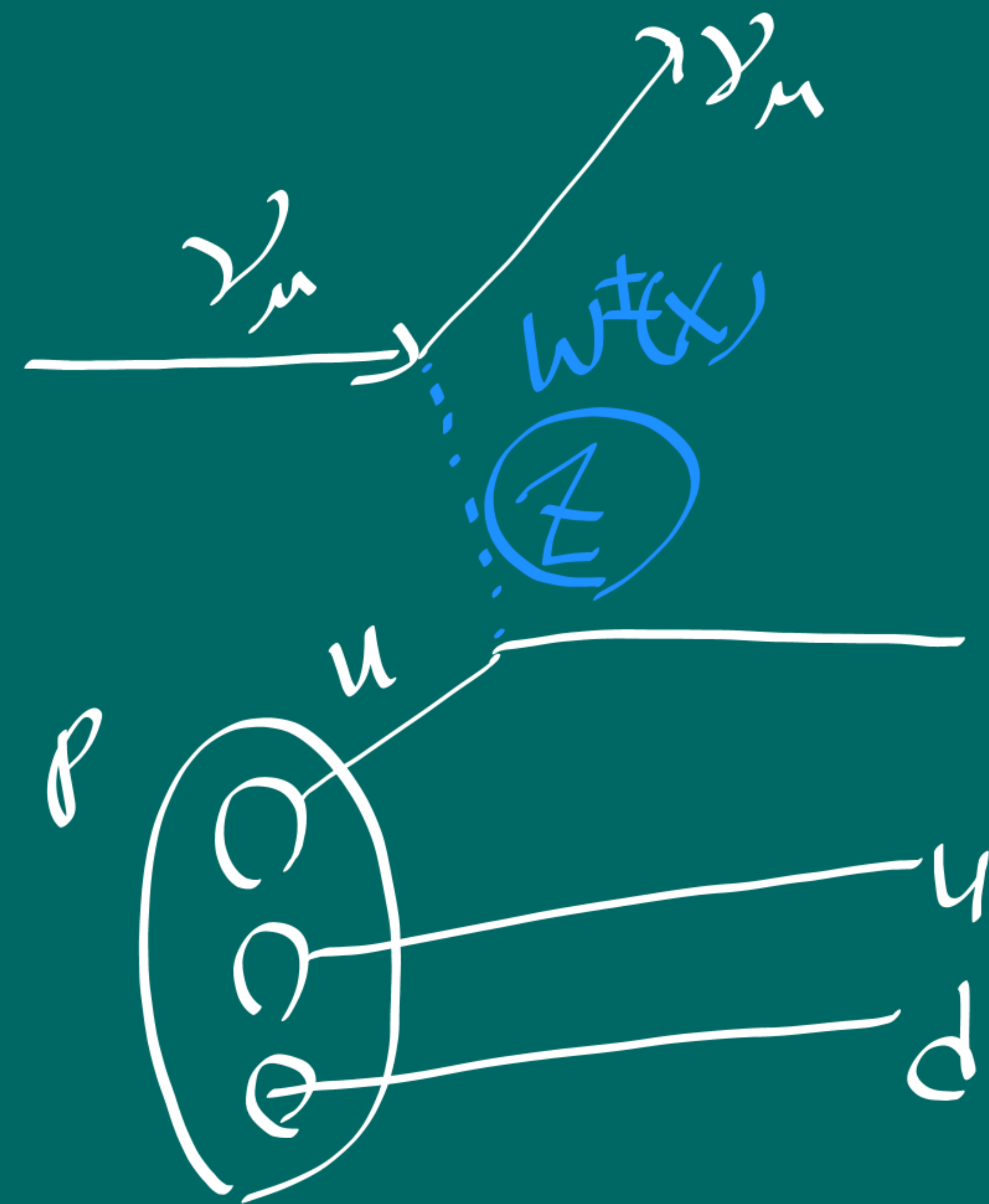
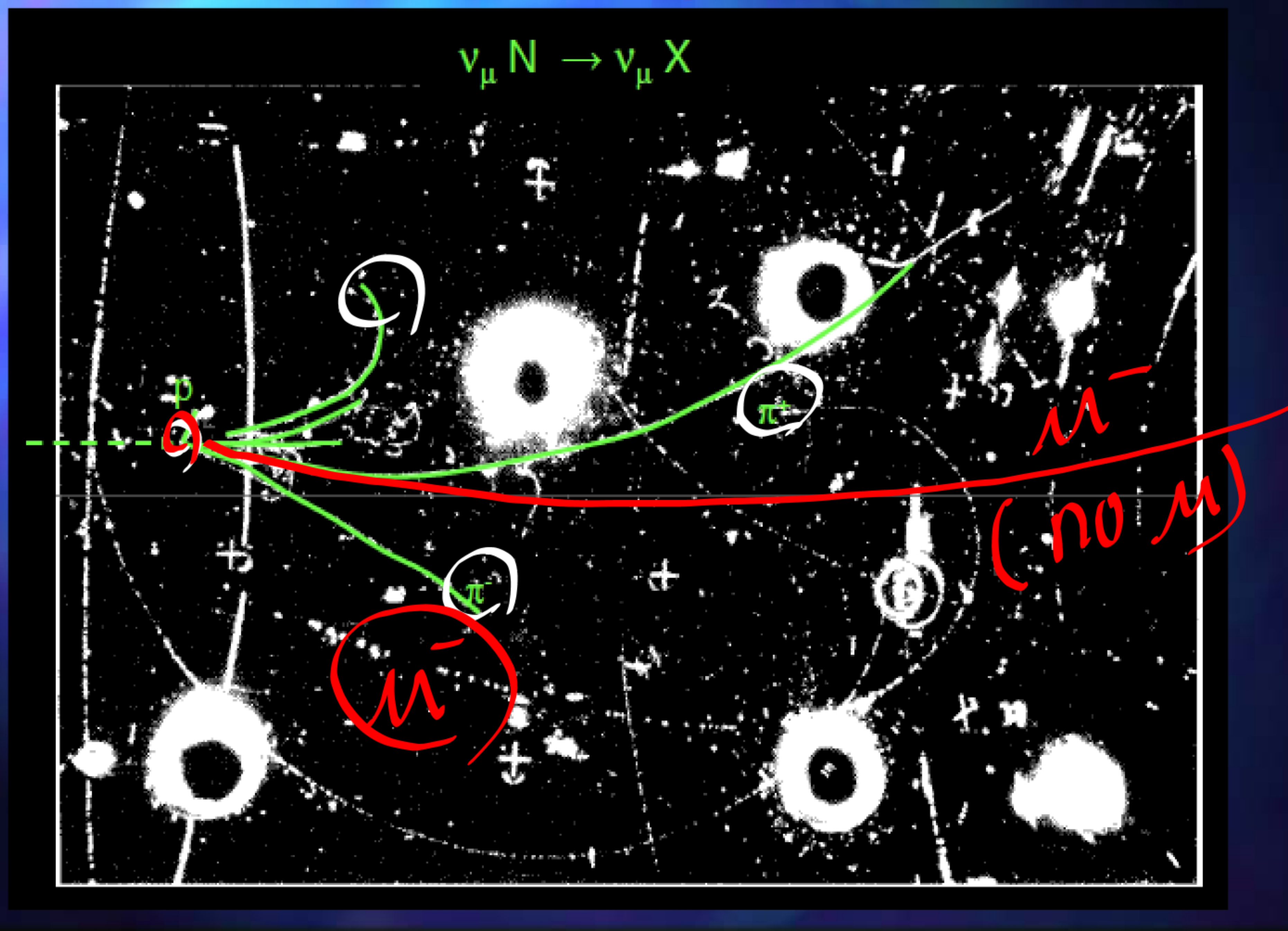
W^+

$$\bar{\nu}_e + e^- \rightarrow \bar{\nu}_e + e^-$$

$$\nu_\mu + N(n/p) \rightarrow \mu^- + X$$

$$\rightarrow \text{Nothing } (\nu_\mu) + X$$

Neutral Current (1971)

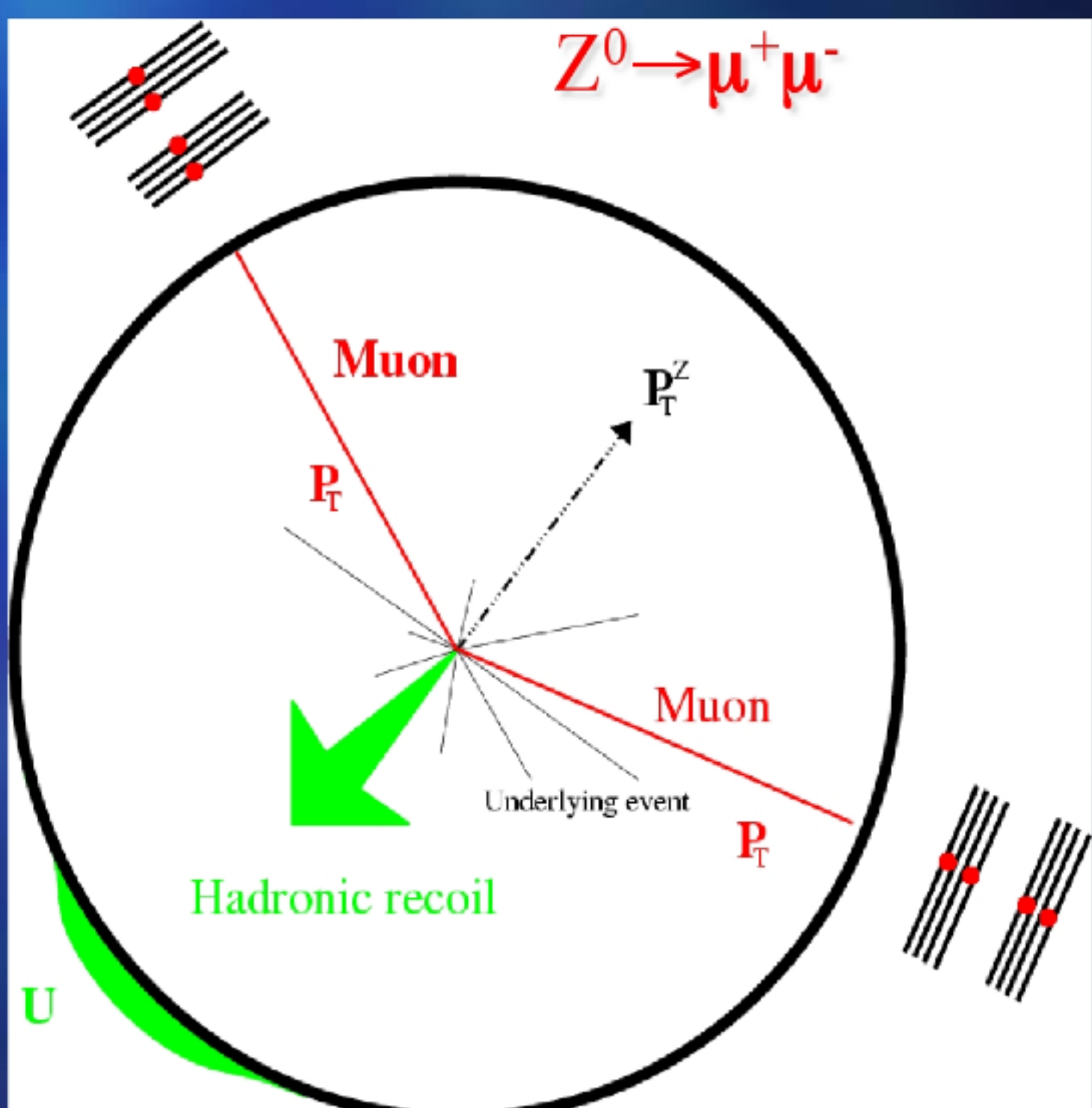
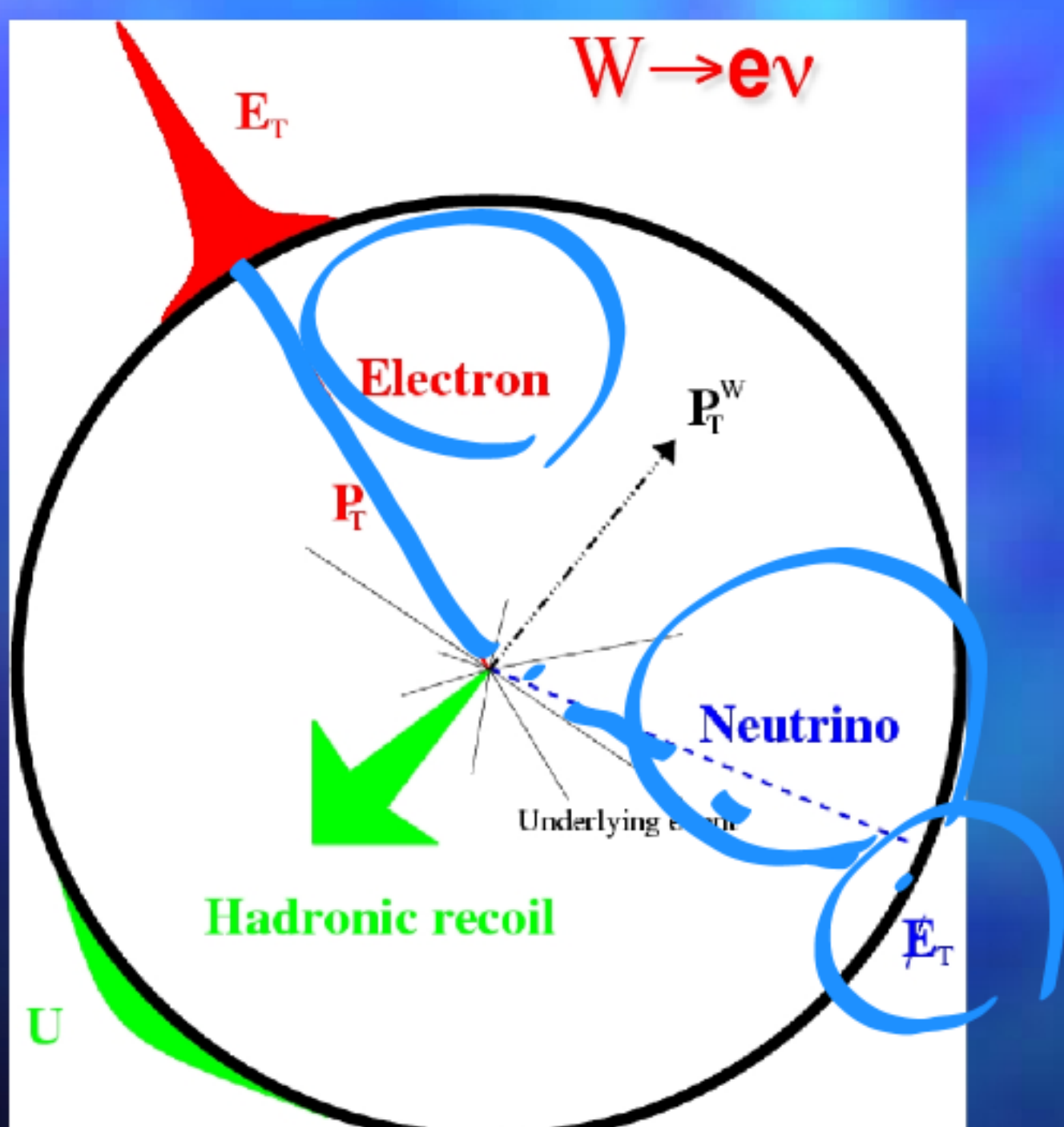
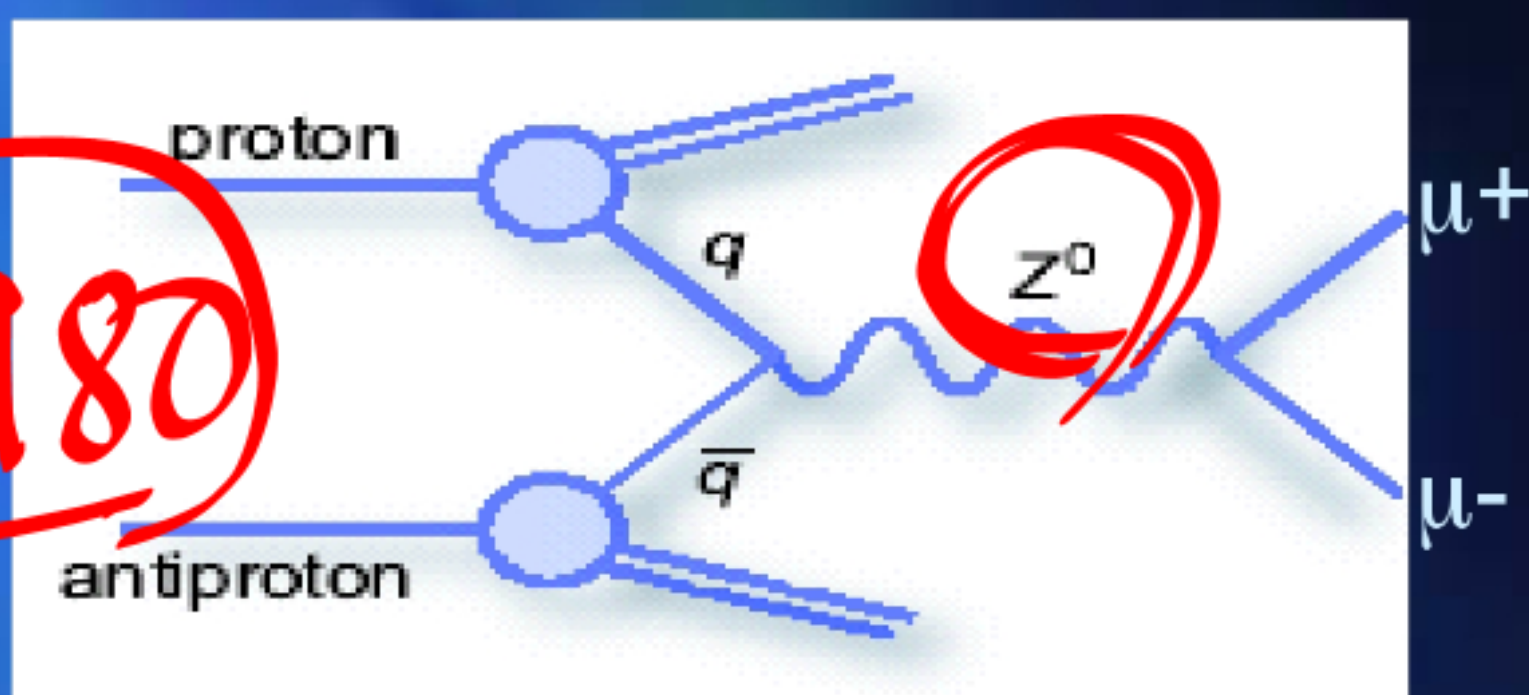
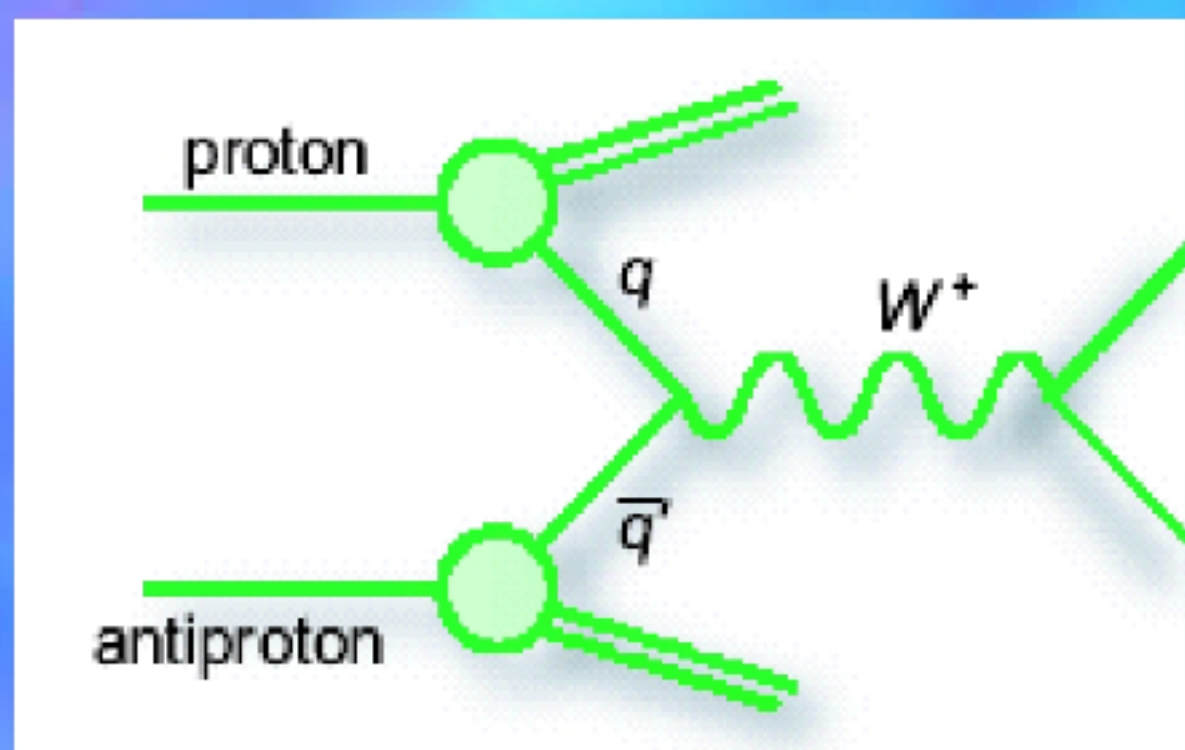


$$G_H \sim \frac{g_W^2}{M_0^2} \quad \text{NC event rate. (Mz)}$$

$$m_W = m_Z \cdot (\cos \theta_w) \quad \theta_w \sim 30^\circ$$

C. Rubia: $p \bar{p}$ (CERN)

W and Z events



Handwritten notes on the right side of the slide:

$$u(40 \text{ GeV}) + e^- \rightarrow W^+ + \nu_e$$

$$(u \bar{d}) \rightarrow W^+$$

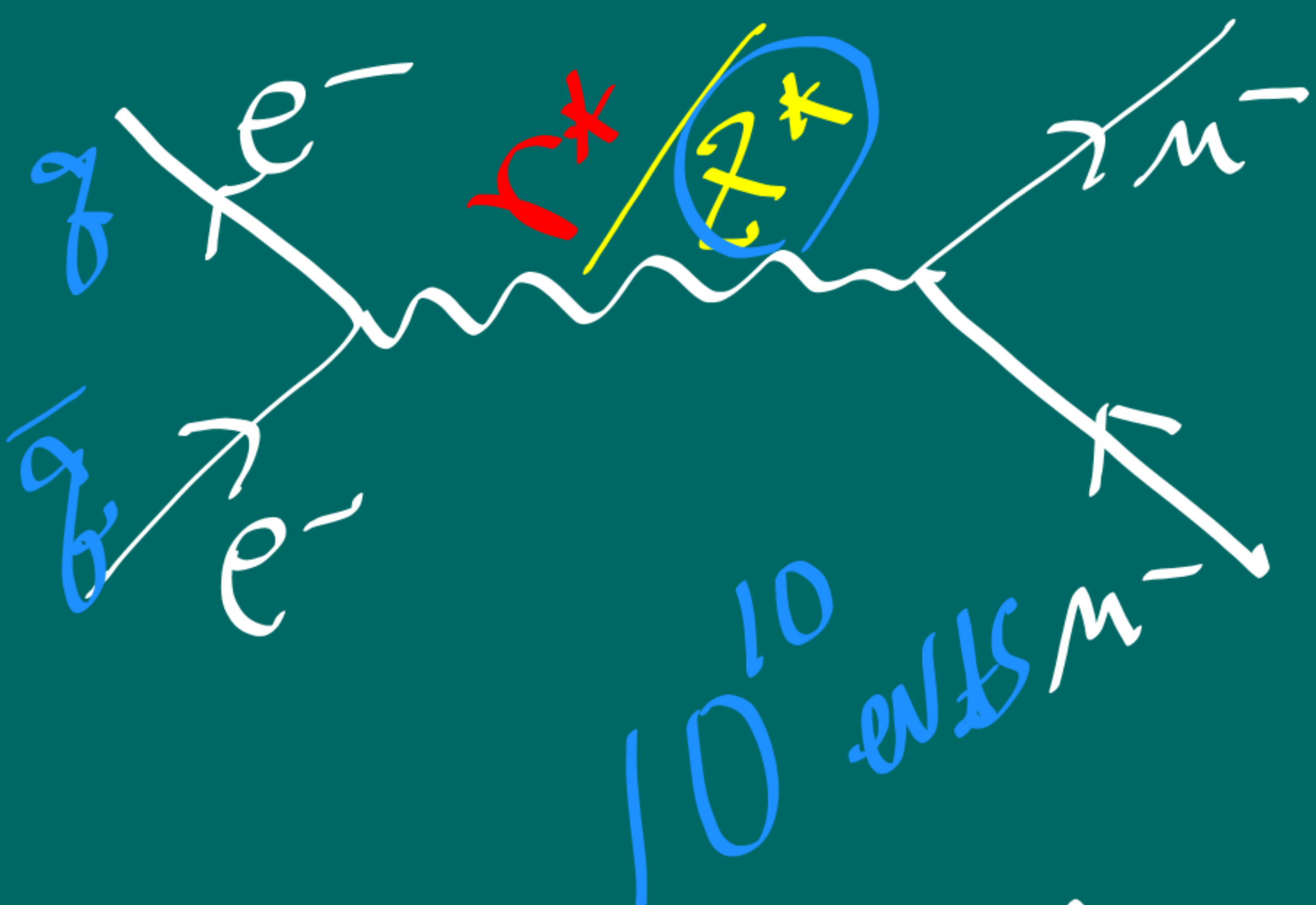
$$g_W^4$$

$$\frac{(-g^2 + M_Z^2)^2}{-M_Z^2}$$

NC: ~1970 → 1981 (discovery)
(pred.) (evidence)

Resonance

$$e^- e^+ \rightarrow \mu^- \mu^+$$



em.

$$\sigma \sim \frac{\alpha_{em}^2}{s}$$

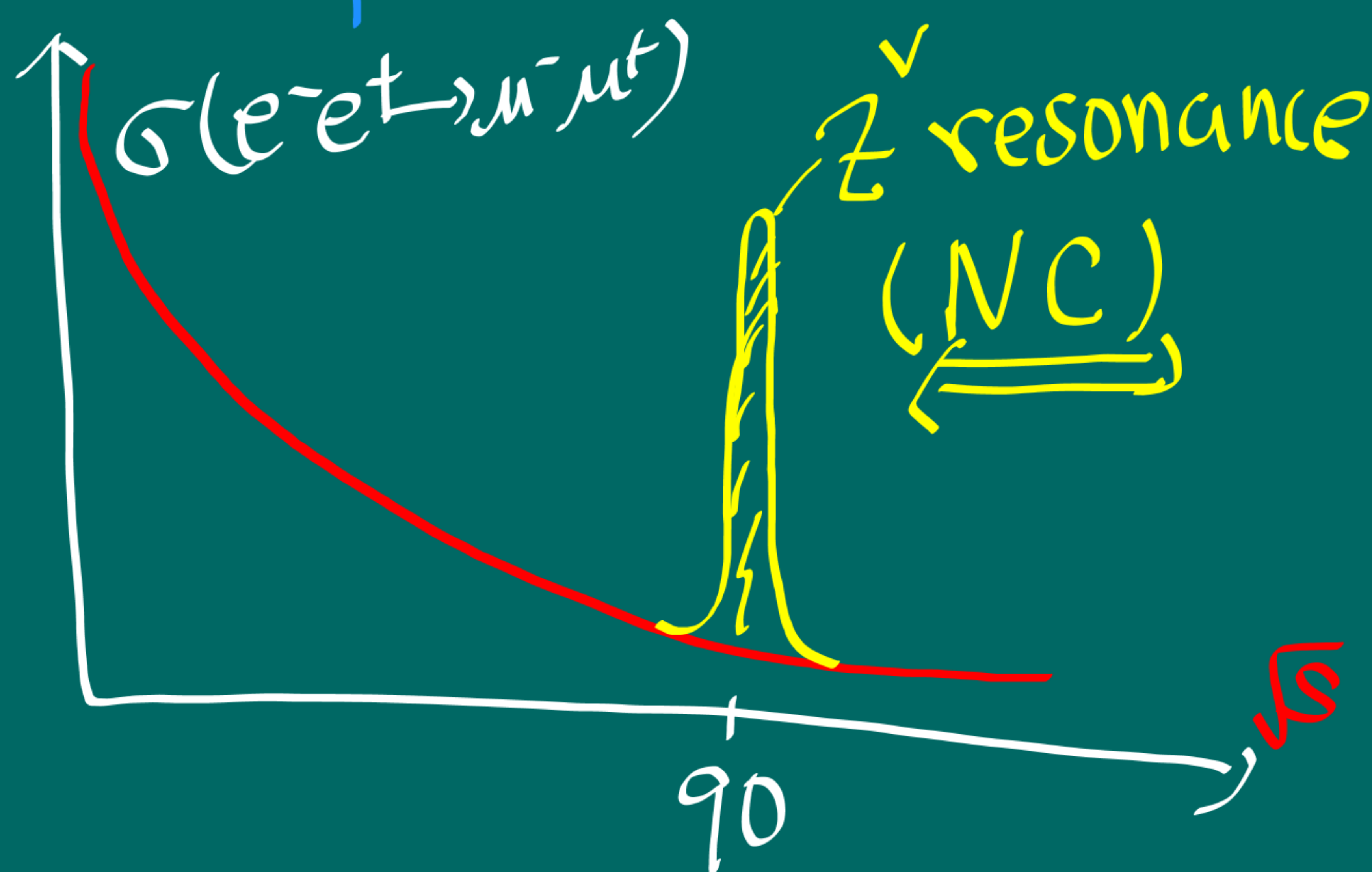
$$\sqrt{s} \ll M_Z$$

Weak.

$$G_F^2 \sim 10^{-10} \text{ den}^2$$

(Not possible)

$$\frac{G_F^2}{(M_W^2 + (g^2 + r))}$$

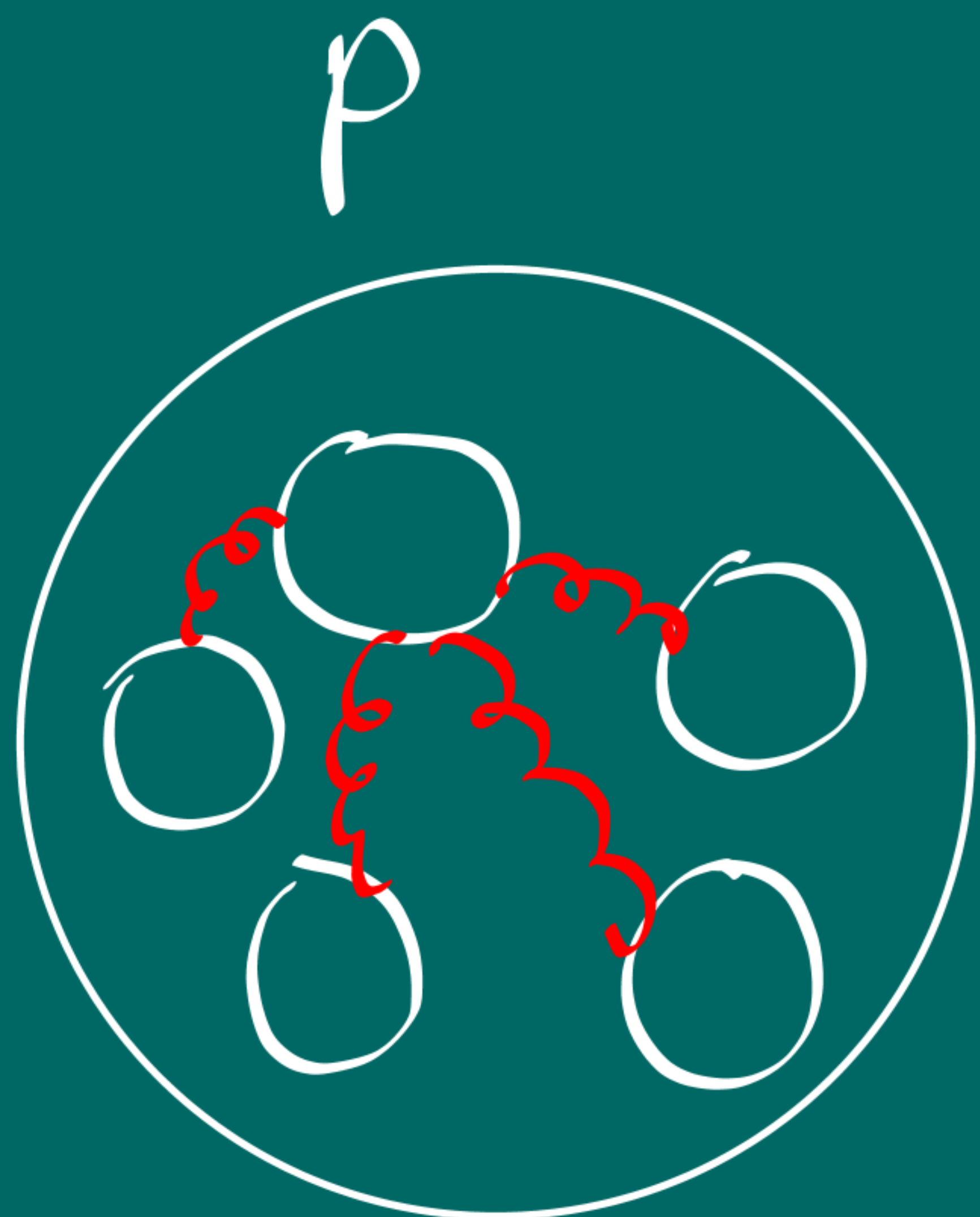


$$\frac{g_0^2}{(M_0^2 + \underline{g^2})} \Leftrightarrow e_m$$

$\Downarrow$
unified

$$Q^2 \sim 10^4 \text{ GeV}^2$$

$$\alpha_{em} \sim \alpha_{weak}$$



Strong Int: mediated by gluon.

Em. $\rightarrow$ electric charge.

Weak $\rightarrow$...

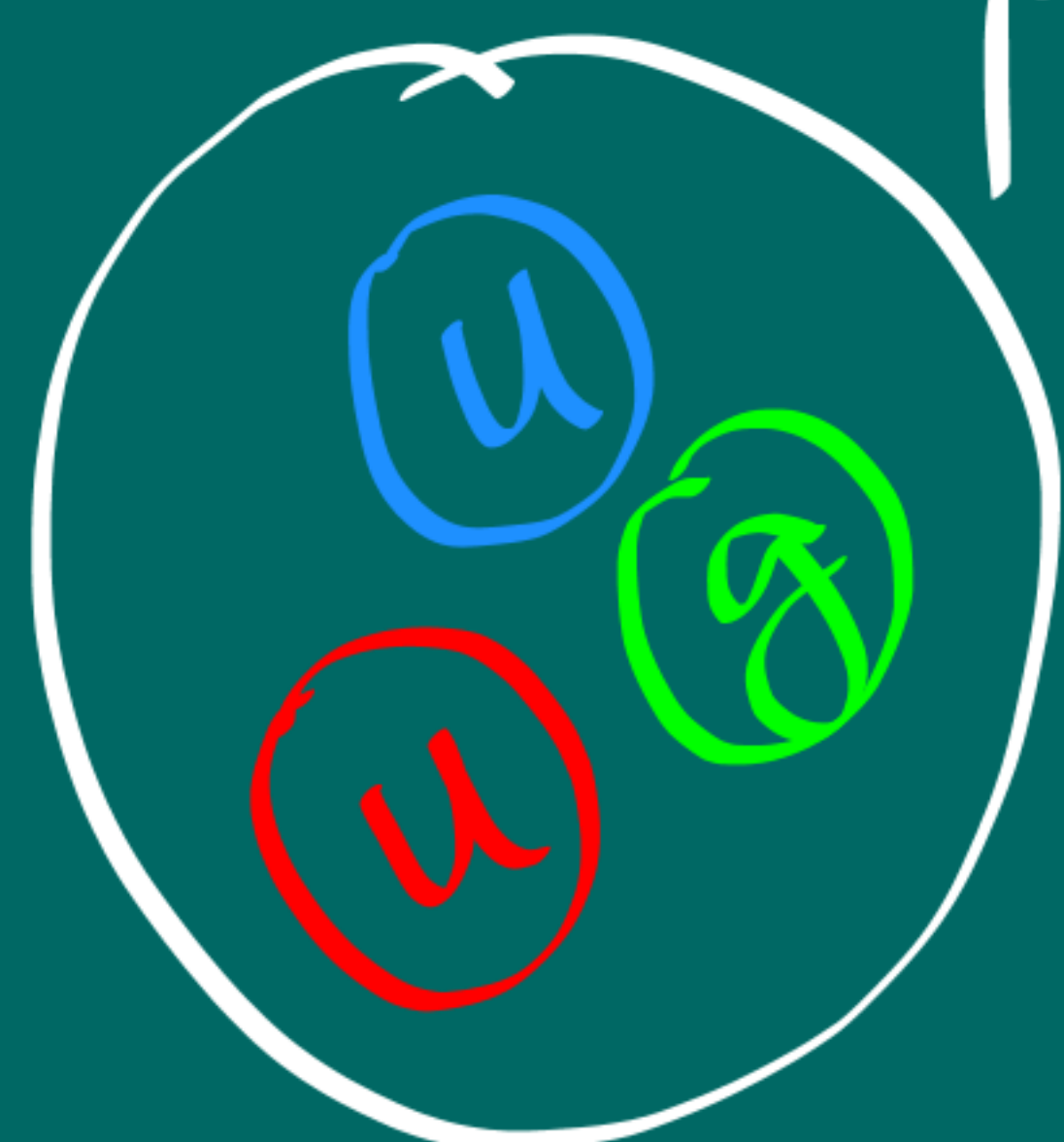
Strong $\rightarrow$ "color" $\bar{r} \bar{g} \bar{b}$

$e^-e^+ \rightarrow 3 \text{ jets}$

$P(\text{colorless})$

quarks: $(3H)$ (r, g, b)

gluon: $8H$



$\rightarrow$ How many colors?

(3)

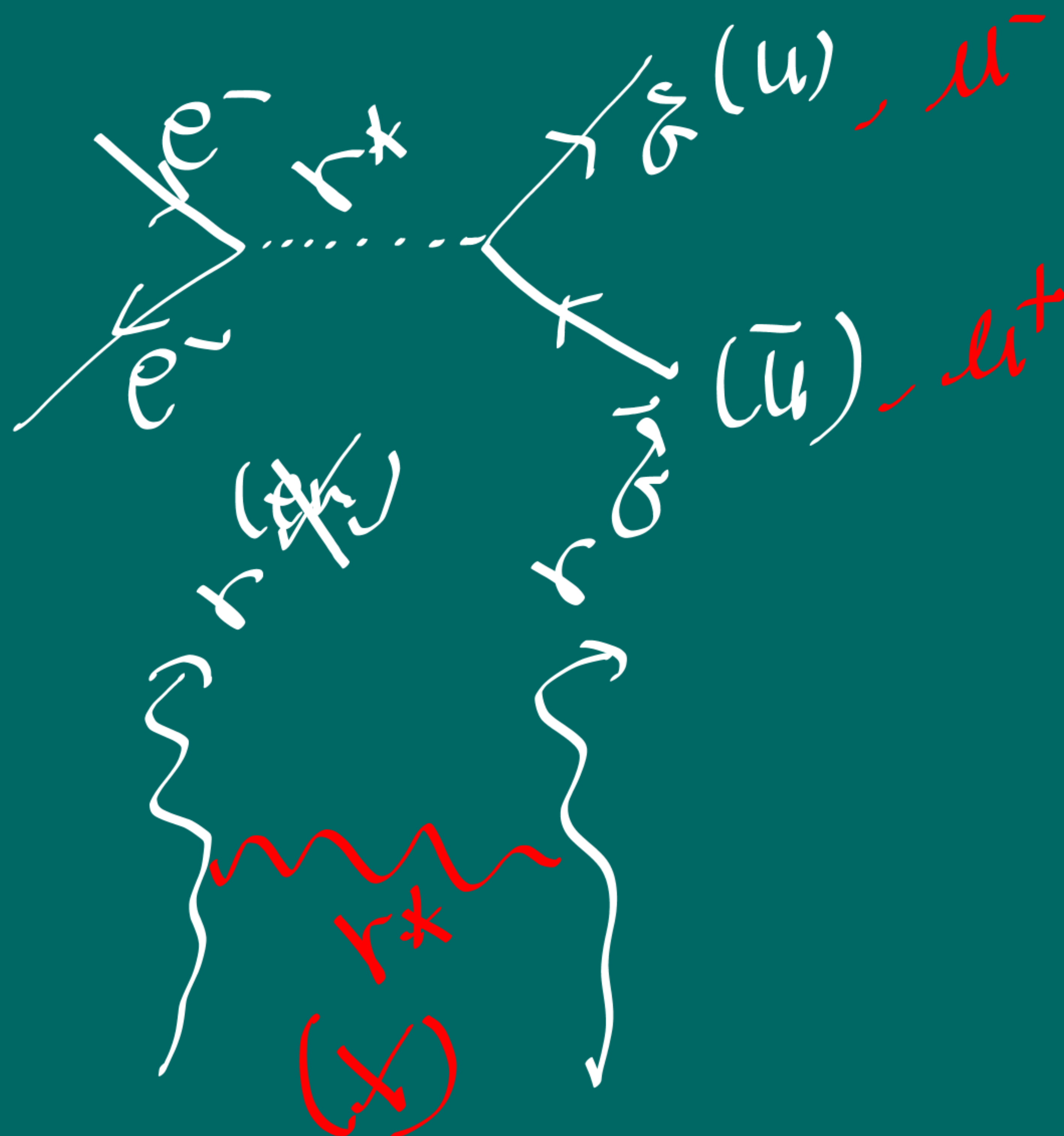
Gluon: (color)



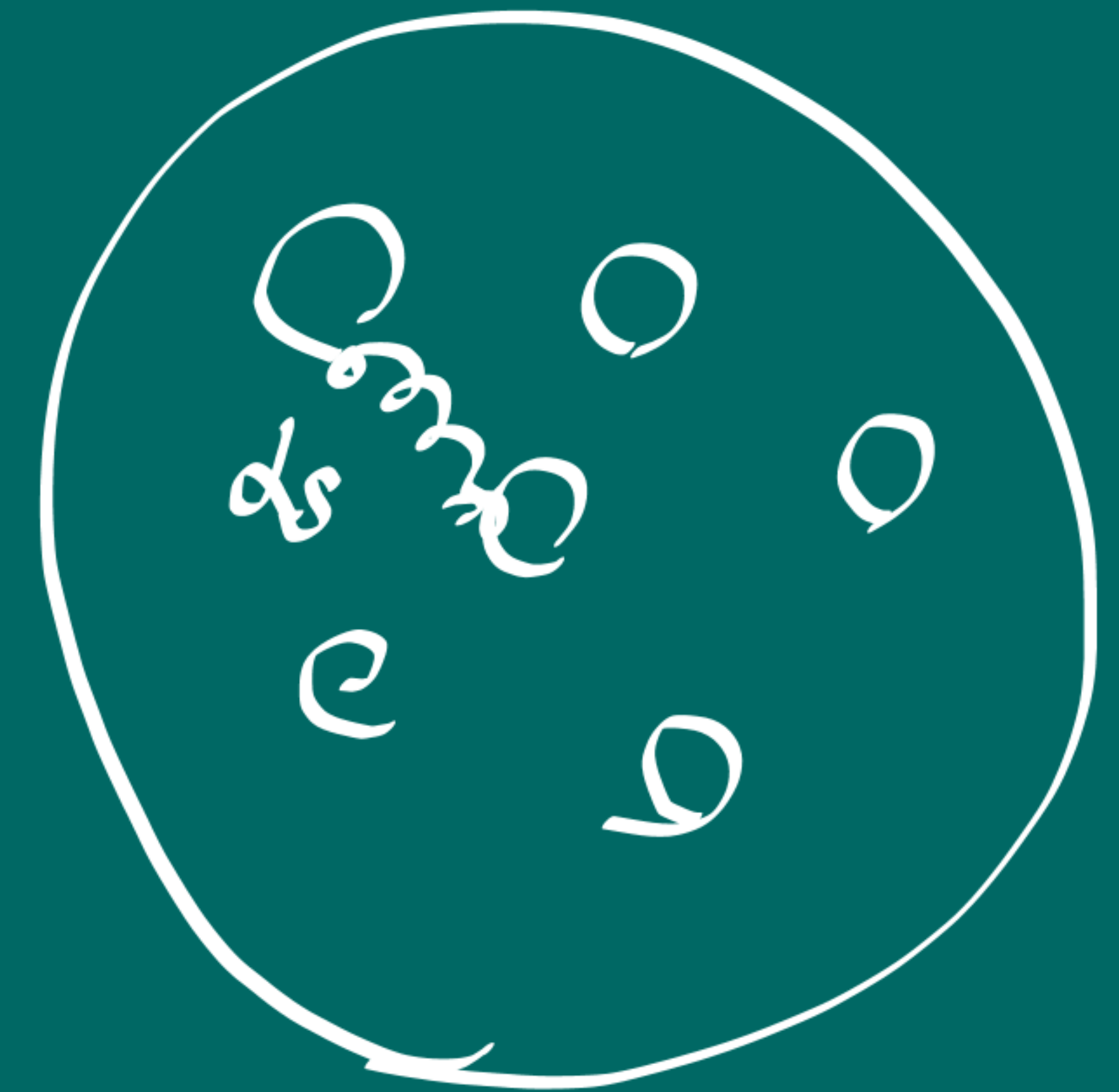
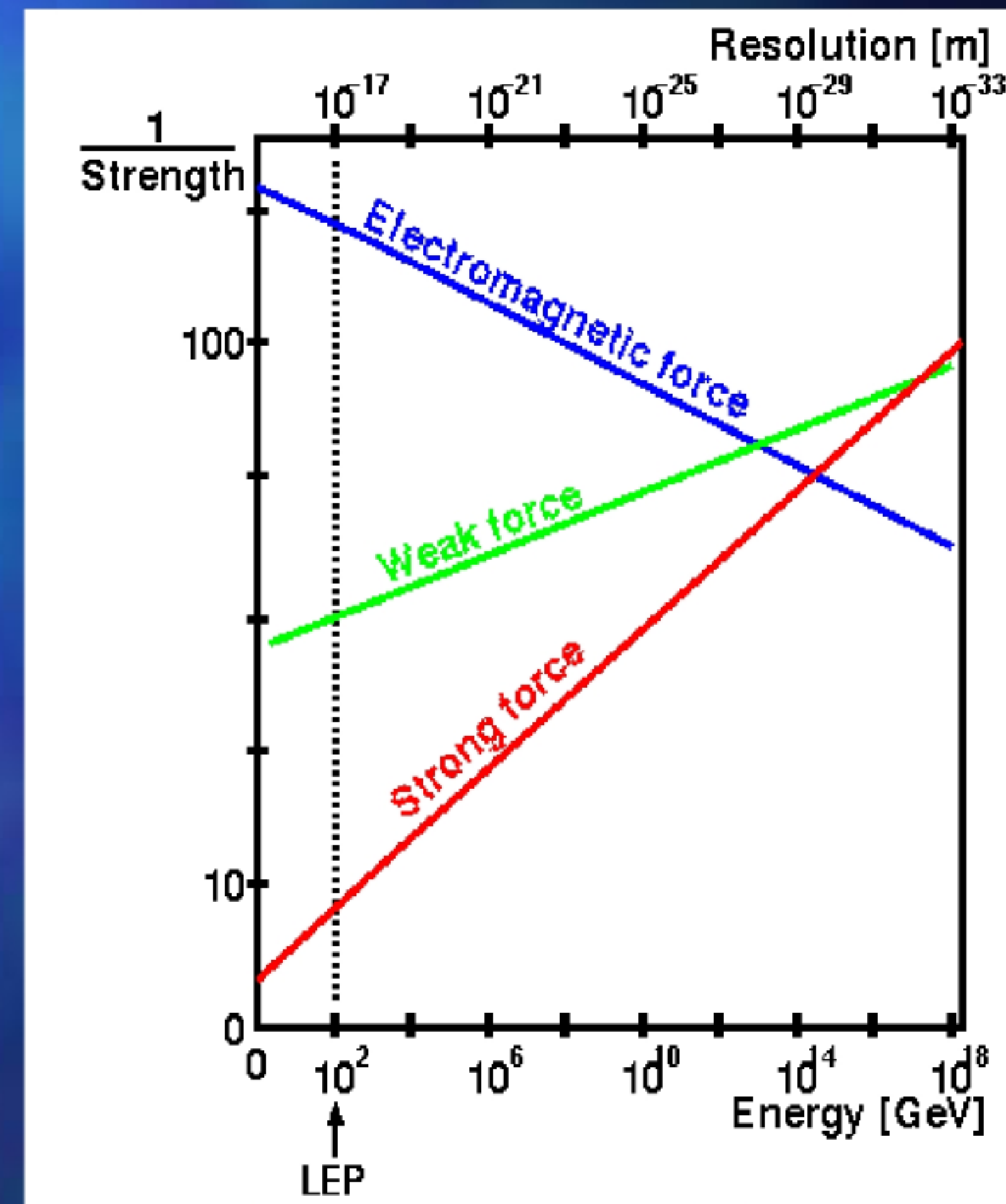
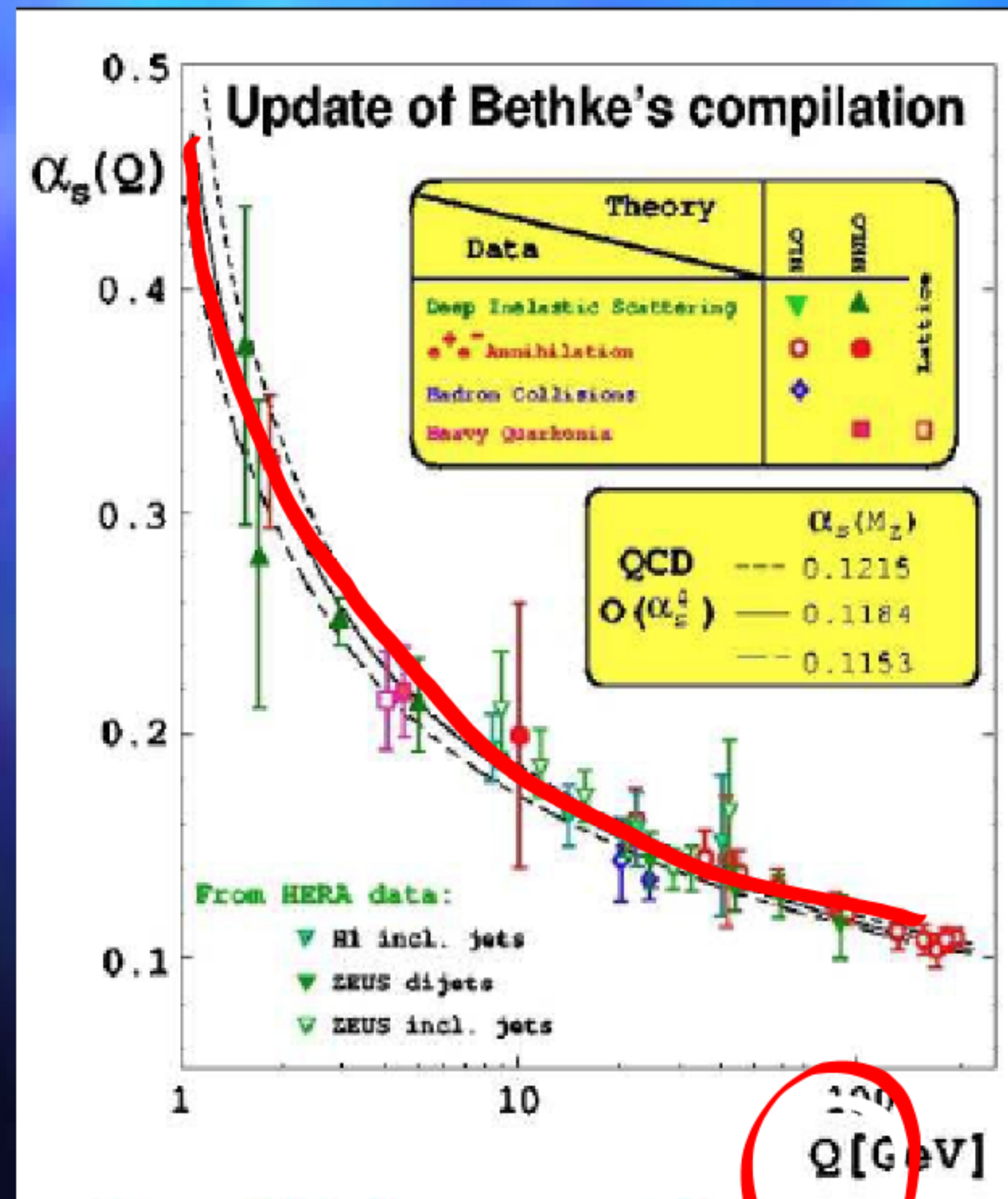
$$\Rightarrow \alpha_s \sim \frac{g_s^2}{4\pi} \quad (\downarrow \quad Q \uparrow)$$

anti-screening.

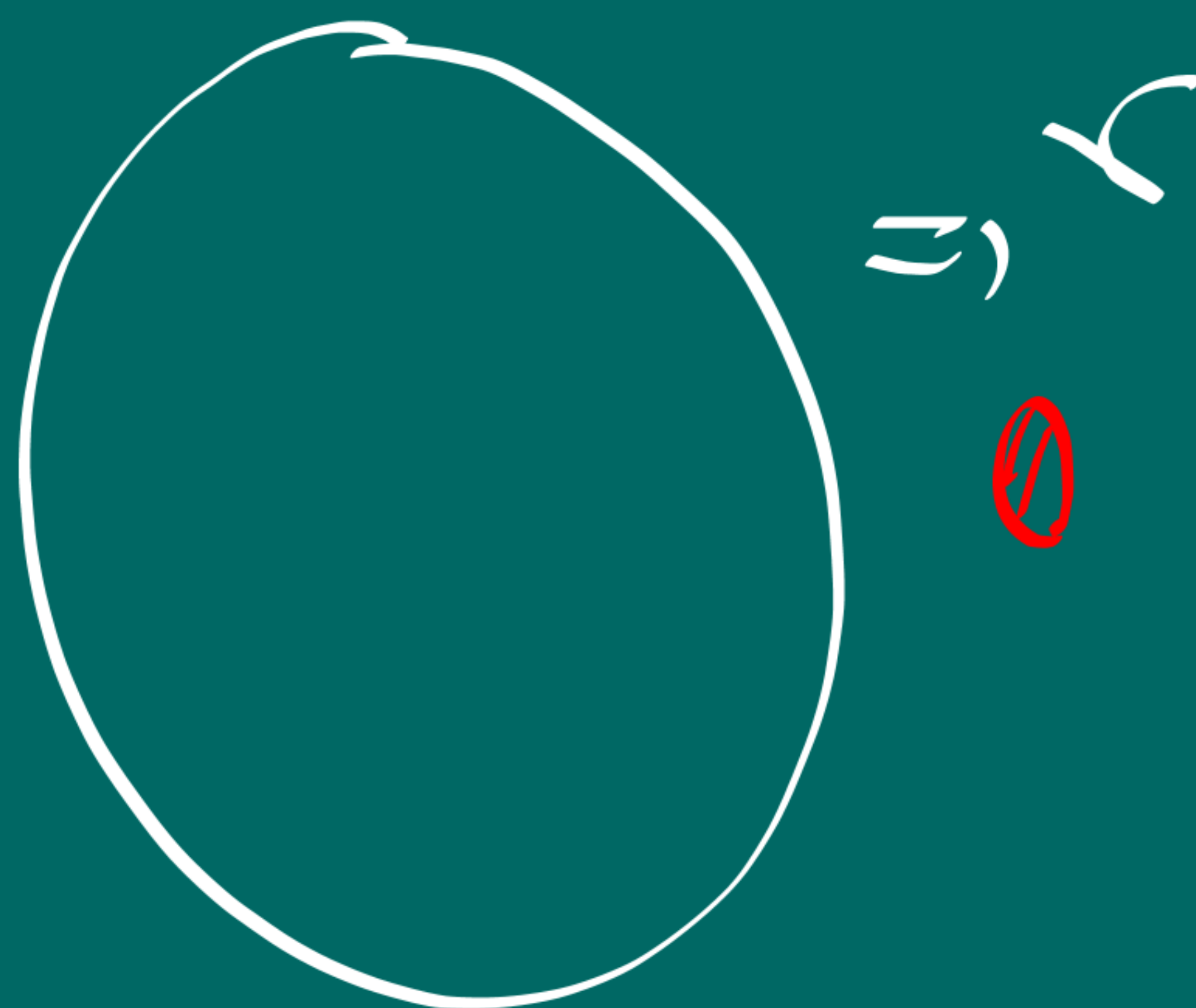
$\Rightarrow$ Non-abelian Gauge theory



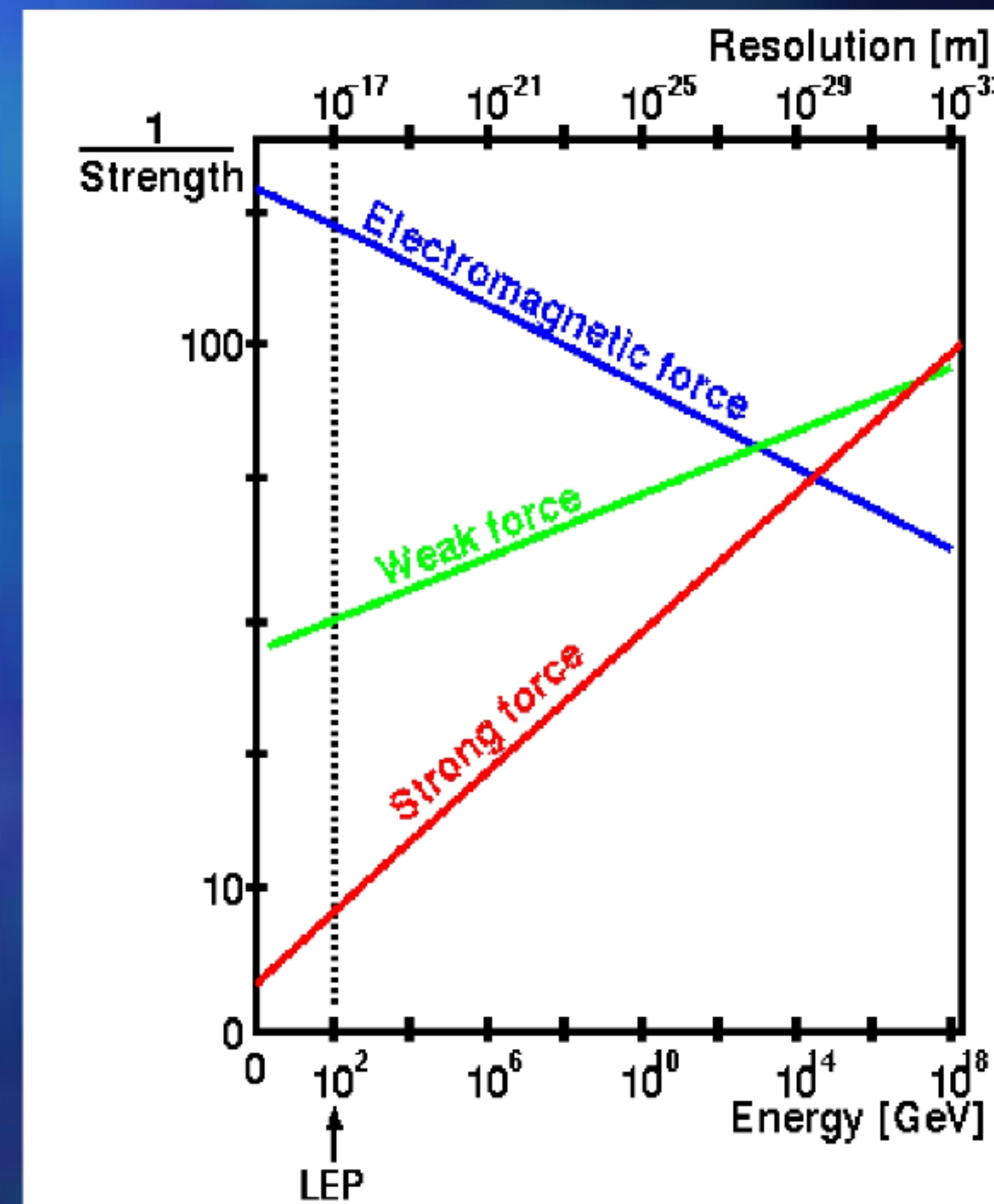
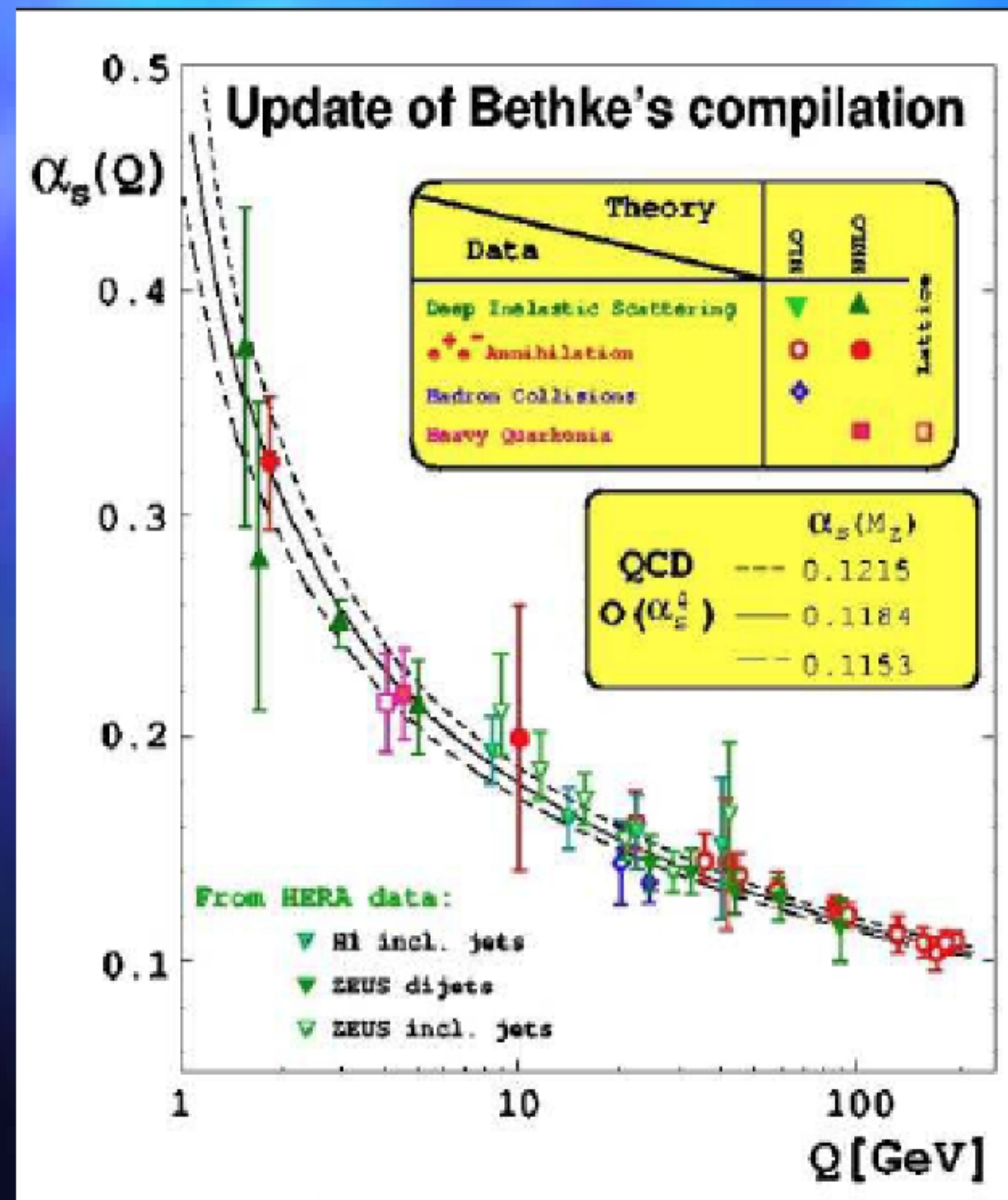
Strong Coupling



At very high Q^2
 $\alpha_s \sim 0$
 "Free quarks"

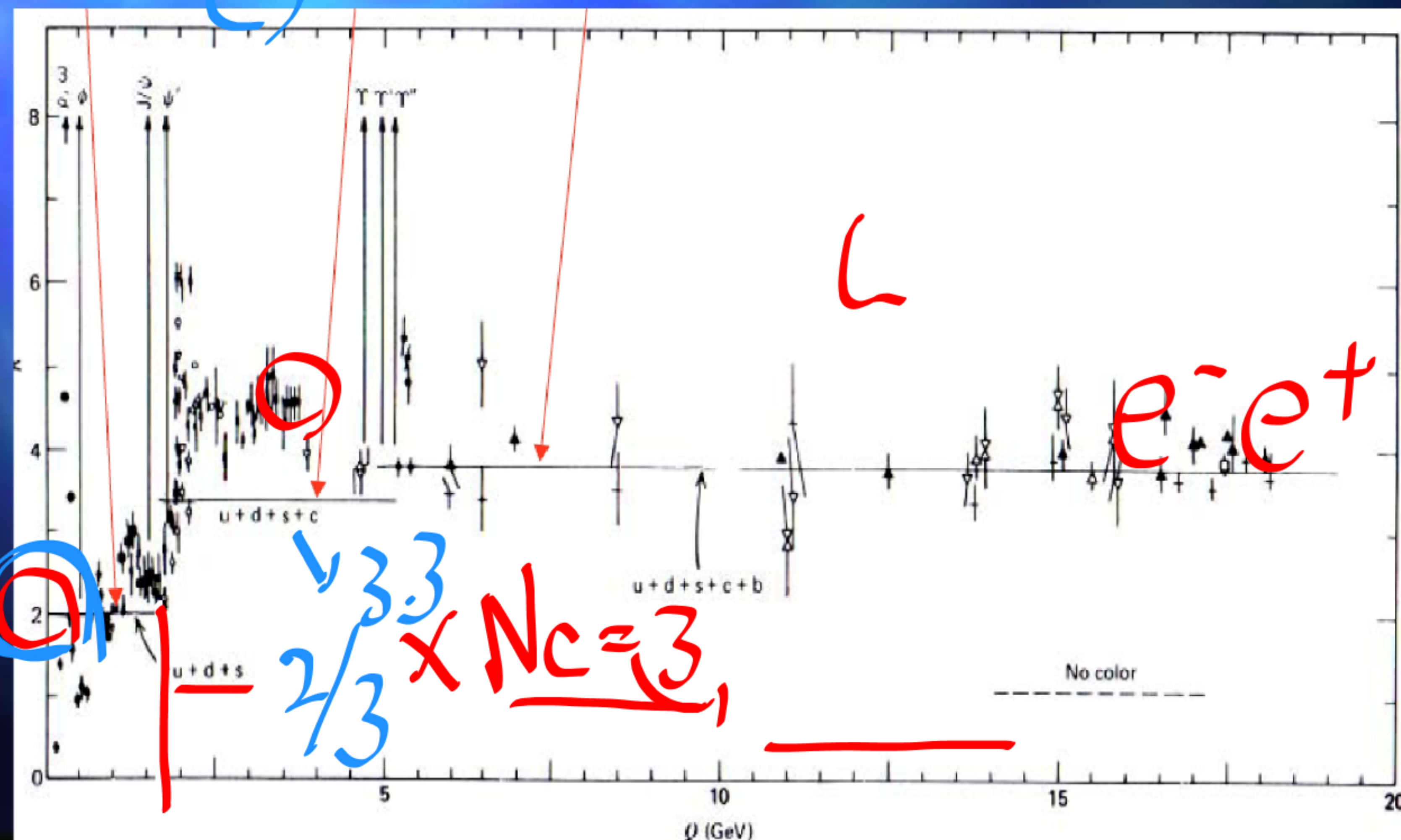
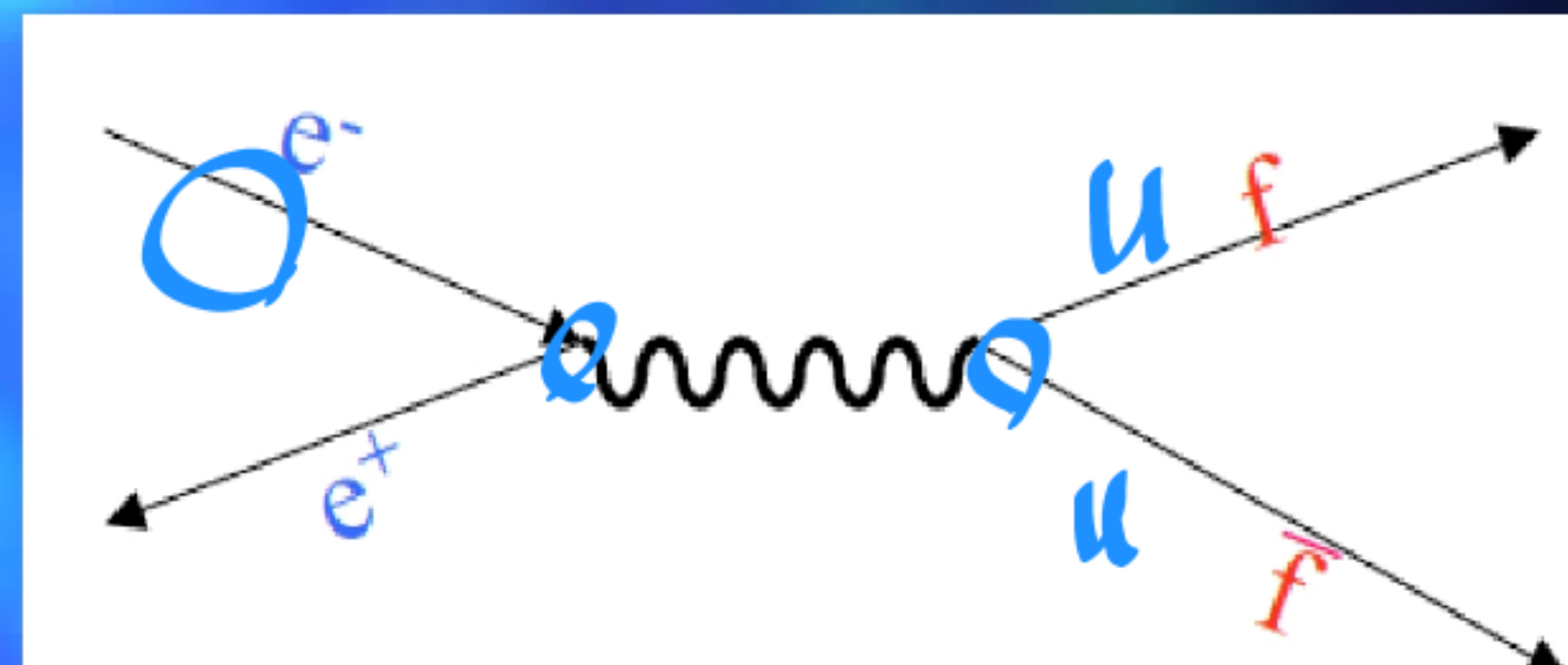


Strong Coupling



QCD Color

$$R = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$



$$e^-e^+ \rightarrow q\bar{q} (u\bar{u}, d\bar{d}, s\bar{s})$$

$$u \left(\frac{2}{3}\right)^2 \cdot \alpha_{em}^2$$

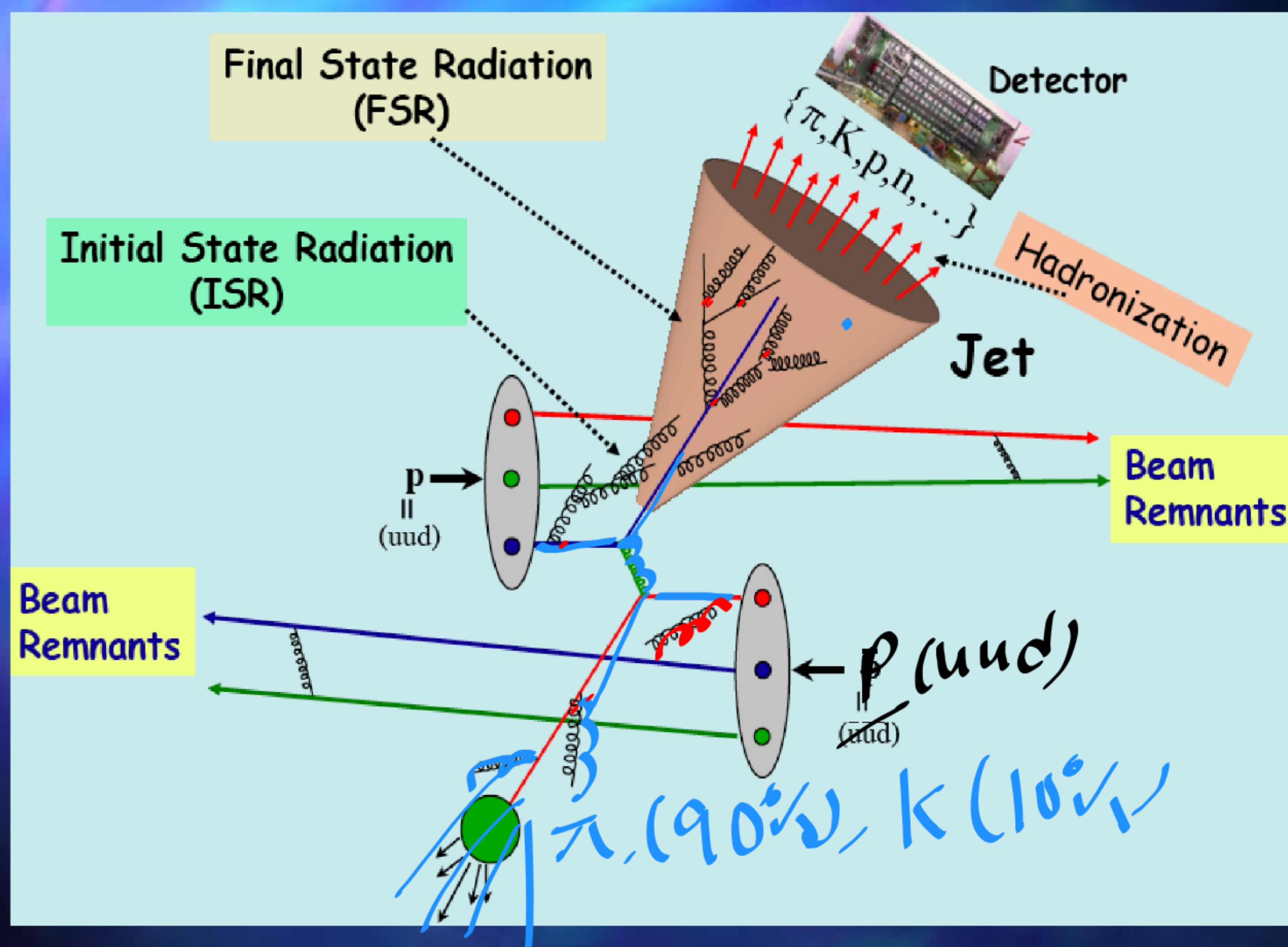
$$d\bar{d} \left(\frac{1}{3}\right)^2 \dots$$

$$s\bar{s} \left(\frac{1}{3}\right)^2 \dots$$

$$= \frac{6}{3} \alpha_{em}^2$$

$$= \frac{2}{3} \alpha_{em}^2 N_c \leftarrow 2$$

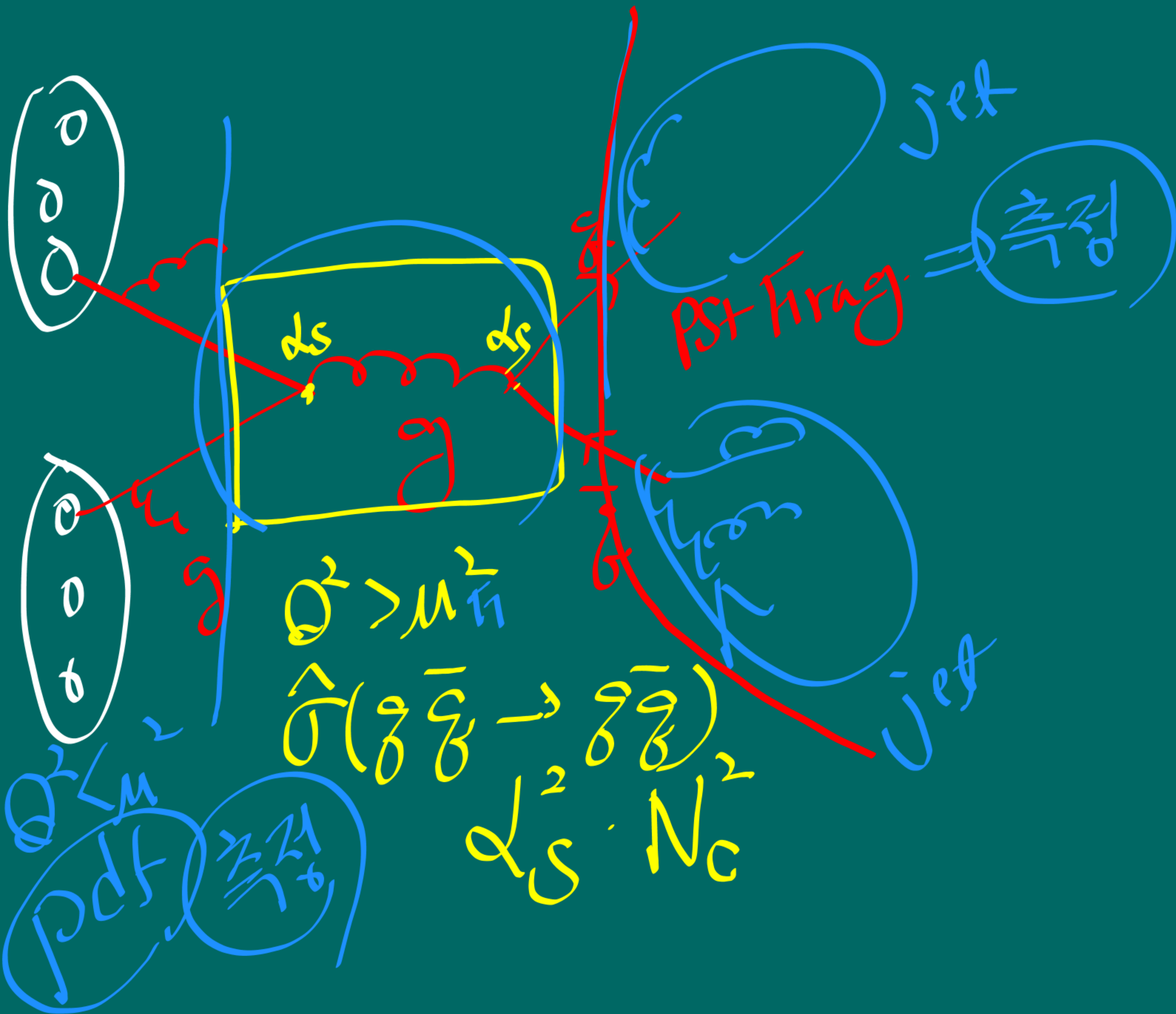
pp collisions



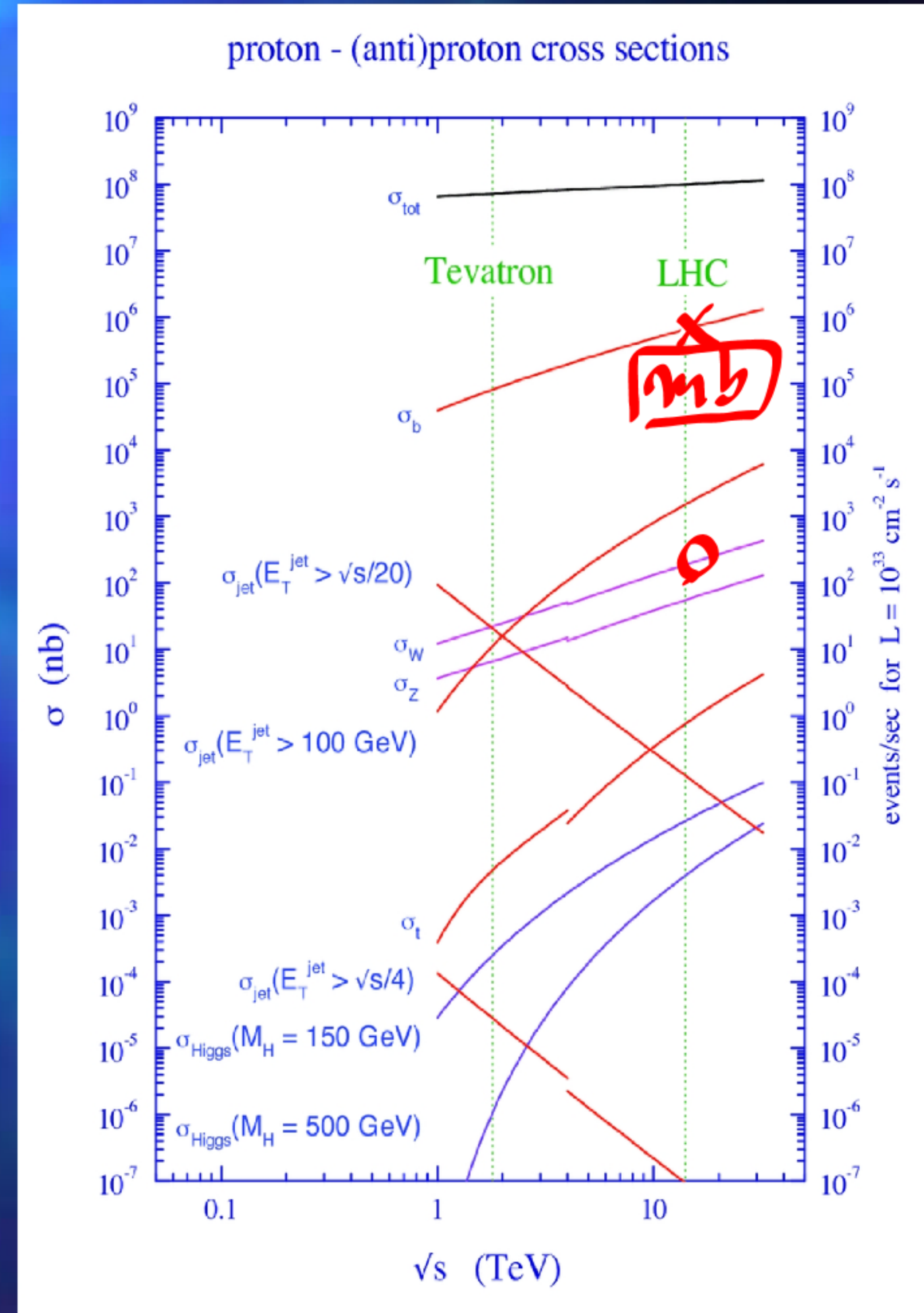
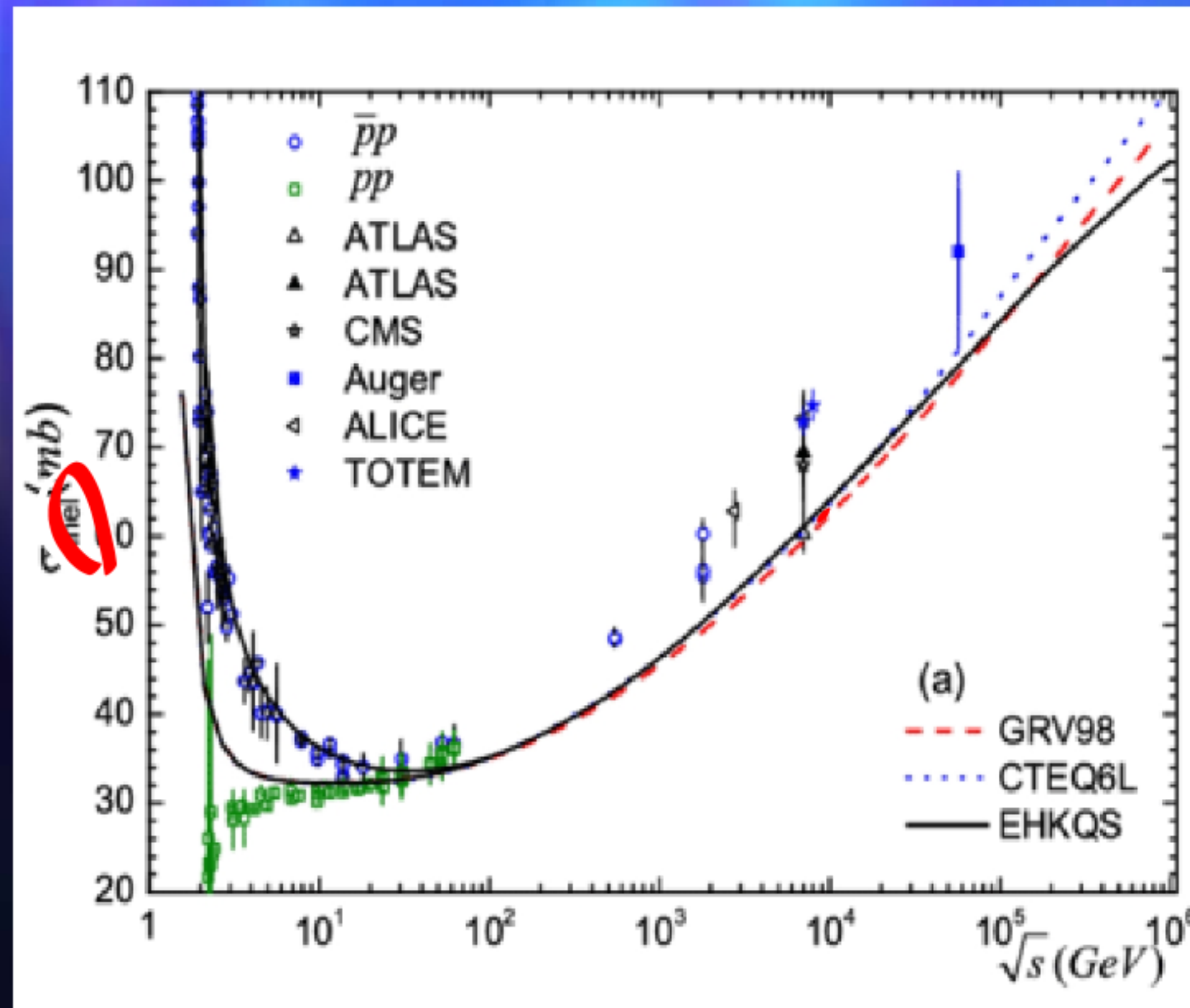
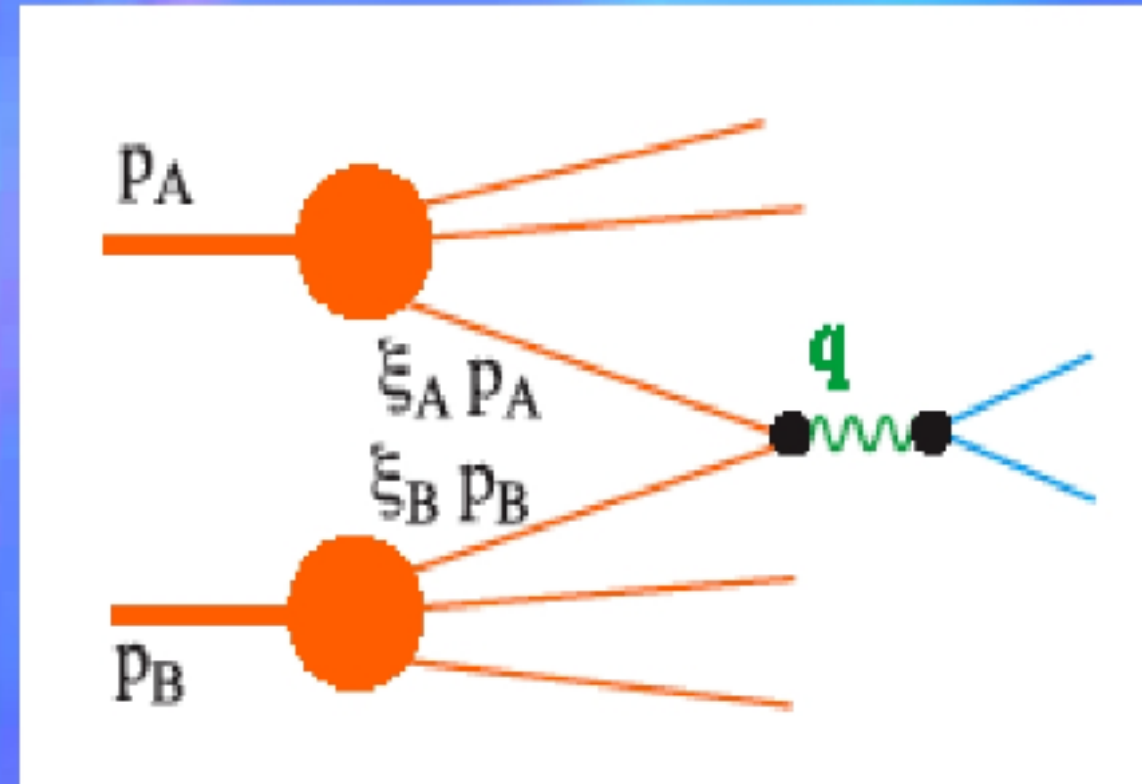
$$p + p \xrightarrow{g} g \bar{g} \rightarrow 2 \text{ jets}$$

$$\sigma(2 \text{ jets}) = ?$$

= a *impossible*



Productions at the LHC



$pp \rightarrow$ (total)
 $\sim 100 \text{ mb}$

Inel: $\sigma \sim 60 \text{ mb}$

$\alpha_s \sim 0.1$
 $\alpha_{em} \sim 0.01$
 $\alpha_{weak} \sim 10^{-5} \alpha_{em}$
(jets)



$$\begin{aligned}\sigma[b\bar{b}] &\sim 4b \\ \sigma(W) &\sim 10^5 \text{ pb} \\ \sigma(W)/\sigma(Z) &\sim 5 \\ \alpha_{em} &\sim 0.1 \sim 0.2 \\ \sigma(W) + \text{jet} &\sim \frac{1}{5}\end{aligned}$$

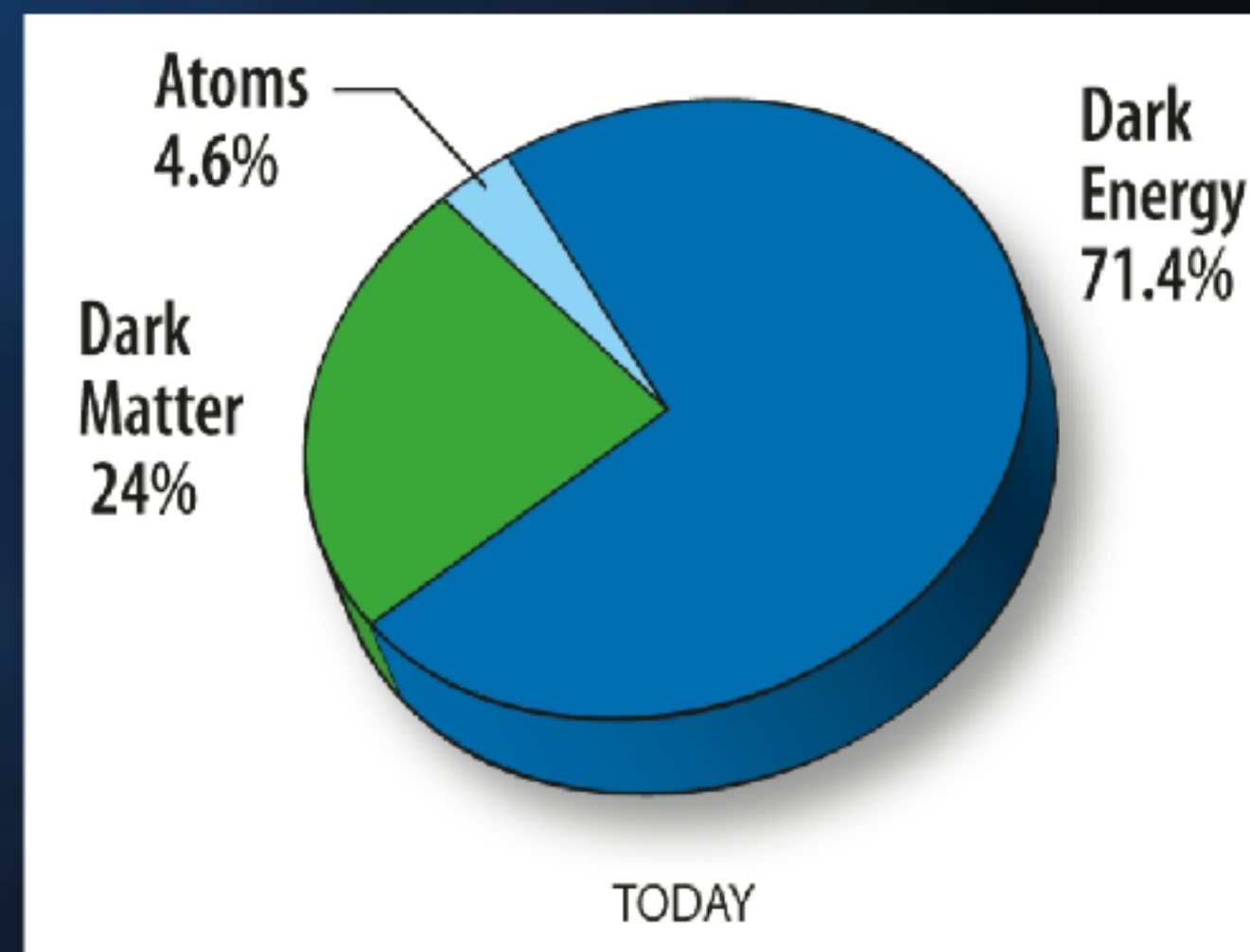
New Symmetry at the LHC?

"new force"

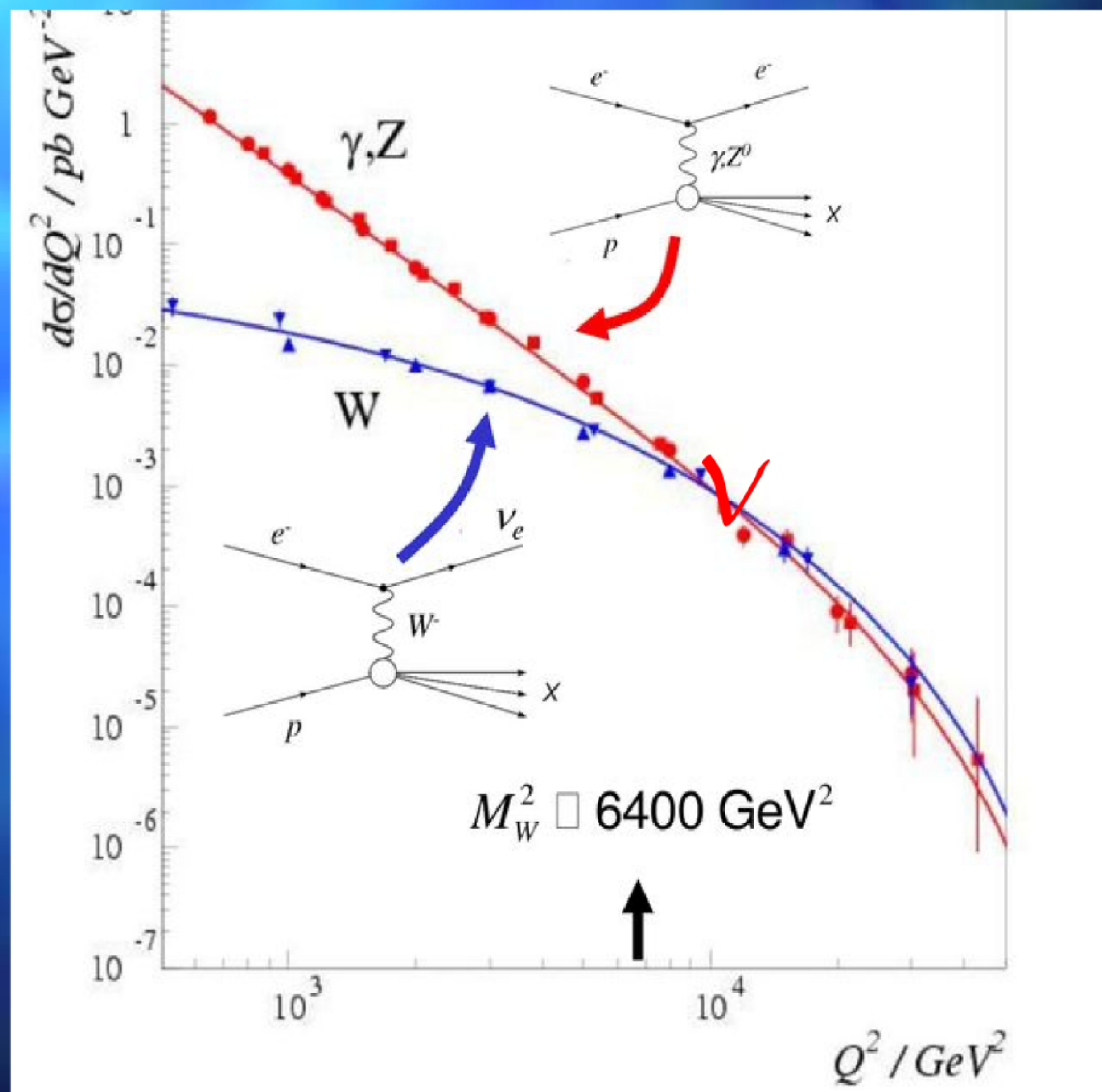
$\nu_n + N$

" γ osc."

- Dark matter? ✓
- Matter and Anti-matter asymmetry?
Where is anti-matter?
- Neutrino oscillation
- Where is my right-handed partner?



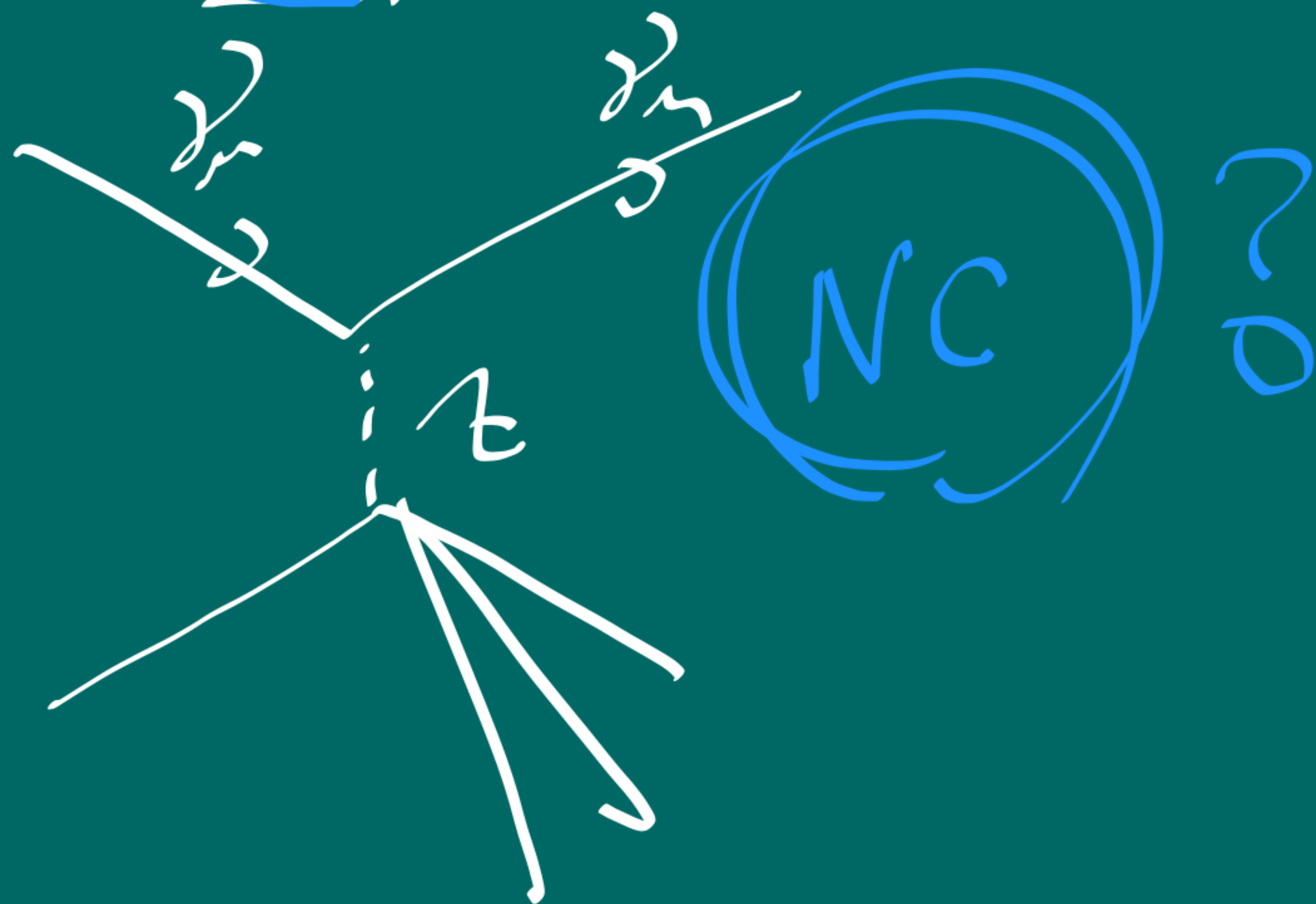
EM+Weak: Unified



$$\pi \downarrow \gamma_\mu + N \rightarrow e^- + X \quad (x)$$

$\mu^- + X$ (CC: new type of γ)
 ~ 1960

$$\sigma(W)/\sigma(Z) \sim 5.$$



How come even Leon
 Lederman miss
 the NC Z events?